

# Contingent Planning using Counter-Examples from a Conformant Planner

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# Context

- Search and rescue missions with local observations
- Uncertain environment
- Partial observability
- Plan  $\rightarrow$  action sequence leading to a goal from an initial state
- Planning under uncertainty
- Find a plan allowing to reach a goal by performing observations of the environment



# State of the art

- Replanning
  - Compute a first plan without considering uncertainties and replan if an unexpected event occurs during the execution of the plan
    - FF-Replan (Yoon et al., 2007)
- Uncertainty modeled by probabilities on state transitions and actions effects
  - Optimal policy applying the best action to each state
  - **Markov Decision Processes** (MDPs) (Puterman, 2014)
  - **Partially observable MDP** (Kaelbling et al., 1998)
    - Belief states and observations to update the belief
  - In the problems we are trying to solve, it is difficult to specify probabilities
- Uncertainty modeled by a set of possible initial states
  - **Conformant Planning** (Bertoli et al., 2001)
    - Compute a plan (an action sequence) solving the problem **whatever the possible initial states** without observation
    - Conformant-FF (Brafman and Hoffmann, 2004) , CPCES (Grastien et al., 2017)
  - **Contingent Planning** (Hoffmann and Brafman, 2005)
    - Compute a **Conditional plan** containing branches allowing an **online decision making** conditioned by the result of **observations**
    - Contingent-FF (Hoffmann and Brafman, 2005) , CLG (Albore et al., 2011)
    - Compilation approaches (Brafman and Shani, 2012)

# Motivations

- Contingent planning has computation time issue
- The objective is to reduce this complexity
  - Compilation based approaches (Brafman and Shani, 2012)
- Reduces the contingent plan computation complexity by using a conformant planner
- Allows subproblems computations without considering the costly computation of observations

# Approach

## Idea

- CPCES Conformant Planner (Grastien et al., 2017), in case of failure:
  - Returns a **counter-example**
  - Returns a **plan solution of some of the possible initial states**
- Give the problem to solve to CPCES
- In case of failure, use the **counter-example** and the **failing plan** to determine **which observation** perform and **when**
- Split the problem in **subproblems** taking into account the observation to **reduce uncertainty** in the subproblems
- Use the Conformant Planner to **iteratively** solve these subproblems

- 1 Formalism
- 2 Algorithm Principle
- 3 Results
- 4 Conclusion
- 5 Approach Improvements

# Plan

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# Formalism

## Problem $(\mathcal{L}, \mathcal{O}, I, G)$

- $\mathcal{L} = \{p_1, \dots, p_n\}$  is a finite set of **propositions**
- $\mathcal{W} = 2^{\mathcal{L}}$  is the set of possible **world states**
- $\mathcal{O}$  is a finite set of **operators**, divided in **action** sets  $A$  and **observation** sets  $O$
- Each operator  $op \in \mathcal{O}$  is defined by **preconditions**  $pre(op) \subseteq \mathcal{L}$  and a **set of effects**  $eff(op)$
- $I \subseteq \mathcal{W}$  is the set of **possible initial states**
- $G \subseteq \mathcal{L}$  is the set of propositions defining the **goal**



# Formalism

## Action application in a world state

- $a \in A$  is *applicable* in the state  $s \in \mathcal{W}$  iff  $pre(a) \subseteq s$
- An effect  $e \in eff(a)$  is defined by a triplet  $(con(e), add(e), del(e))$
- If  $a$  is applicable in  $s$ , then the application of  $a$  results in a state  $T(s, a)$  with  $T$  the **transition function** such that:

$$T(s, a) = s - \bigcup_{e \in eff(a) \text{ s.t. } con(e) \subseteq s} del(e) \cup \bigcup_{e \in eff(a) \text{ s.t. } con(e) \subseteq s} add(e)$$

## Application of an observation in a world state

- $o \in O$  is applicable in  $s \in \mathcal{W}$  iff  $pre(o) \subseteq s$
- $eff(o) \in \mathcal{L}$  is defined by the **truth value** of the observed proposition
- The application of  $o$  in  $s$  has **no effect** on  $s$ ,  $T(s, o) = s$

# Formalism

## Belief state

- **Belief**  $\mathcal{B} = \{s_1, \dots, s_n\} \subseteq \mathcal{W}$  is the propagation of the possible initial states

## Action and Observation application in a Belief

- An action  $a \in A$  is applicable in a belief  $\mathcal{B}$  if  $a$  is applicable in each state of  $\mathcal{B}$ . The application of  $a$  in  $\mathcal{B}$  consists in applying  $a$  to each state of  $\mathcal{B}$
- An observation  $o \in O$  is applicable in a belief  $\mathcal{B}$  if  $o$  is applicable in each state of  $\mathcal{B}$ . The application of  $o$  in  $\mathcal{B}$  results in a new belief in which the states that does not contain the observed proposition are removed

