



Zurich Research Laboratory

Reliability of Data Storage Systems

Ilias Iliadis
April 20, 2015

Keynote NexComm 2015

www.zurich.ibm.com

Long-term Storage of Increasing Amount of Information

An increasing amount of information is required to be stored

- Web services
 - Email, photo sharing, web site archives
- Fixed-content repositories
 - Scientific data
 - Libraries
 - Movies
 - Music
- Regulatory compliance and legal issues
 - Sarbanes–Oxley Act of 2002 for financial services
 - Health Insurance Portability and Accountability Act of 1996 (HIPAA) in the healthcare industry

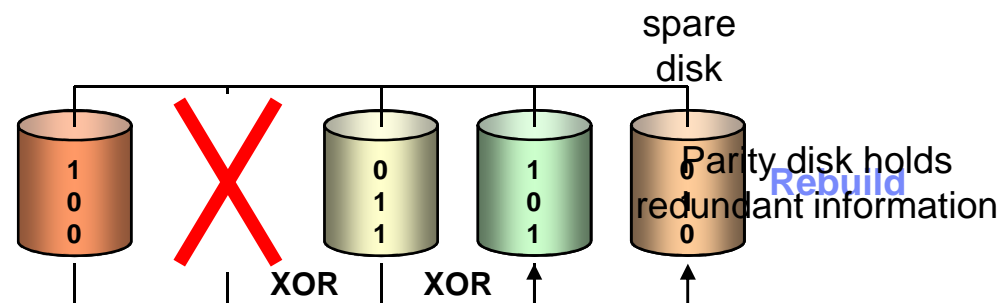
Information needs to be stored for long periods and be retrieved reliably

Storage

- Disk drives widely used as a storage medium in many systems
 - personal computers (desktops, laptops)
 - distributed file systems
 - database systems
 - high end storage arrays
 - archival systems
 - mobile devices
- Disks fail and need to be replaced
 - Mechanical errors
 - Wear and tear: it eventually leads to failure of moving parts
 - Drive motor can spin irregularly or fail completely
 - Electrical errors
 - A power spike or surge can damage in-drive circuits and hence lead to drive failure
 - Transport errors
 - The transport connecting the drive and host can also be problematic causing interconnection problems

Data Losses in Storage Systems

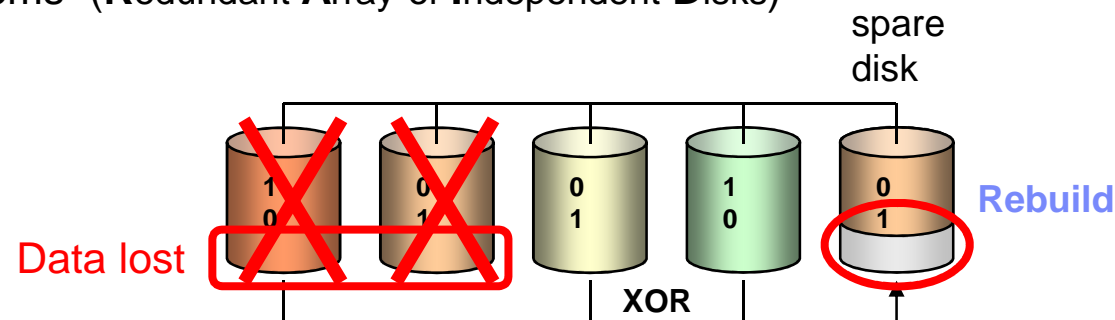
- Storage systems suffer from data losses due to
 - component failures
 - disk failures
 - node failures
 - media failures
 - unrecoverable and latent media errors
- Reliability enhanced by a large variety of redundancy and recovery schemes
 - RAID systems (**R**edundant **A**rray of **I**ndependent **D**isks)



- RAID-5: Tolerates one disk failure

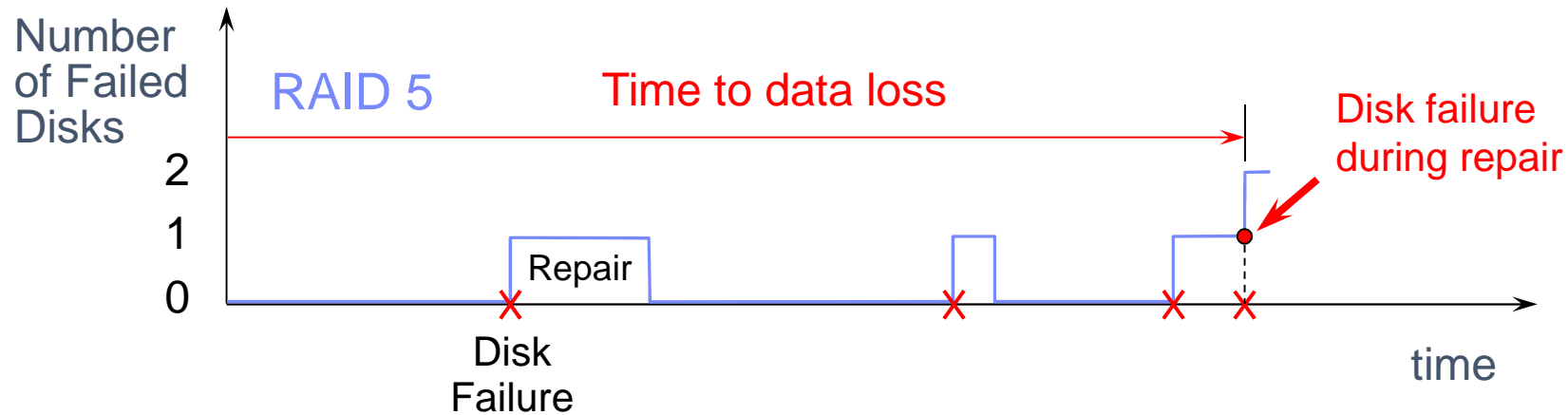
Data Losses in Storage Systems

- Storage systems suffer from data losses due to
 - component failures
 - disk failures
 - node failures
 - media failures
 - unrecoverable and latent media errors
- Reliability enhanced by a large variety of redundancy and recovery schemes
 - RAID systems (**R**edundant **A**rray of **I**ndependent **D**isks)



