My name is Fritz Laux. I’m a retired professor from Reutlingen University where I was responsible for the database teaching and research since the start of our department.

I am a cofounder of DBTechNet, a European initiative of academics and industry to improve and promote database education.

Over the years I was part of three EU-funded projects and numerous research and development projects in cooperation with industry.

With 40 years of experience in database modelling and design I learned about the importance of database modelling. Data modelling is, and always will remain a crucial part of SW development.

As fashions and practices come and go, I tried to combine the best ideas.

This is why my recent work focusses on Graph Data Models.
What can you expect from this presentation?

First I will point out some weaknesses of the original GM and suggest enhancements to make it ready for data modelling.

It will quickly become clear, that we need to capture more semantics.

Second, this leads to the Typed Graph Model (TGM) which provides more semantics and ensures data integrity.

The talk is built around examples for modelling typical relational-, and object-oriented structures by using the TGM.

During the presentation we will answer the following questions:

- Which enhancements are needed?
- What is the semantic expressiveness of our model compared to competing models?
- Is it better matching the way we communicate reality?
- Is there support for multiple abstraction levels?

The presentation will conclude by some modelling guidelines for the TGM.
The popularity of the Graph Model (GM) stems primarily from its application to social networks. Even if the flexibility of the GM is tempting, its schema-less application is prone to data quality problems.

- Robinson and his colleagues from Neo4J recommend in their book to use "Specification by Example", which uses real objects like the following (p. 42):

  ![Graph Model Example](image)

  - The problem with this is that we cannot exemplify all situations
  - The object “Review” depends on the existence of a “User” and a “Performance”
  - We cannot know if Billy is allowed to have multiple reviews (on the same performance?)

**In order to express this semantics it is necessary to abstract and specify integrity constraints**

- This means we have to deal with abstract things (like a generic Person) and not only with real objects (like Billy)

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The Typed Graph Model (TGM)
Let us start with a short recap of the original graph definition.

A mathematical (directed) Graph $G = (V, E)$ is defined as

- a set of Vertices $V$ and
- a set of Edges $E$ connecting 2 (ordered) vertices $(u, v)$, with $u, v \in V$.

The vertices can be numbered for identification and the edges may have "weight" for calculating the cost of a path.

**Shortcomings for data modelling:**

1. Two modelling elements are not sufficient to express data structures
   - e.g. even the relational model has 3 modelling elements
   - We want to distinguish different association types, e.g. inheritance, aggregation

2. The Graph Model is originally instance based
   - If we apply the GM on the Schema level, how can we ensure integrity constraints, e.g. capture the multiplicity of an association?

The main shortcomings for data modelling are first of all, that real world objects have structure and properties, which cannot be distinguished in the original GM.

This weakness was tried to overcome with graph enhancements, like labels and properties attached to the vertices.

Second, the GM is instance based and therefore captures only a particular situation as we have already seen in the previous slide. The GM cannot express structural constraints.
There have been some research on using the GM on a schema level. The nodes were considered as classes and edges are not instances any more but edge types. The proposed models usually fail when edge cardinality is necessary or models make no sufficient distinction between nodes, properties and their respective data types.

In order to overcome the restricted modelling capabilities we need mainly two extensions:

1. More modelling elements, and
2. Clear distinction between the abstraction levels: instance and schema.

To solve the overloading of nodes we add properties and types to the nodes which serve as classes on the schema level.

Nodes have a type. Types are stronger than labels because a type represents the allowed structure and value range of an object whereas a label is only a name.

Edges have a type too which defines the kind of association, for instance, aggregation or generalization.
A typed graph data model is a tuple \( TGM = (N, E, TGS, \phi) \) where:

- \( N \) is the set of named (labeled) hyper-nodes \( n \) with data types from schema TGS.
- \( E \) is the set of named (labeled) hyper-edges \( e \) with properties of types from schema \( TGS \).
- \( \phi \) is a homomorphism that maps each node \( n \) and edge \( e \) to the corresponding type element of TGS.
- In addition \( TGS \) offers min-max multiplicity for each end of an edge plus integrity constraints \( C \).

**Definition (simplified): The Typed Graph Model (TGM)**

- **Our Typed Graph Model** informally constitutes a property hyper-graph that conforms to a schema.
- It consists of typed hyper-nodes \( N \) from a Typed Graph Schema \( TGS \) and typed hyper-edges \( E \) from Schema \( TGS \).
- Essential for the integrity of a data graph instance is the homomorphism \( \phi \) that maps each instance element to a schema element that defines its type and ensures the integrity of the instance.
- The Typed Graph Schema \( TGS \) offers min-max cardinality for each edge endpoint and supports additional integrity constraints.
- We use the UML class notation for visualizing nodes and UML associations for edges as it provides a compact rendering and extensions using constraints.

The fact that hyper-nodes and any data types are supported, including user-defined complex data types gives the TGM the potential to build schemata on different abstraction levels as we will see in the second example. This is very important to keep large data models manageable.

Next we turn back to our initial example from Robinson's book and show how it will be modeled and improved.
• On the left we have Robinson’s example amended to show that Billy is allowed to write more than one Review. We use the same visualization as in their book.

• The schema on the right uses UML for better visual clarity of both levels.