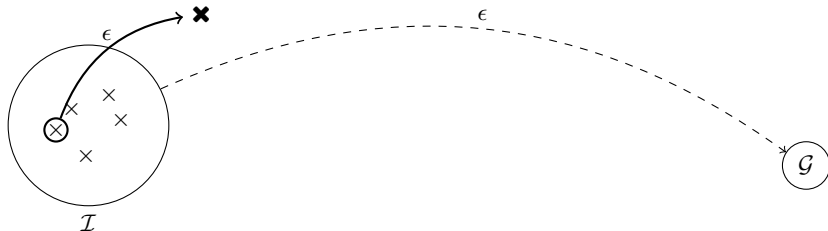
## Conditionnal Plan

- **Operators Graph**, leading an initial belief to a **goal** belief
- **Branchings** in the graph corresponds to **observations results**, whether the observed properties are in the current belief or not

# Plan

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# CPCES (Grastien et al., 2017)



CPCES checks if the empty plan is solution

## Legend

x

possible initial state

----->

plan proposed to Z3

○ → x

counter-example found by Z3

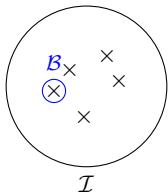
→

plan computed by FF

a

returned element

## CPCES (Grastien et al., 2017)



CPCES selects a counter-example state in which the empty plan fails

## Legend



possible initial state



plan proposed to Z3



counter-example found by Z3

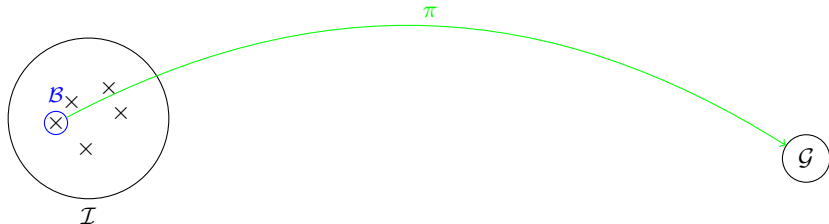


plan computed by FF



returned element

## CPCES (Grastien et al., 2017)



FF is used to compute a plan  $\pi$  from the set of considered states  $\mathcal{B}$

## Legend

x

possible initial state

- - - - -&gt;

plan proposed to Z3

○ → x

counter-example found by Z3

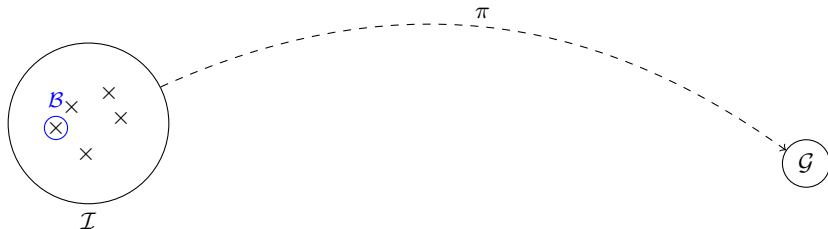
→

plan computed by FF

a

returned element

## CPCES (Grastien et al., 2017)



The SAT-solver Z3 checks if  $\pi$  is valid for the complete set of initial states

## Legend

x

possible initial state

-----&gt;

plan proposed to Z3

○ → ✕

counter-example found by Z3

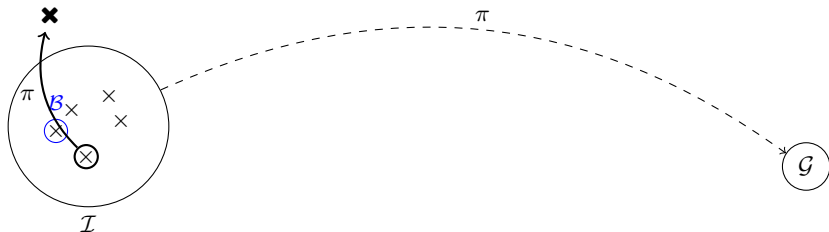
—————&gt;

plan computed by FF

a

returned element

## CPCES (Grastien et al., 2017)



If  $\pi$  is valid then it is returned, else a counter-example is found

## Legend

x

possible initial state

- - - - -&gt;

plan proposed to Z3

○ → x

counter-example found by Z3

→

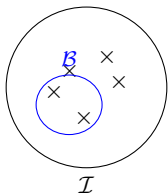
plan computed by FF

a

returned element



## CPCES (Grastien et al., 2017)



CPCES adds the counter-example to  $\mathcal{B}$  and iterates until a conformant plan is found