- RAID-5: Tolerates one disk failure
- RAID-6: Tolerates two disk failures

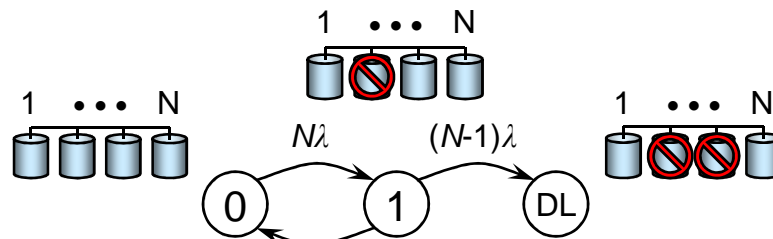
Time to Failure and MTTDL



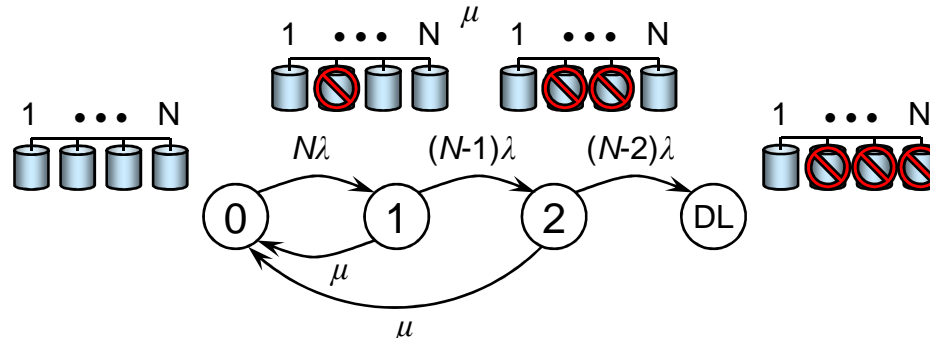
— Reliability Metric: **MTTDL** (Mean Time to Data Loss)

➤ Continuous Time Markov Chain Models

RAID 5:



RAID 6:



— λ : 1/MTTF for disks

— μ : 1/MTTR

$$MTTDL \approx \frac{\mu}{N(N-1)\lambda^2}$$

[Patterson et al. 1988]

$$MTTDL \approx \frac{\mu^2}{N(N-1)(N-2)\lambda^3}$$

[Chen et al. 1994]

original MTTDL equations

Markov Models for Unrecoverable Errors

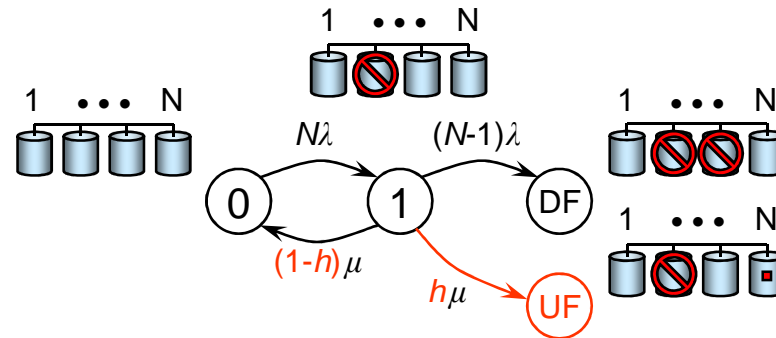
Parameters:

- C_d : Disk capacity (in sectors)
- P_s : P (unrecoverable sector error)
- h : P (unrecoverable failure during rebuild in critical mode)
- q : P (unrecoverable failure during RAID 6 rebuild in degraded mode)

$$h = 1 - [(1 - P_s)^{C_d}]^{(N-1)}$$

Reliability Metric: MTDDL (Mean Time To Data Loss for the array)

RAID 5:

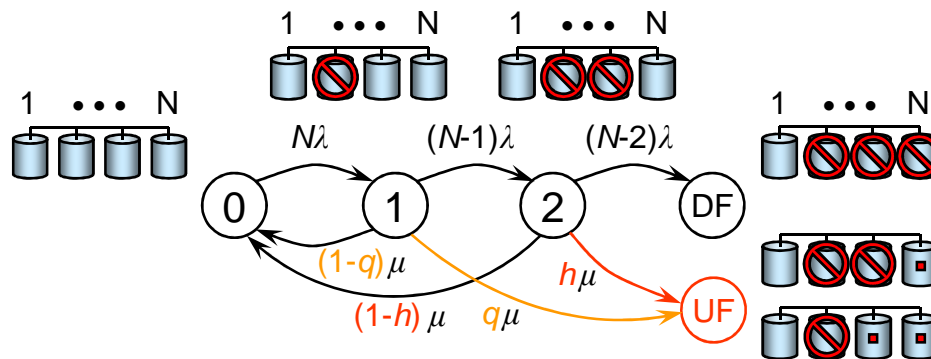


Data loss owing to:

- DF: Disk Failure
- UF: Unrecoverable Failure

$$MTDDL = \frac{(2N-1)\lambda + \mu}{N\lambda[(N-1)\lambda + \mu h]}$$

RAID 6:



$$h = (N - 2)C_d P_s + O(P_s^2)$$

$$q = \binom{N-1}{2} C_d P_s^2 + O(P_s^3)$$

$$q \ll h \text{ for } P_s \ll 1$$

MTTDL for RAID 5 and RAID 6

Assumptions:

UD : 10 PB = 10^{15} bytes user data base

C_d : 300 GB SATA disk drive capacity

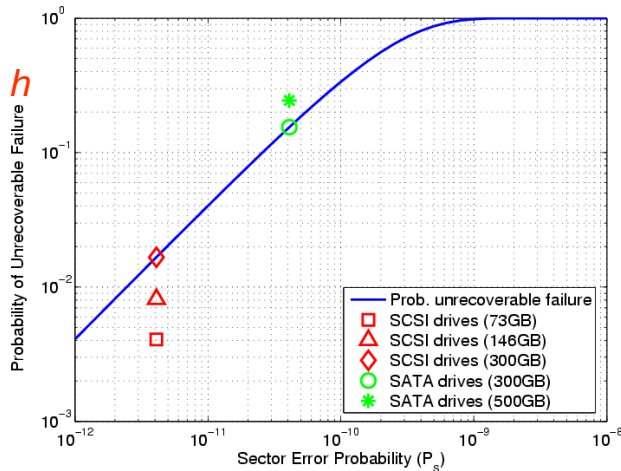
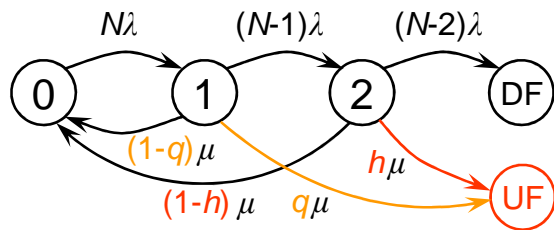
N : 8 disks per array group for RAID 5
16 disks per array group for RAID 6

N_{total} : 38096 disks: 4762 arrays for RAID 5
2381 arrays for RAID 6

$MTTF_d$: 500 000 hours for a SATA disk

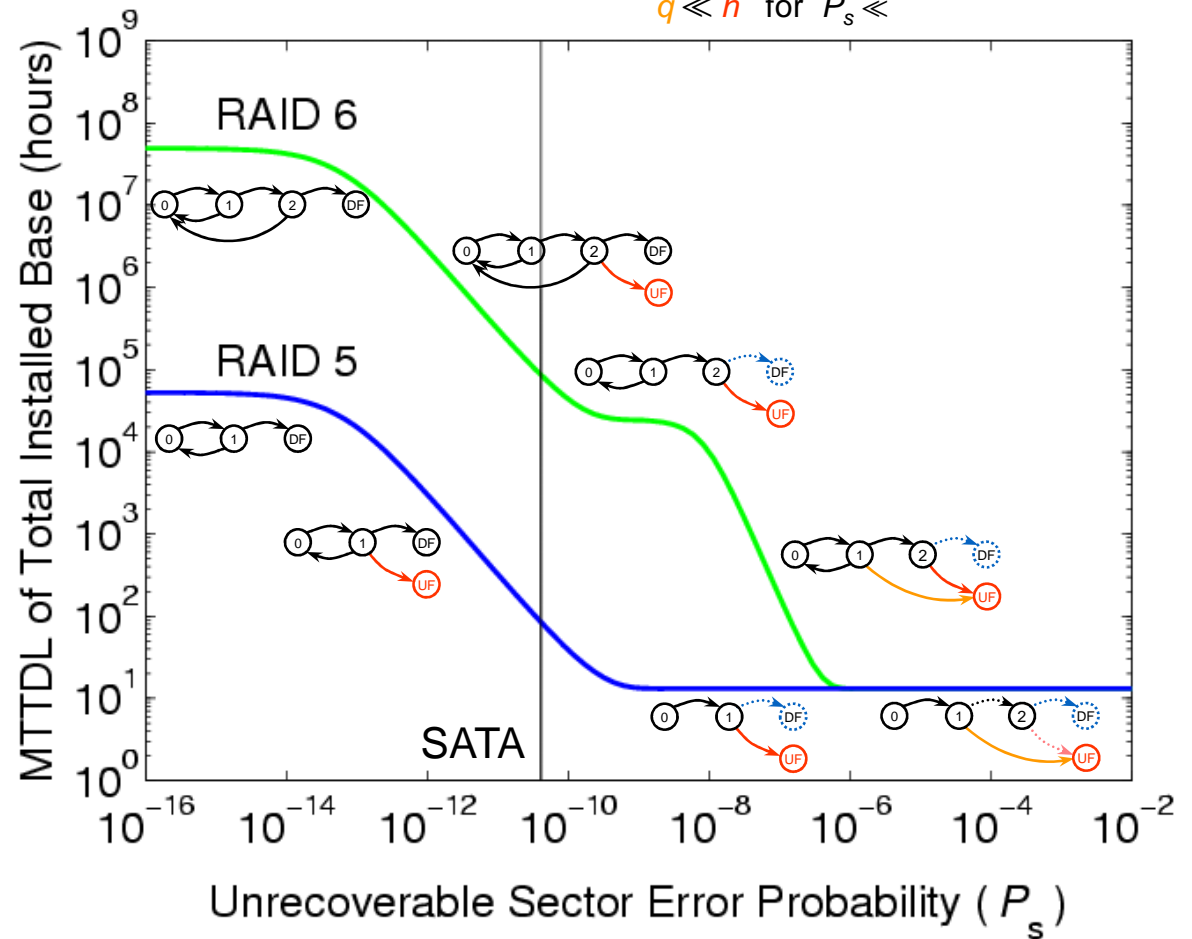
$MTTR_d$: 17.8 hours expected repair time

P_b : $P(\text{unrecoverable bit error}) = 10^{-14}$ for SATA
 $\Rightarrow P_s = 4096 \times 10^{-14} = 4.096 \times 10^{-11}$

