



Quantum Threats to the TLS 1.3 Protocol

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Presenter's short résumé:

Field of research: quantum computing and its implications on cybersecurity

M.Sc. in Computer Science (ABD)

PG Certificate in Algorithms and Data Structures

PG Certificate in Software Engineering

B.Sc. in Physics/Biological Physics

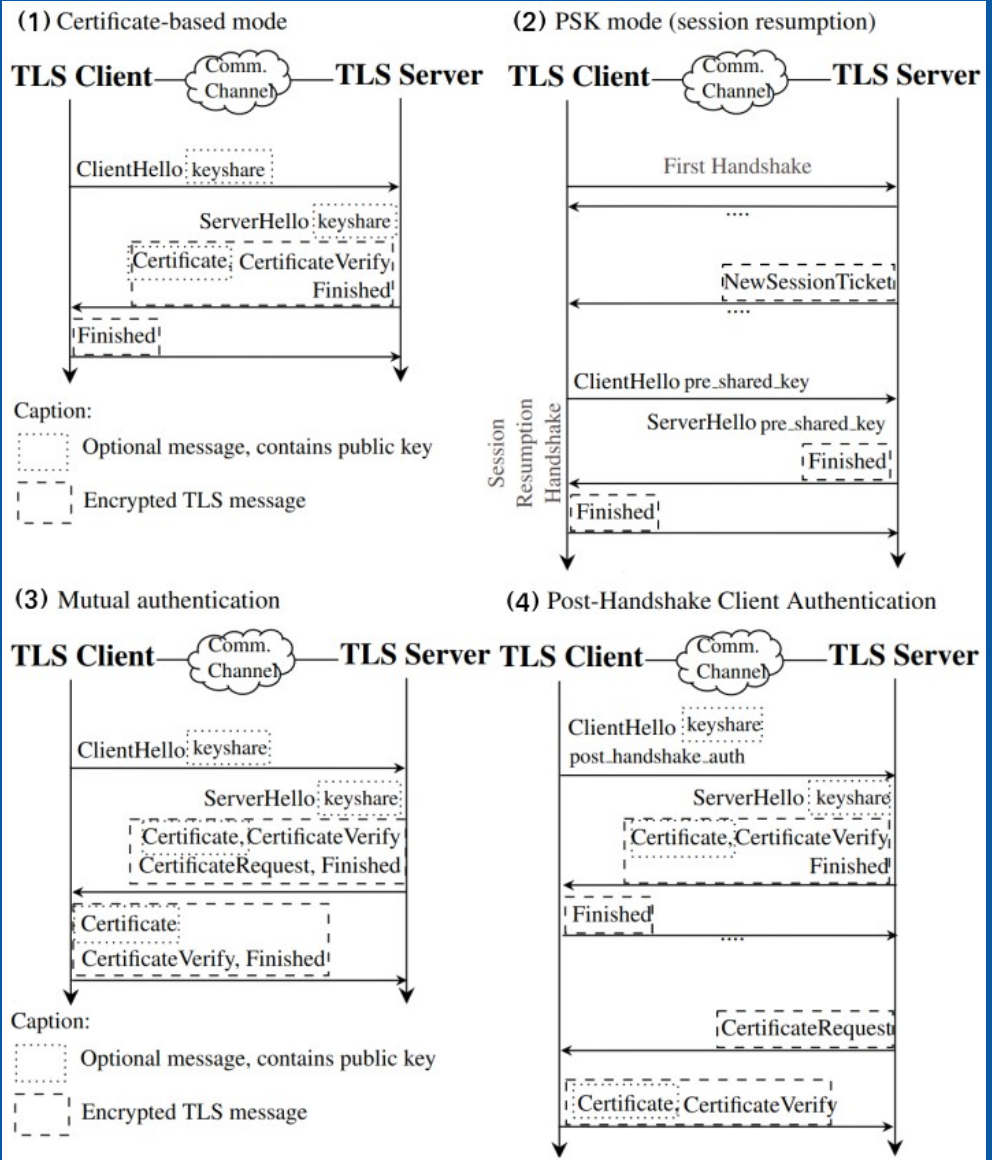


The TLS 1.3

- Transport Layer Security (TLS) 1.3, defined in RFC 8446 [3], is a notorious internet security protocol, present in more than 60% of all internet connections based on HTTPS [1], [2].
- It provides end-to-end secure channels, and, like many others, uses public key cryptography (PKC).