## Legend

x

possible initial state

- - - - -&gt;

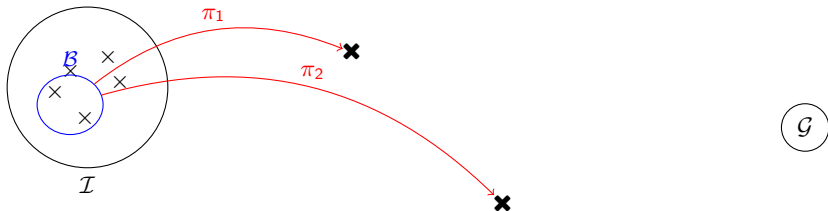
plan proposed to Z3

counter-example found by Z3

plan computed by FF

returned element

## CPCES (Grastien et al., 2017)

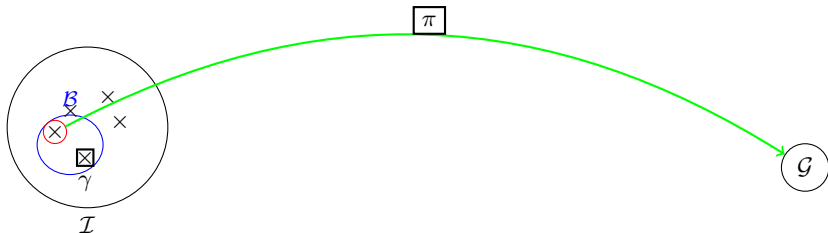


If FF cannot compute a plan, then there is no conformant plan

## Legend

×	possible initial state	----->	plan proposed to Z3
○ → ×	counter-example found by Z3	—————>	plan computed by FF
<span style="border: 1px solid black; padding: 2px;">a</span>	returned element		

## CPCES (Grastien et al., 2017)



The last counter-example and the previous plan are then returned

## Legend

x

possible initial state

- - - - -&gt;