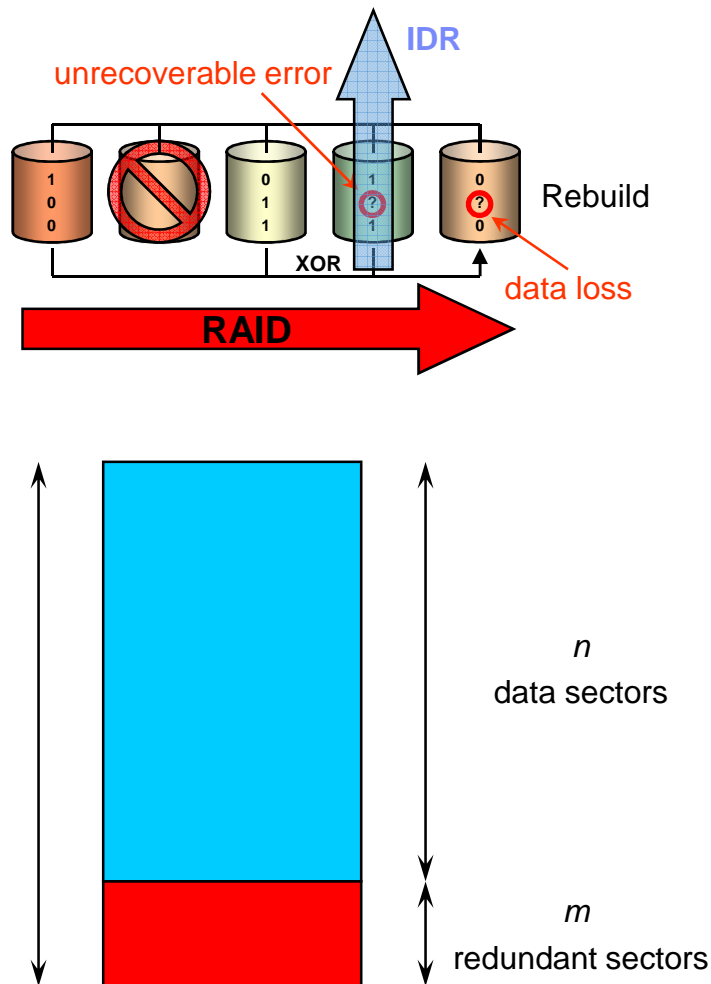


h : $P(\text{unrecoverable failure during rebuild in the critical mode})$
 q : $P(\text{unrecoverable failure during RAID 6 rebuild in the degraded mode})$

$q \ll h$ for $P_s \ll$



Intra-Disk Redundancy (IDR) Scheme



- Design concept:
 - For every ' n ' data sectors, ' m ' parity sectors are assigned
 - Redundant sectors are placed on the same disk drive as data
 - The ' m ' parity sectors protect against uncorrectable media errors of any ' m ' sectors in a group of ' n ' sectors

- Intra-disk redundancy segment:
 - $l = n+m$ sectors

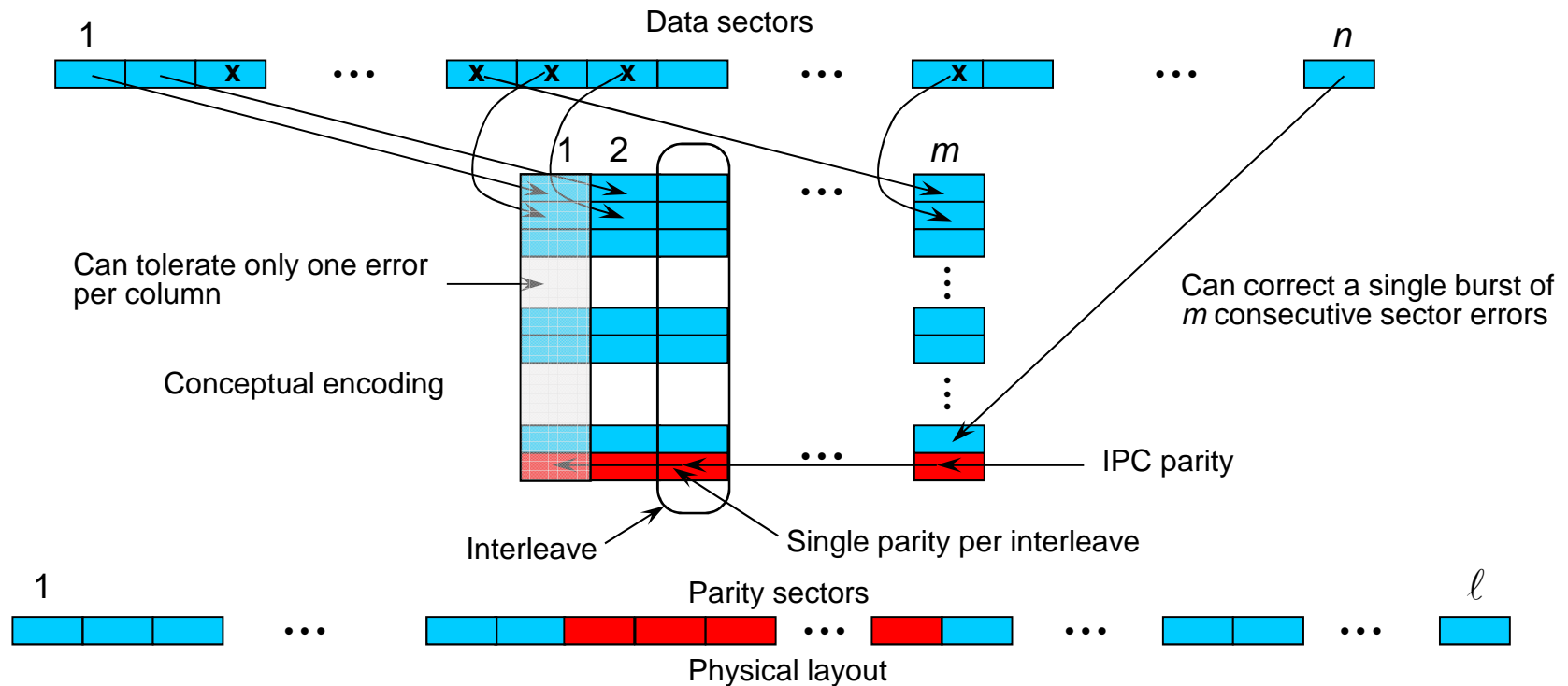
- Storage efficiency is $n/(n+m)$

- By choosing proper values of n and m , storage efficiency, performance and reliability can be optimized