• The function $\Phi$ maps the User to the data type Person which ensures that the User must have exactly one name. This is indicated by the number 1 in brackets. The Review itself is tied to the complex type Review with a mandatory Rating and an optional Review text. The Performance can have 2 properties, an optional title and a mandatory date. Even the date format is clearly prescribed by a format template.

The association cardinalities between Person and Review signify that a Person has at least one Review. The mapping $\Phi$ ensures that there are no Users without Review.

The homomorphism $\Phi$ preserves structure between both graph levels. This means, that wrote review instances are tied to the 1 to many relation and therefore no second author is allowed to link to Billy’s reviews.

A Review always refers to exactly one Performance, but, a Performance may have any number of Reviews, including none.
In this example we demonstrate the modelling capabilities and its semantic expressiveness.

The graph schema represents a commercial enterprise that sells products and parts to customers. The enterprise assembles products from parts and if the stock level is not sufficient, it purchases parts from different suppliers.

The figure models this situation using TGM in UML rendering.

It demonstrates the abstraction power of the TGM showing two schema abstraction levels.

The upper part (a) shows the model on a detailed level. The properties are suppressed in the diagram for simplicity, except for Customer and CustOrder.

The schema is grouped into 3 disjoint sub-graphs depicted with dashed lines.

In the lower part (b) these sub-graphs are shown as hyper-nodes. This allows a simplified and more abstracted view of the graph model.

- Also, some aggregate properties (for example, #orders and the total of customer orders) are shown to illustrate the modelling capabilities. The hyper-edges connecting these abstracted nodes must use the most general multiplicity of the edges it combines.

- In our example the edge orders/from combines two edge types, the orders edge - with an optional 1 - 1 multiplicity and the from edge - with unlimited multiplicity, which leads to the most general multiplicity.
The Typed Graph Model (TGM)

The TGM models a relational data structure in a straightforward manner:

- **The table name** is used as node label and the attributes are used as node properties including their data types.
- If we have a foreign key relationship, it is mapped to an edge with many to one cardinality. The foreign key attribute \( k_2 \) can be omitted because the edge carries already the necessary information.
- A tuple of a join table depends on the existence of the foreign keys. Therefore we need to attach the non-key attribute \( \text{Col} \) in our example here.
  - as property of the edge-type linking the tables. This is rendered in UML as an association class.
Because we already use UML for rendering the TGM, it is easy to see that classes correspond one-to-one with typed hyper-nodes. Any methods are simply ignored as we only deal with the network structure of the Object-Oriented Model. Any complex internal class structure can be directly modeled by appropriate data types.

- The UML provides a rich set of association types, which need to be mapped to the types of the edges. Our TGM provides types not only for nodes but also for edges.
- With this information it is also possible to model different association types like aggregation, generalization, etc. Even user defined associations are possible, for instance, an aggregate could be further qualified as un-detachable or detachable composition.

The arrow of the edge only indicates the reading direction of the association name but does not limit the navigation of the TGM.
The Object-Oriented Model (OOM for short) and the TGM share the same UML notation. Any modelling element of OOM has a unique UML rendering and corresponds to a distinct TGM modelling element. This means, any object-oriented structure can be represented as a TGM.

This indicates that TGM is stronger than the OOM if only data structuring is concerned.

- The OOM is a strictly stronger model than the RM, ERM, and XML Schema because all its modelling elements have unique counterparts in OOM if we use user defined data types.

In fact, it is possible to define a user defined datatype, for example, in XML schema and use it in a TGM model to represent a hierarchical structure.
Let me now answer the questions from the beginning of my talk:

**Is the TGM suitable for data schemas?**

Yes, we have seen the model is applicable on schema and instance level.

It provides sufficient semantics by using 4 modelling elements, namely nodes, properties, labels and edges. Each element has a data type to ensure data integrity.

**Is it better matching the way we communicate reality?**

No, the models considered in the examples all basically rely on objects/entities/nodes and associations/relationships/edges.

**What is the semantic expressiveness of the TGM?**

We argued that the TGM has better modelling power than the prevalent models (RM, ERM, XML schema or OOM).

**Is there support for multiple abstraction levels?**

There is no special notation for it. It is possible and the responsibility of the designer.

**Consequences of using the TGM vs. other data models?**

In general, there is no real benefit as the modelling decisions remain the same.

There is no semantic mismatch with TGM if the target database is a Graph Database.
Our conclusion is:

The TGM is designed to be used on the meta-level.

This means that nodes represent entity sets or classes with properties that define the details.

The use of UML is preferred for a compact visual representation.

The model is not orthogonal which gives the freedom but also the burden for modelling decisions. The consequence is that it is hard to establish quality criteria for modelling.

When using ternary or higher order edge types it is not always easy to decide on the correct cardinality.

In real world scenarios the TGM tends to become large.

It may help to suppress properties in the diagram and provide separate lists for properties.

Overview diagrams which use higher abstraction level aggregates can provide a view that is easier to comprehend.

To model partial structures separately may help to reduce complexity.
Our work started out from Robinson's book and involved more than 20 sources listed in the paper, out of which we present here the 4 most important ones.

The Typed Graph Model (TGM)

References

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3) J. Hidders: “Typing Graph-Manipulation Operations”, Proc. 9th International Conference on Database Theory (ICDT), 2003, pp. 391-406