plan proposed to Z3

○ → x

counter-example found by Z3

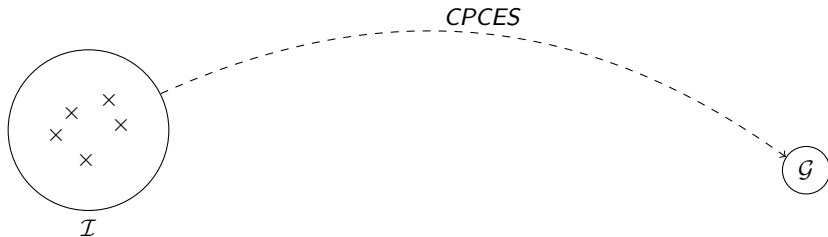
→

plan computed by FF

a

returned element

# Contingent Process



CPCES is called to compute a conformant plan

## Legend

×

state

----->

application

----->

failure

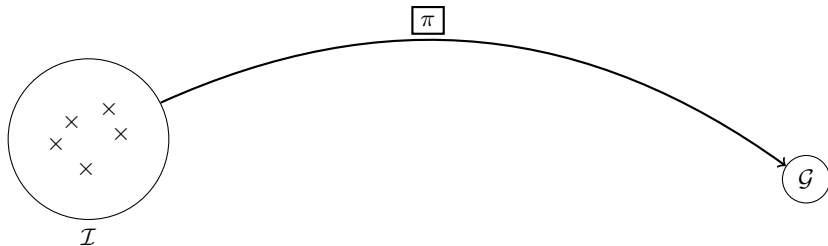
----->

success

$\boxed{a}$

returned element

# Contingent Process



If CPCES finds a conformant plan then it is returned

## Legend

×

state

----->

application

----->

failure

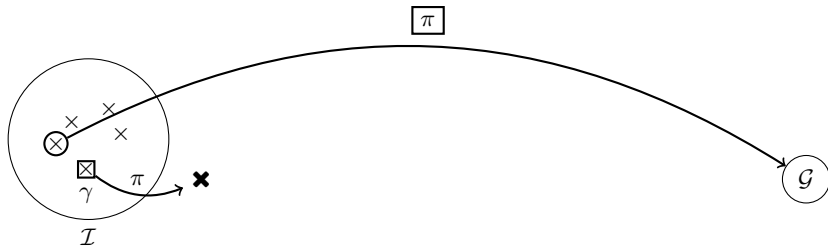
----->

success

$a$

returned element

# Contingent Process



Else a counter-example and a failing plan are extracted

## Legend

x

state

----->

application

----->

failure

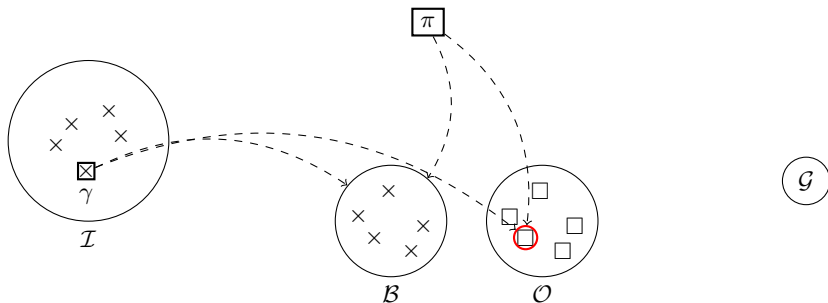
----->

success

$a$

returned element

# Contingent Process



Identify the observation to perform and in which belief

## Legend

x

state



success

- - - - -&gt;

application

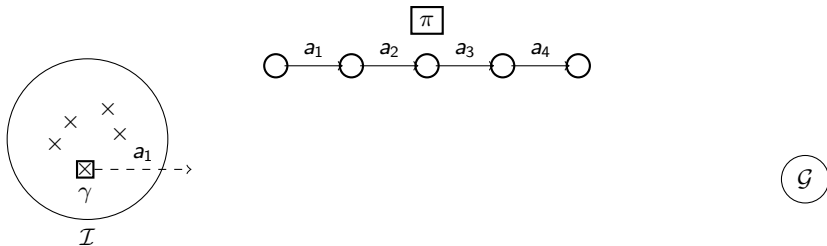


returned element



failure

# Contingent Process



Identification of the action of  $\pi$  that fails in  $\gamma$

## Legend

×

state

----->

application

----->

failure

----->

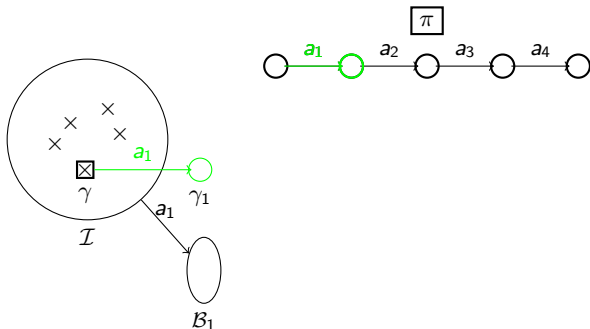
success

$a$

returned element



# Contingent Process



If the action is applicable, apply it to  $\mathcal{I}$  to keep track of the beliefs

## Legend

x

state

- - - - -&gt;

application

- - - - -&gt;