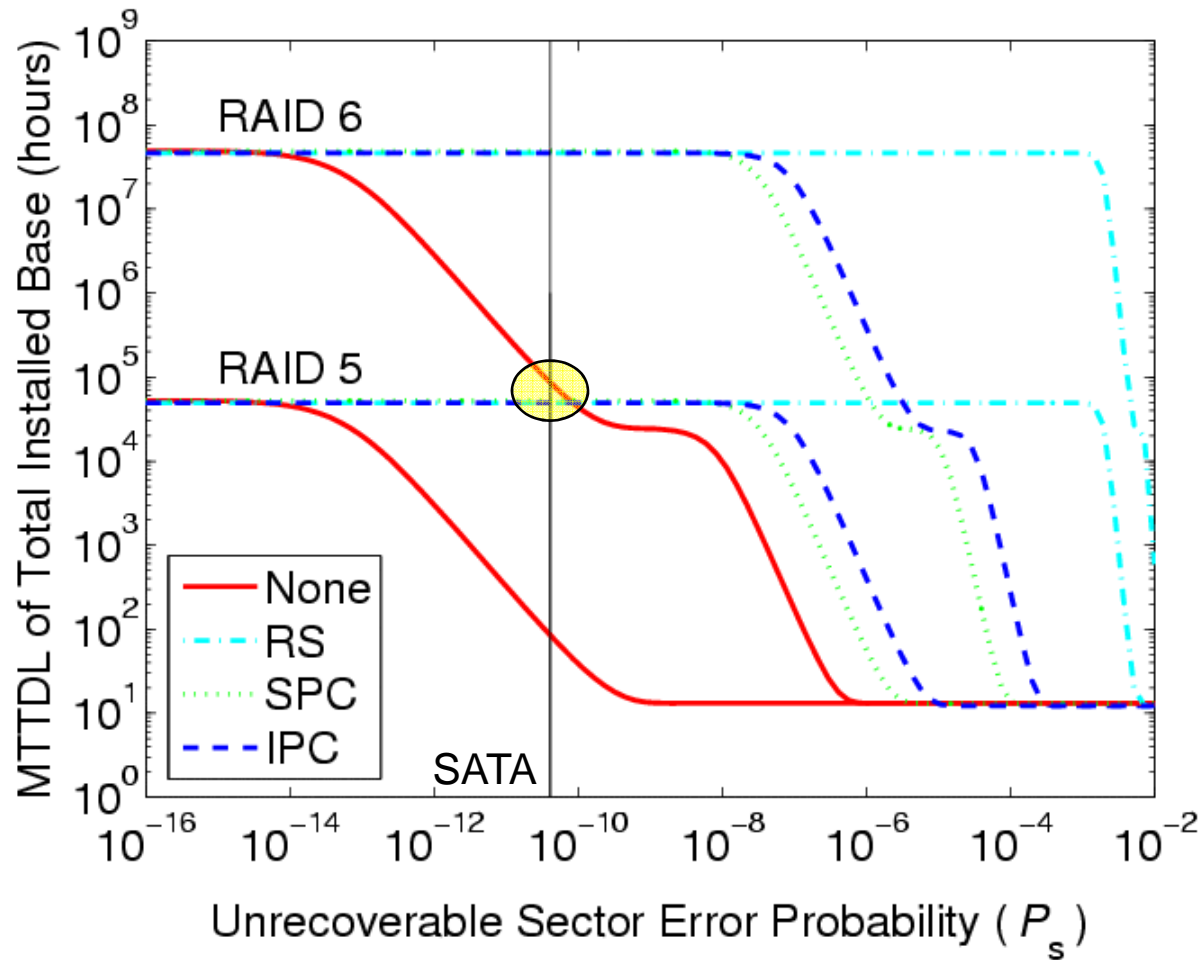
Dholakia *et al.*, "A New Intra-disk Redundancy Scheme for High-Reliability RAID Storage Systems in the Presence of Unrecoverable Errors," ACM Trans. Storage 2008