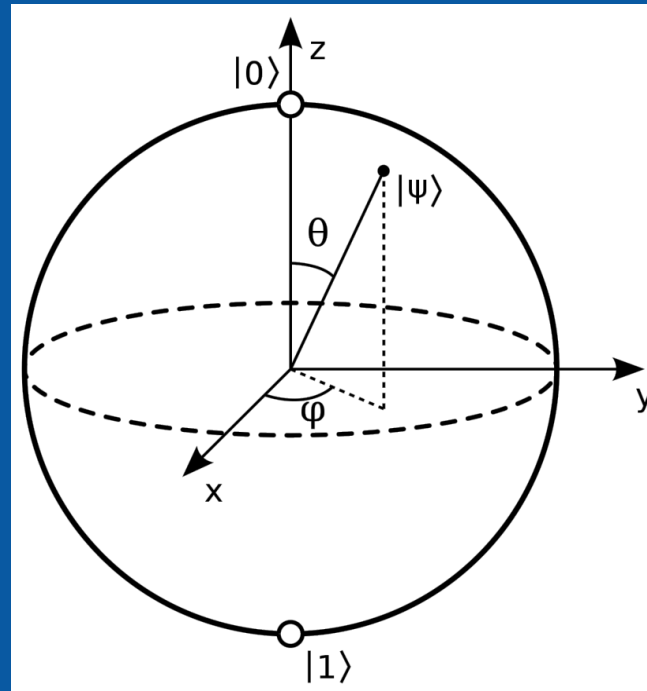


The TLS 1.3



The quantum computer

- Qubit: $|\psi\rangle = a |0\rangle + b |1\rangle$
- Normalization: $|a|^2 + |b|^2 = 1$



The quantum computer

- Register: $|q\rangle = |q_1\rangle \otimes |q_0\rangle = c_{00}|00\rangle + c_{01}|01\rangle + c_{10}|10\rangle + c_{11}|11\rangle$
- Gate model: $|q_n\rangle = G^n|q_{n-1}\rangle$
- Adiabatic model: applies an adiabatically slow time evolution of the state of the initial register (suitable for minimization problems)



Quantum algorithms for a PKC attack

— Shor's period finding algorithm, 1994 [4]: exponential speedup for solving factorization and DLP based problems [7], [14] with some newer implementations extending its usability to ECDLP [15], [16]

Best implementation of Shor's algorithm [17]	To break RSA-2048
$2n+1$ qubits	4097 qubits
Roughly $n^3 \log(n)$ gates	Billions of gates



Quantum algorithms for a PKC attack

- However, due to errors in the measurements, the calculations have to be done multiple times or circa 1568 noisy qubits have to be used to simulate each perfect logical qubit [19]
- Other things to consider are gate and coherence times. Adding gates makes the total execution time longer and it cannot be longer than the coherence time.

Superconducting	Neutral atoms	Trapped ions
25 ns	19 μ s	32 μ s



Quantum algorithms for a PKC attack

- There are also good adiabatic implementations for factoring algorithms [21], [22], [23], and for DLP [24]
- The table is adapted from [14], [17], [25]

Year	Key length	Algorithm
2001	4 bits	Shor
2012	5 bits	Shor
2012	16 bits	Adiabatic
2016	18 bits	Adiabatic
2018	19 bits	Adiabatic
2019	20 bits	Adiabatic
2020	41 bits	Adiabatic



Threat model

Quantum eras	Description
Pre-quantum	The era we are now, when QC are still not powerful enough for an effective break on cryptography;
Post-quantum initial	Quantum hardware is primitive and expensive, demanding a high skill level to break even short keys;
Post-quantum intermediate	Quantum hardware, price, and skill level to perform an attack are at an intermediate stage;
Post-quantum advanced	QC is fully established and available at a lower cost.



Threat model

Available resources	Skill level	Becomes a threat at which post-quantum era?
Governments and large organizations	3	Initial
	2	Intermediate
	1	Advanced
Hacker groups and small organizations	3	Intermediate
	2	Advanced
	1	∞
Individuals	3	Advanced
	2	∞
	1	∞



Attack scenarios

- Break confidentiality: passive or active attack
- Impersonation: active attack only



Attack scenarios:

Breaking confidentiality

— On certificate-based (server) mode:

- 1) collect Client and ServerHello, extracting the public keys epk_{CH} and epk_{SH} present in keyshare messages;
- 2) use Shor's algorithm for ECDLP to break the KEX: it computes the private key from epk_{CH} or epk_{SH} in order to recover the ephemeral private key;
- 3) use the recovered ephemeral key to derive the symmetrical keys, using the TLS Key Schedule [3], allowing to decrypt the whole communication



Attack scenarios: Breaking confidentiality

— On mutual authentication mode: same as previous



Attack scenarios: Breaking confidentiality

— On post-handshake authentication mode: same as previous



Attack scenarios:

Breaking confidentiality

— On PSK-based resumption mode:

- 1) use previous steps on the First Handshake;
- 2) use the recovered ephemeral key to derive the symmetrical keys used throughout the communication;
- 3) decrypt the NewSessionTicket message, recovering the ticket information;
- 4) use the recovered information to derive the resumption PSK;
- 5) use the PSK to derive the second handshake's symmetrical keys



Attack scenarios: Impersonation

— On certificate-based (server) mode:

- 1) collect Client and ServerHello, extracting the public keys epk_{CH} and epk_{SH} present in keyshare messages;
- 2) use Shor's algorithm for ECDLP to break the KEX: it computes the private key from epk_{CH} or epk_{SH} in order to recover the ephemeral private key;
- 3) use one of the recovered private keys to derive the symmetrical keys, using the TLS Key Schedule [3], and then decrypt the authentication messages;



Attack scenarios: Impersonation

4) use one of the alternatives to attack the Certificate message and return the certificate private key:

- use Shor's algorithm or adiabatic QC to solve the factorization problem on the RSA public key; or
- use Shor for ECDLP on the public key based on elliptic curves



Attack scenarios: Impersonation

— On mutual authentication mode: same as for server authentication mode, but the attacker can choose to impersonate server or client. The main difference is the target Certificate message (from the server or client)



Attack scenarios: Impersonation

— On post-handshake authentication mode: impersonate the server is similar to the previous modes, but to impersonate client:

- 1) check the presence of the `post_handshake_auth` extension;
- 2) use the steps 1-2 of the Certificate-based authentication (server);
- 3) decrypt the communication using the recovered symmetric keys, searching for the `CertificateRequest` message;



Attack scenarios: Impersonation

4) use one of the alternatives to attack the client's Certificate message and return the private key:

- solve the factorization problem with Shor's algorithm or adiabatic QC; or
- use Shor for ECDLP instead



Attack scenarios: Impersonation

— On PSK-based resumption mode: similar steps as used for server authentication mode, but the steps should be applied to the First Handshake. Having the PSK information, the attacker can impersonate both peers. However, PSKs duration time can be limited up to 7 days [3], so the attack window is limited



Attack scenarios: SNDL resources

Site	1h of captured packets (MB)	Expected storage cost for 24h (GB)	Expected storage cost for 1y (TB)
Instagram.com	835.4	19.6	7
Youtube.com	723.7	17	6
Amazon.com	272.6	6.4	2.3
Gmail.com	124.8	2.9	1



Mitigation: QKD

- Quantum cryptography: the use of physics to create a different class of cryptography. QKD is the most common.
- QKD pros:
 - the mathematics of quantum mechanics guarantees the key exchange is perfectly secure;
 - the no-copy property of quantum mechanics ensures there will be no man-in-the-middle attack, because a measurement of the system would modify it



Mitigation: QKD

- QKD cons:
 - no-copy property makes it impossible to re-rout or broadcast a qubit, making it necessary special network channels and hardware;
 - it is affected by decoherence and most of the current QKD systems do not allow travels further than 200 km [28];
 - implementation costs immensely for large networks. Making it a viable solution only for limited use cases



Mitigation: PQC

- PQC: classical devices with math problems hard for a QC to solve.
- NIST, 2022, announced 4 algorithms promised to be quantum-safe:
 - CRYSTALS-Kyber [29], a key encapsulation mechanism that can be used to establish symmetric keys;
 - CRYSTALS-Dilithium [30], a DSA;
 - Falcon [31], another DSA;
 - SPHINCS+ [32], a hash-based DSA



Mitigation: PQC

- PQC pros:
 - more viable for KEX than QKD;
 - there are also implementations for digital signatures
- PQC cons:
 - have been tested for years, but it's still impossible to tell for how long they will remain unbreakable [28];
 - Most of them are slower than the traditional algorithms for KEX or digital signature, impacting in slower page loads and a risk of packet loss



Mitigation: Hybrid

- Hybrid implementations combine pre- and post-quantum cryptography.
- E.g.:
 - Combining the output of a pre- and a post-quantum algorithm with XOR in a KEX;
 - Creating 2 signatures, one with a pre- and another with a post-quantum algorithm



Mitigation: ROI

- Key length requires more gates, hence, longer execution time.
- Adding encryption layers, since the QC has to be used for each one of them [25];
- PFS, PCS, key management, short-term certificates can diminish the data recovered on each attack or shorten the window for an attack;
- Because the amount of storage necessary for a SNDL attack is huge, company have to be aware of social engineering attacks



Conclusion

- The paper exposed:
 - The threats of QC on TLS 1.3;
 - Existing quantum algorithms for an attack against PKC;
 - Achievements of these algorithms;
 - Detailed steps for a quantum attack in different handshake modes;
 - Approximate requirements for SNDL;
 - Mitigation methods



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