failure

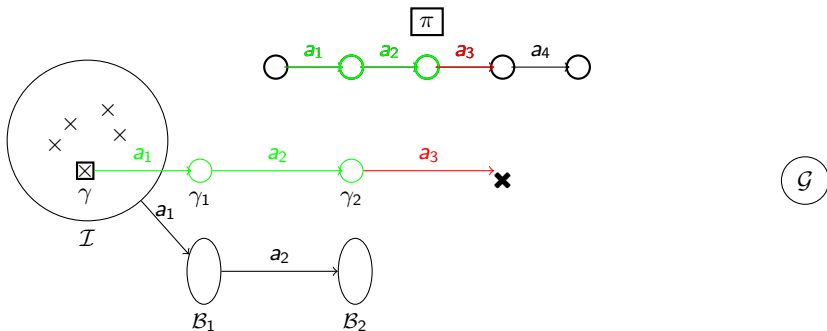


success

a

returned element

# Contingent Process



The process iterates until an action is not applicable

## Legend

$\times$

state



success

--->

application

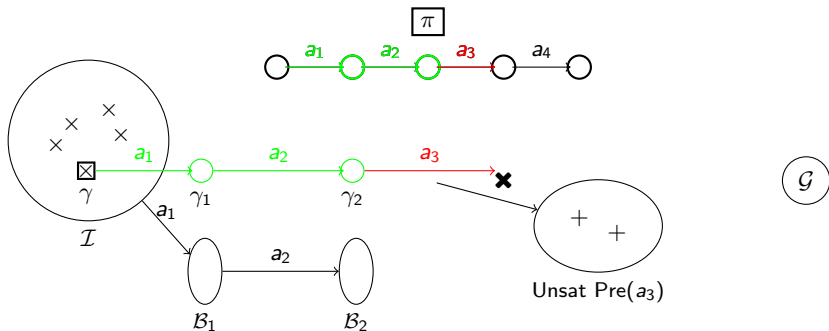
$a$

returned element

—>

failure

# Contingent Process



Extract the propositions in the preconditions of  $a_3$  that fail

## Legend

$\times$

state

----->

application

----->

failure

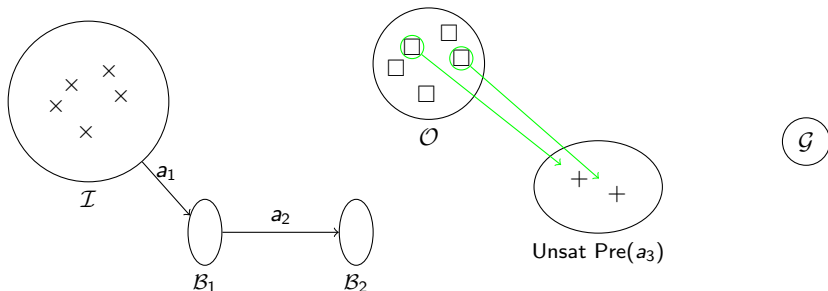
----->

success

$a$

returned element

# Contingent Process



Extract the observations able to observe one of the unsatisfied propositions

## Legend

x

state

- - - - -&gt;

application

- - - - -&gt;

failure

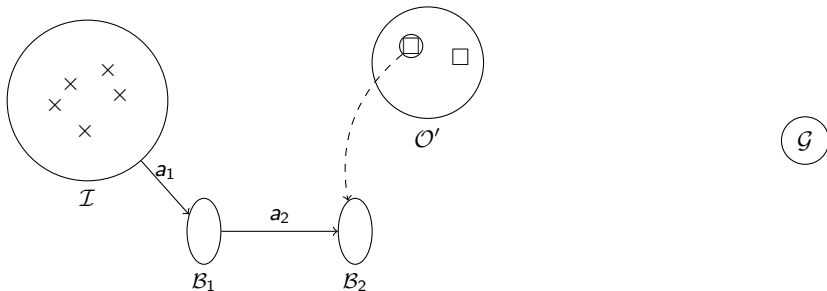


success

a

returned element

# Contingent Process



Apply a first observation to each belief

## Legend

x

state

- - - - -&gt;

application

-&gt;

failure

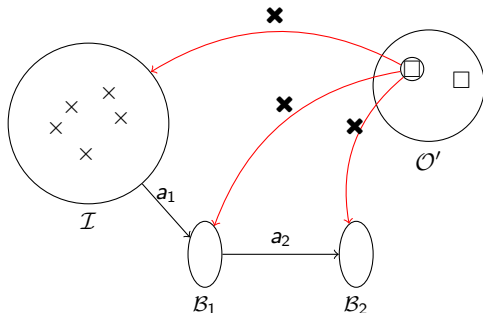
-&gt;

success

a

returned element

# Contingent Process



The current observation is not applicable in any belief

## Legend

x

state

- - - - -&gt;

application

- - - - -&gt;

failure

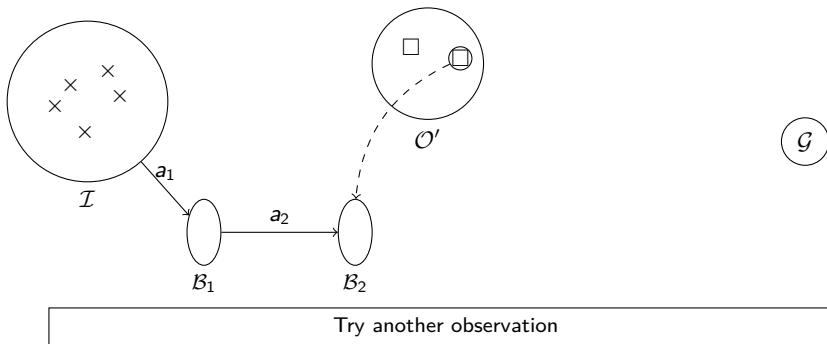
→

success

a

returned element

# Contingent Process



## Legend

x

state

- - - - -&gt;

application

- - - - -&gt;