Interleaved Parity Check (IPC) Coding Scheme

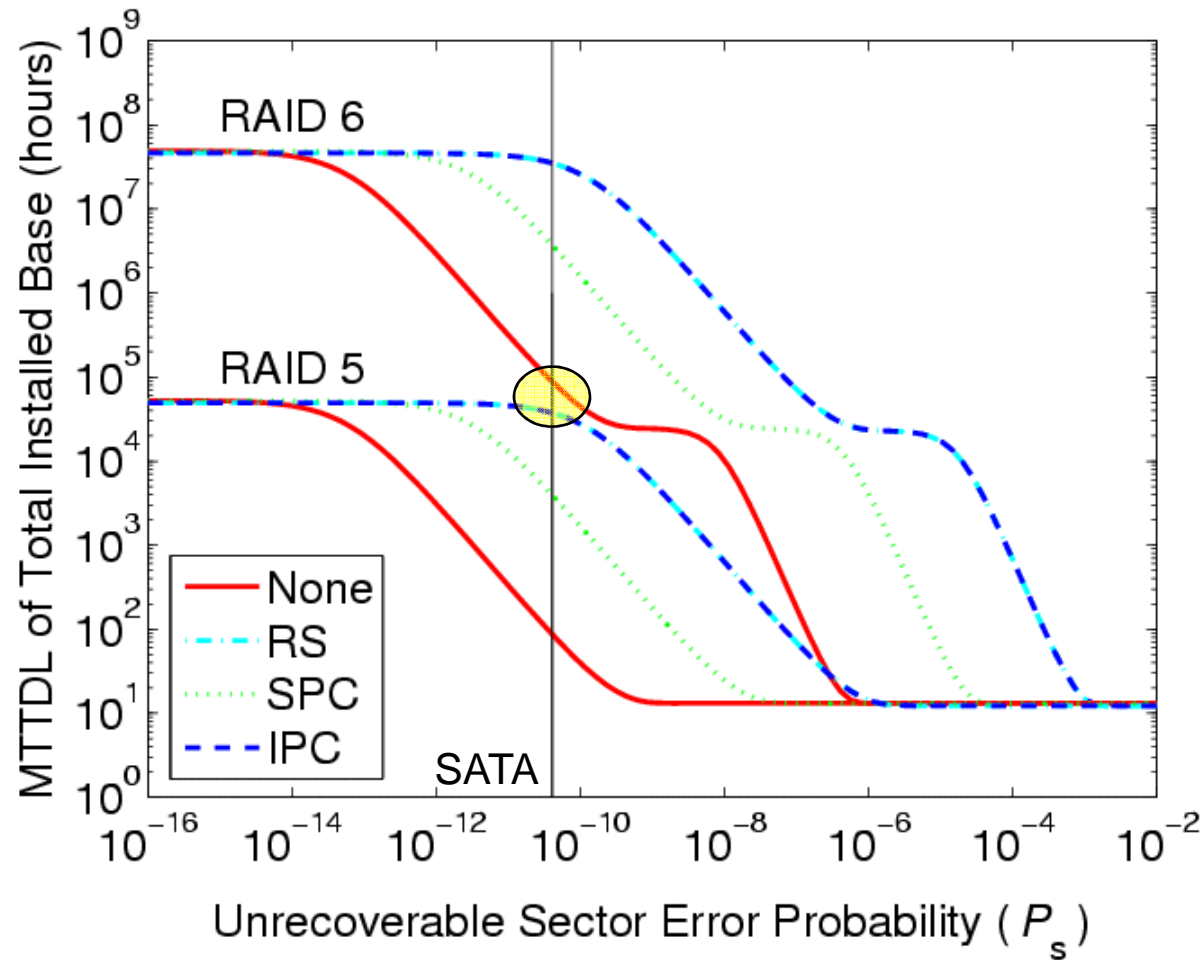
- Advantages
 - Easy to implement, using existing XOR engine
 - Flexible design parameters: segment size, efficiency
- Disadvantage
 - Not all erasure patterns can be corrected



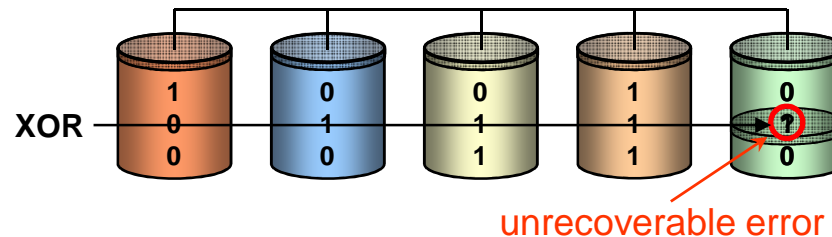
MTTDL for Independent Unrecoverable Sector Errors



MTTDL for Correlated Unrecoverable Sector Errors

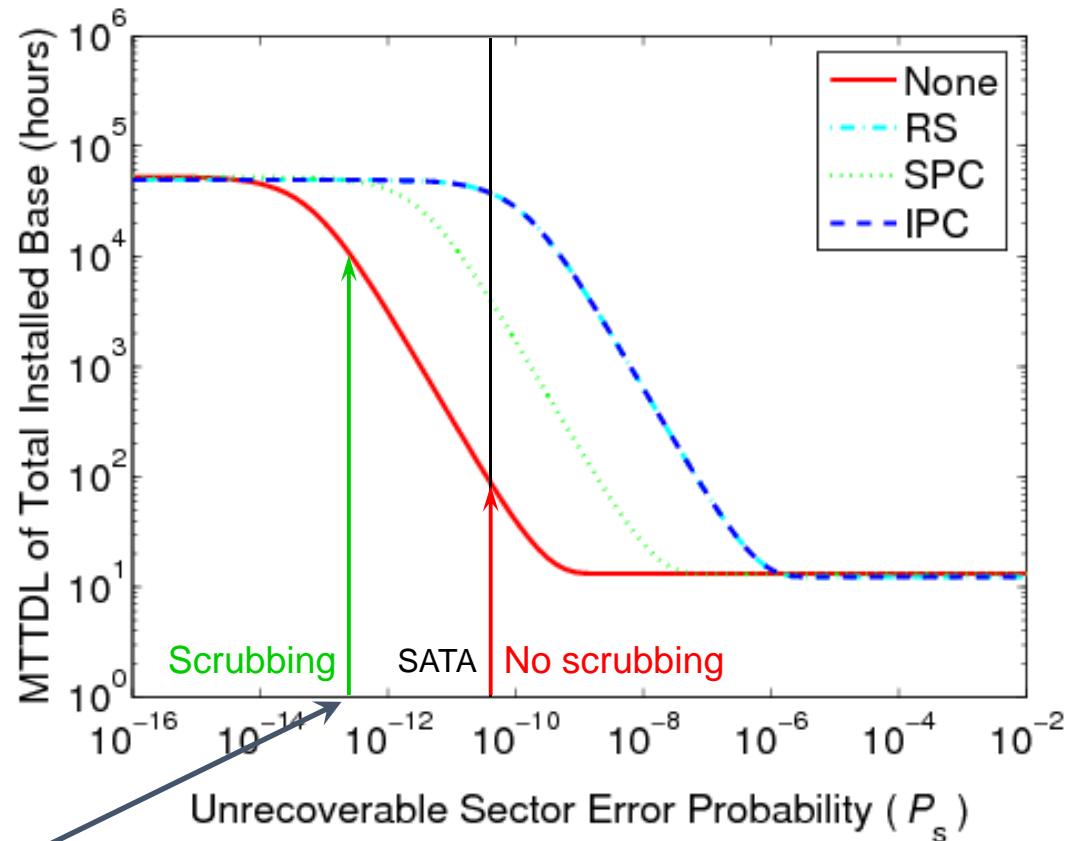


Disk Scrubbing



- Periodically accesses disk drives to detect unrecoverable errors
 - T_s : Scrubbing period = time required for a complete check of all sectors of a disk
- Identifies unrecoverable errors at an early stage
- Corrects the unrecoverable errors using the RAID capability
- Increases the workload because of additional read operations
- Sector write operations result in unrecoverable errors
 - $P_w = P(\text{sector-write operation results in an error})$
 - Transition noise (media noise), “high-fly” write, off-track write
 - Contribution of thermal asperities and particle contamination ignored
- Disk-unrecoverable sector errors
 - are created by write operations and remain **latent** until read or successfully over-written
- Workload
 - h : load of a given data sector = rate at which sector is read/written
 - e.g. $h=0.1 / \text{day}$ → 10% of the disk is read/written per day
 - r_w : ratio of write operations to read+write operations
 - typically 2/3

