

Extending ASP Based Reasoning to Expressive Constructive Description Logics

Loris Bozzato

DKM - Data and Knowledge Management Research Unit,
FBK, Fondazione Bruno Kessler - Trento, Italy

Email: <surname>@fbk.eu

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Contact

Loris Bozzato [bozzato\[at\]fbk.eu](mailto:bozzato@fbk.eu)

Researcher @ DKM - Data and Knowledge Management Research Unit
FBK - Fondazione Bruno Kessler, Trento, Italy

<https://dkm.fbk.eu/people/profile/bozzato>

Research interests (KRR)

- Context representation and reasoning
- Defeasibility in description logics
- Constructive semantics for description logics

Constructive description logics

Constructive interpretations of description logics

- **Goal:** develop reasoning tools for Constructive DLs
- **Approach:** use connections to Answer Set Programming (ASP)

→ we want to highlight this line of research and the challenges in its extension to more expressive DLs

Constructive DL \mathcal{ELc} [Bozzato, 2018]

- Information term (IT) semantics for \mathcal{EL}
- Restriction of \mathcal{BCDL} [Ferrari et al., 2010]

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Information terms $\text{IT}_{\mathcal{N}}(K)$ [Miglioli et al., 1989]

Structured objects that **constructively justify the truth** of a formula K

Realizability $\mathcal{M} \triangleright \langle \alpha \rangle K$

Truth of K in a model \mathcal{M} **justified w.r.t. α**

Constructive DL \mathcal{ELC} [Bozzato, 2018]

- Information term (IT) semantics for \mathcal{ELC}
- Restriction of \mathcal{BCDL} [Ferrari et al., 2010]

Information terms $IT_{\mathcal{N}}(K)$ [Miglioli et al., 1989]

Structured objects that **constructively justify the truth** of a formula K

Realizability $\mathcal{M} \triangleright \langle \alpha \rangle K$

Truth of K in a model \mathcal{M} **justified w.r.t. α**

E.g.: Truth of $\exists R.C(a)$ in \mathcal{M} justified by IT (b, α) s.t.

- $\mathcal{M} \models R(a, b)$ and
- α justifies truth of $C(b)$

Task

Compute **information terms** of input KB Γ in \mathcal{EL}

Idea

Use relations across IT and Answer Sets semantics

[Fiorentini and Ornaghi, 2007] on propositional nested expressions

→ We extend these results to \mathcal{ELC} formulas

Result (sketch) [Bozzato, 2018]

The (minimal) **information terms** for a set Γ of \mathcal{EL} formulas can be obtained by computing the **answer sets** of input formulas in Γ

ASP based generation of IT [Bozzato, 2018]

- Model generating rewriting (P_1)
Generates interpretations for input \mathcal{EL} formulas (fixed roles assertions)
- Model generating rewriting (P_1^f)
Generates interpretations for input \mathcal{EL} formulas (with existential fillers)
- IT generating rewriting (P_2)
Retrieves IT as complex terms, using definition of ITs

Asp-it prototype

ASP based IT generator for OWL EL ontologies

<https://github.com/dkmfbk/asp-it>

Current challenges:

- Semantic extension to **expressive DL operators**
- **ASP translation extension** to expressive DLs
- **Further reasoning tasks:** manipulation of ITs
- **Implementation and application** to real use cases

Extension to \mathcal{EL}_{\perp} [Bozzato and Fiorentini, 2020]

- **Constructive DL \mathcal{ELc}_{\perp} :** IT semantics for \mathcal{EL}_{\perp}
- Formal relation between **ASP and IT semantics in \mathcal{ELc}_{\perp}**



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