failure

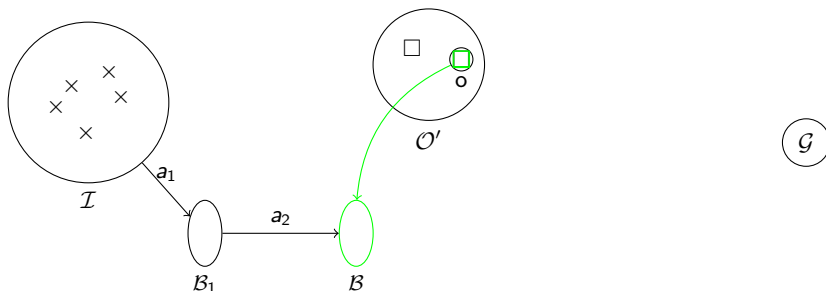
→

success

 $a$ 

returned element

# Contingent Process



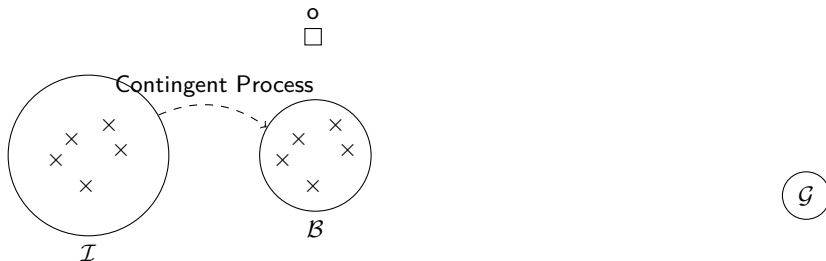
If the observation is applicable, the observation and belief are extracted

## Legend

$\times$	state	$\longrightarrow$	success
$-----\rightarrow$	application	$\boxed{a}$	returned element
$\longrightarrow$	failure		



# Contingent Process

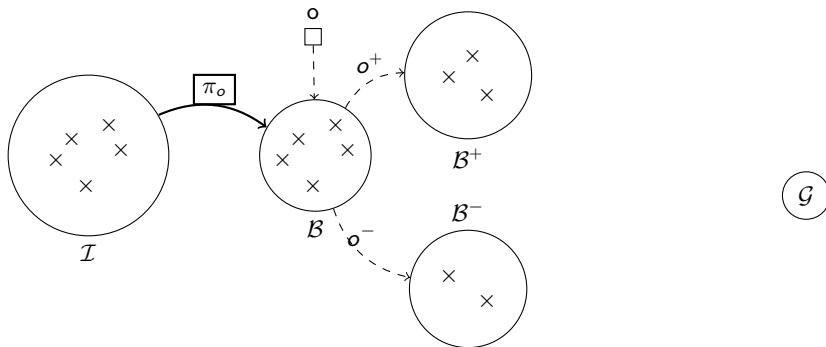


Restart the Contingent process to compute a plan leading to the observation

## Legend

×	state	→	success
---	application	$\boxed{a}$	returned element
→	failure		

# Contingent Process



Split the belief considering the observation

## Legend

x

state

- - - - -&gt;

application

- - - - -&gt;

failure

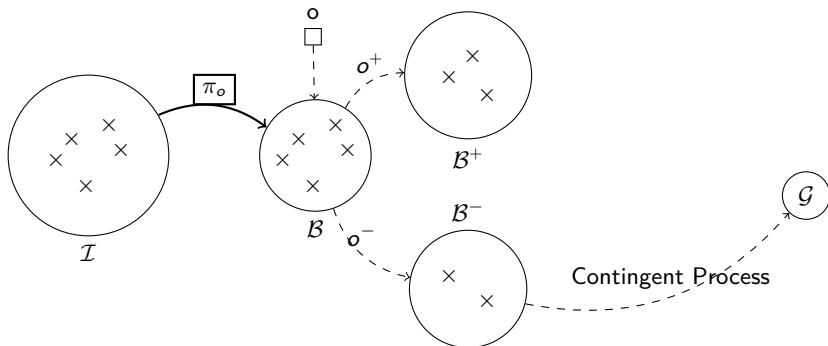
→

success

 $a$ 

returned element

# Contingent Process



Start the Contingent process to compute the branch from  $\mathcal{B}^-$  to the goal

## Legend

x

state



success

- - - - -&gt;

application

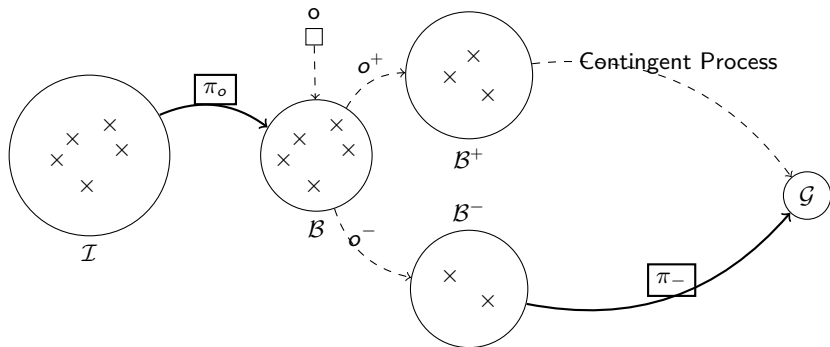


returned element

- - - - -&gt;

failure

# Contingent Process



Start the Contingent process to compute the branch from  $\mathcal{B}^+$  to the goal

## Legend

x

state



success



application

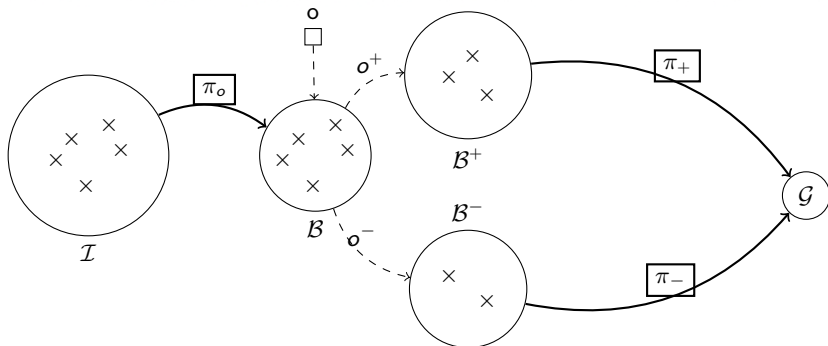


returned element



failure

# Contingent Process



Once each branch leads to the goal, the resulting Contingent plan is returned

## Legend

x

state

- - - - -&gt;

application

- - - - -&gt;

failure

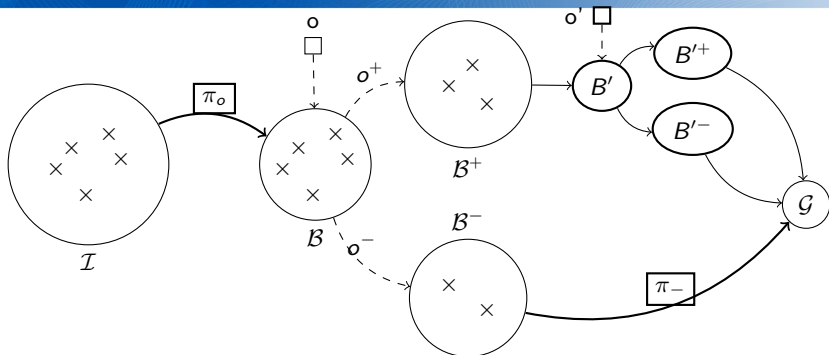
→

success

a

returned element

# Contingent Process



The process is recursive: a subplan can be Conformant, or Contingent

## Legend

x

state

- - - - -&gt;

application

- - - - -&gt;

failure

→

success

a

returned element

# Contingent Planning Algorithm

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**Algorithm 1:** Contingent Planning Procedure

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**Input:**  $\mathbb{P} = (\mathcal{L}, \mathcal{O}, I, G)$

**Output:**  $\pi_c$

**begin**

```
   $\pi, \gamma := \text{conformantPlanner}(\mathbb{P})$   
  if  $\gamma = \emptyset$  then  
    return  $\pi$   
   $\mathcal{B}_o, o := \text{findObservation}(I, \mathcal{O}, \pi, \gamma)$   
   $\pi_o := \text{ContingentPlanning}((\mathcal{L}, \mathcal{O}, I, \mathcal{B}_o))$   
   $\mathcal{B}^+ := T(\mathcal{B}_o, o) \text{ with } \nu^+(o) = \text{eff}(o)$   
   $\pi_p := \text{ContingentPlanning}((\mathcal{L}, \mathcal{O}, \mathcal{B}^+, G))$   
   $\mathcal{B}^- := T(\mathcal{B}_o, o) \text{ with } \nu^-(o) = \text{eff}(o)$   
   $\pi_n := \text{ContingentPlanning}((\mathcal{L}, \mathcal{O}, \mathcal{B}^-, G))$   
  return  $(\pi_o ; \text{if } o \text{ then } \pi_p \text{ else } \pi_n)$ 
```

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- The algorithm is described in the paper
- Our approach is sound because we rely on a sound conformant planner to compute each branch of the plan
- The returned solutions are conformant or contingent solutions
- We compare our approach with Contingent-FF (Hoffmann and Brafman, 2005)
- 7 benchmarks of 4 problems each
- Time out of 5 min

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# Results

Problem	Contingent Planning with counter-examples					Contingent-FF			
	time	size	depth	shortest	observations	time	size	depth	observations
blocks/p3	0.94	6	4	3	1	0.00	6	4	1
blocks/p7	5.6	89	16	10	7	0.05	<b>55</b>	<b>9</b>	7
blocks/p11	6.4	169	29	20	7	0.43	<b>117</b>	<b>18</b>	7
blocks/p15	8.05	244	39	27	7	3.20	<b>163</b>	<b>25</b>	7
btcs/p10	0.76	19	19	19	<b>0</b>	0.02	19	10	9
btcs/p30	2.36	59	59	59	<b>0</b>	0.8	59	30	29
btcs/p50	8.13	99	99	99	<b>0</b>	9.79	99	50	49
btcs/p70	24.11	139	139	139	<b>0</b>	57.31	139	70	69
ebtcs/p10	6.21	19	10	2	9	0.01	19	10	9
ebtcs/p30	22.73	59	30	2	29	0.42	59	30	29
ebtcs/p50	56.8	99	50	2	49	4.93	99	50	49
ebtcs/p70	156.11	139	70	2	69	29.10	139	70	69
grid/p2	3.61	9	9	9	0	0.01	9	9	0
grid/p3	4.05	<b>19</b>	<b>19</b>	19	<b>0</b>	9.78	174	43	15
grid/p4	21.24	<b>45</b>	<b>45</b>	45	<b>0</b>	227	464	68	17
grid/p5	18.64	<b>31</b>	<b>31</b>	<b>31</b>	<b>0</b>	TO	-	-	-
erovers/p2	1.09	<b>11</b>	<b>9</b>	5	1	0.00	13	10	1
erovers/p4	3.39	23	17	5	3	0.00	23	<b>14</b>	3
erovers/p6	NO	-	-	-	-	0.09	<b>346</b>	<b>48</b>	<b>7</b>
erovers/p8	3.34	<b>44</b>	<b>21</b>	15	3	0.01	95	36	3
logistics/p1	0.39	<b>9</b>	9	9	<b>0</b>	0.01	10	7	1
logistics/p3	0.49	<b>14</b>	14	14	<b>0</b>	0.01	18	8	2
logistics/p5	0.58	<b>29</b>	29	29	<b>0</b>	0.054	172	26	7
logistics/p7	0.75	<b>31</b>	31	31	<b>0</b>	0.2	247	27	11
elogistics/p1	1.07	10	7	4	1	0.00	10	7	1
elogistics/p3	1.8	18	8	5	2	0.00	18	8	2
elogistics/p5	9.02	<b>138</b>	<b>22</b>	20	7	0.12	172	26	7
elogistics/p7	10.63	<b>185</b>	26	21	11	0.13	247	26	11

# Results

- Generally we find **shorter plans**
- When a **conformant solution** exists:
  - We find a **conformant plan** while Contingent-FF (Hoffmann and Brafman, 2005) include **observations**
- When there is no conformant solution:
  - Generally the **same number of observations** but **shorter plans**
- Drawbacks:
  - Lack of completeness
  - Computation time

# Plan

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# Conclusion

- Contingent Planner computing contingent plans with a limited complexity
- Use a conformant planner to compute **conformant subplans** if possible
- Use a **counter-example** and a **failing plan** to find an **observation**
- Split the problem in **subproblems** with **less uncertainty**
- Iterate until no counter-example exists
- Any conformant planner can be used if it returns a counter-example

# Plan

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# Approach improvements

## Huge Space Version

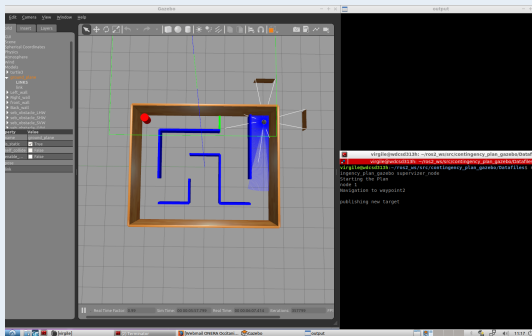
- We do not compute the beliefs internally, we directly modify the PDDL problem and domain
- We ask CPCES (Grastien et al., 2017) to find a plan leading to one of the possible observations
- To compute the branches we enforce CPCES to start with the plan leading to the observation and we transmit a SMT constraint to indicate the result of each observation contained in the previous branch
- Ongoing results

## Backtracking

- Backtracking on the observations
- Handle a list of the plans computed from every possible observations
- Improve the completeness of the approach
- Ongoing results

# Simulation Environment

- Simulation environment of robotic mission
- Internship of Virgile De La Rochefoucauld at the Onera



- Albore, A. et al. (2011).  
Translation-based approaches to automated planning with incomplete information and sensing.  
PhD thesis, Universitat Pompeu Fabra.
- Bertoli, P., Cimatti, A., and Roveri, M. (2001).  
Heuristic search+ symbolic model checking= efficient conformant planning.  
In IJCAI, pages 467–472. Citeseer.
- Brafman, R. and Hoffmann, J. (2004).  
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