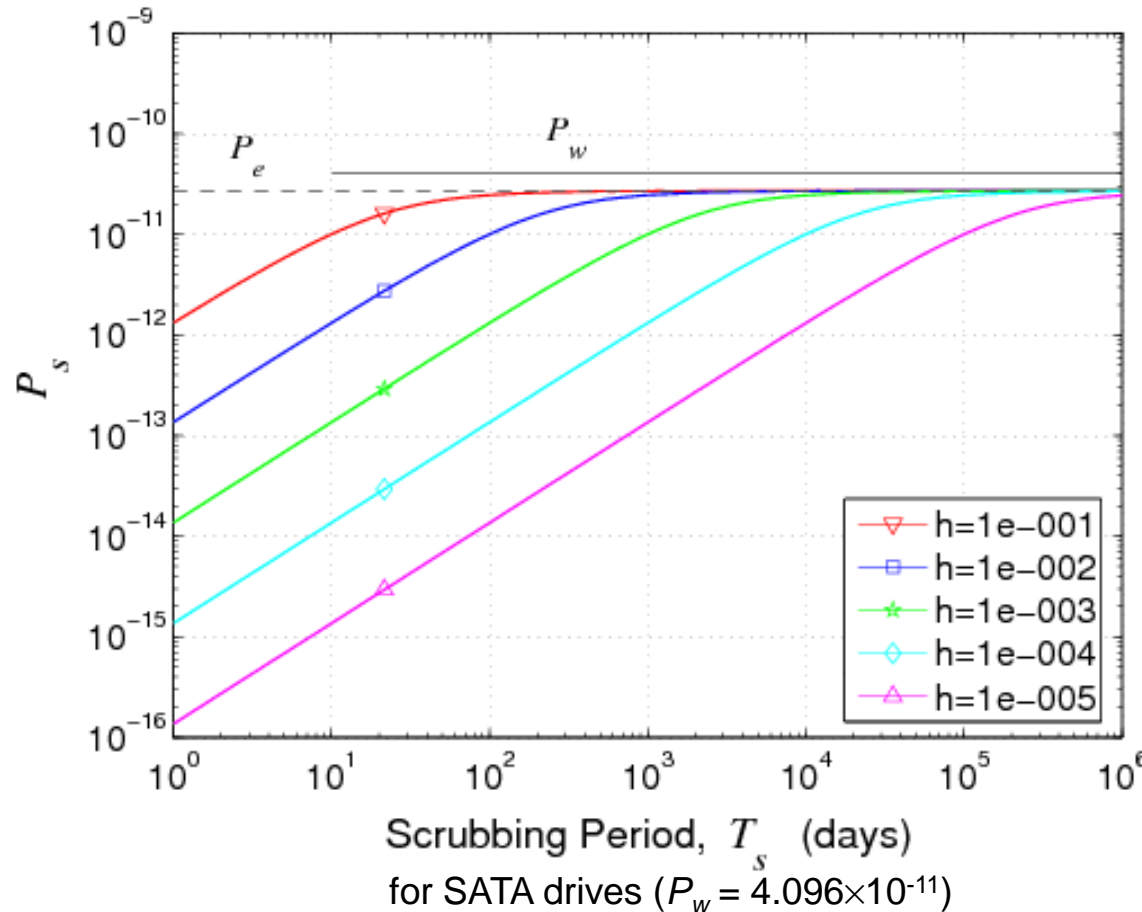
Modeling Approach



- derive $P_s = P(\text{sector error} \mid \text{scrubbing is used}) = f(T_s, P_w, h, r_w)$
- evaluate $MTTDL = f(P_s)$

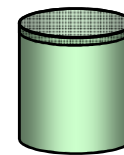
Analytical Results: Probability of Unrecoverable Sector Error

P_s : P (unrecoverable error on a tagged sector at an arbitrary time)



- Without scrubbing: $P_s \rightarrow P_e = r_w P_w$
 - P_e depends on the ratio r_w of read/write operations, but not on the workload h

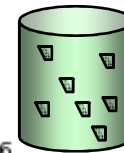
- Deterministic scrubbing scheme:



$$P_s = \left(1 - \frac{1 - e^{-hT_s}}{hT_s} \right) P_e$$

- $P_s \leq P_e \leq P_w$

- Random scrubbing scheme:



$$P_s = \frac{hT_s}{1 + hT_s} P_e$$

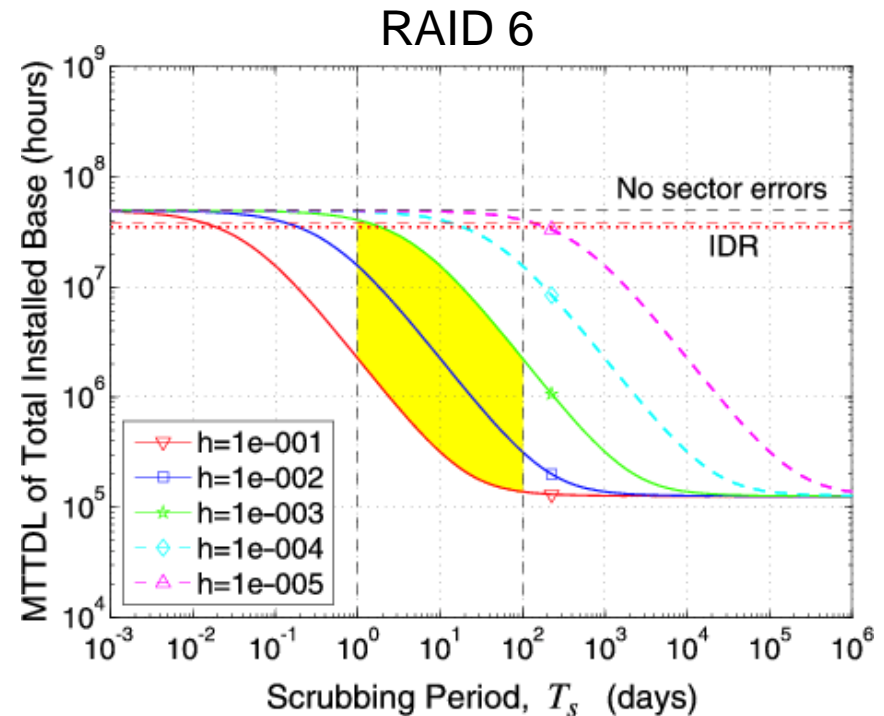
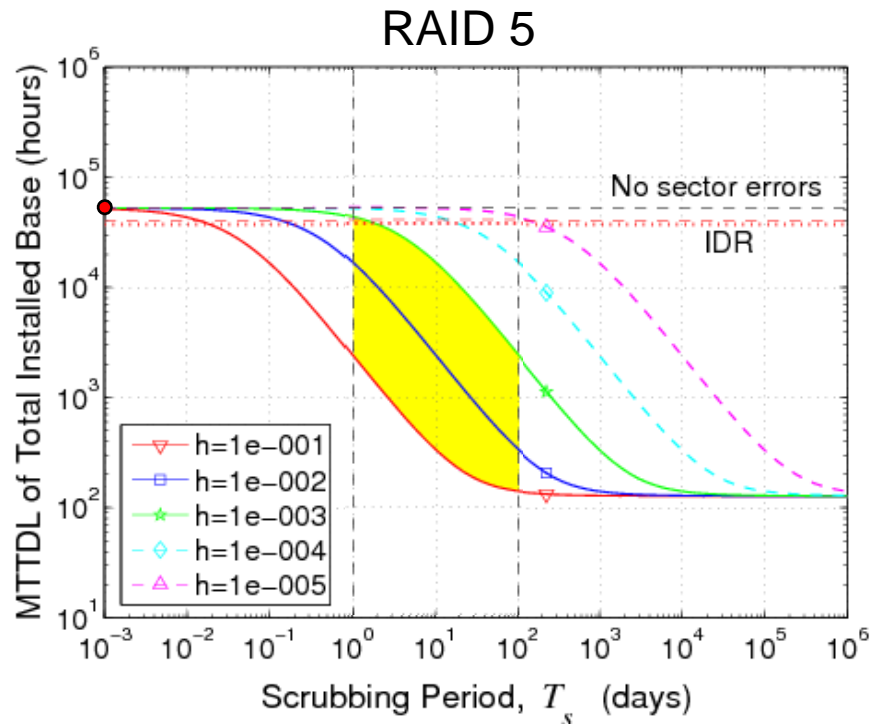
- P_s (deterministic) < P_s (random)
- $hT_s \ll 1 \rightarrow P_s$ (deterministic) $\approx \frac{1}{2} P_s$ (random)

Iliadis *et al.*, "Disk Scrubbing Versus Intradisk Redundancy for RAID Storage Systems," ACM Trans. Storage 2011

Reliability Results for RAID-5 and RAID-6 Systems

SATA disk drives: $C_d = 300\text{GB}$, $\text{MTTF}_d = 500,000\text{ h}$, $\text{MTTR} = 17.8\text{ h}$, $N=8$ (RAID 5), $N=16$ (RAID 6)

MTTDL for an installed base of systems storing 10PB of user data

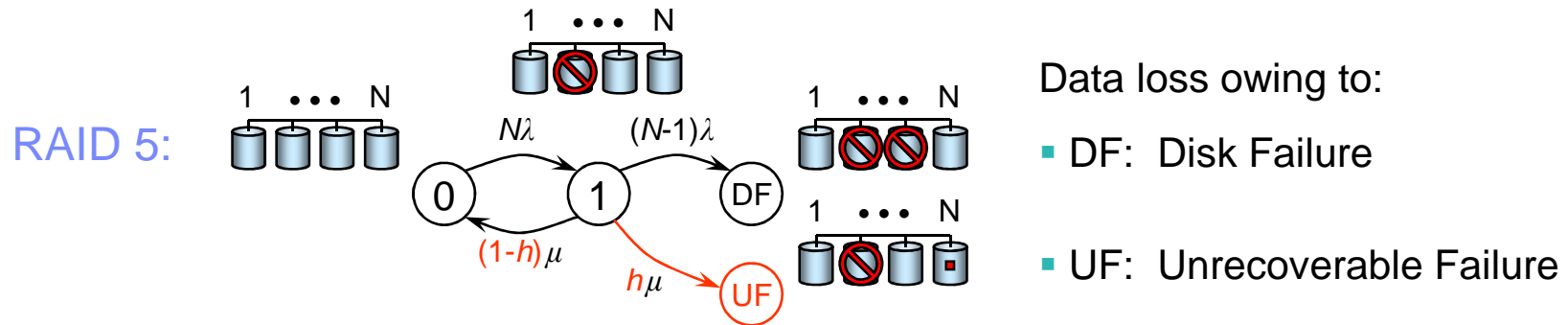


- The IDR scheme improves MTTDL by more than two orders of magnitude, which practically eliminates the negative impact of unrecoverable sector errors
- The scrubbing mechanism may not be able to reduce the number of unrecoverable sector errors sufficiently and reach the desired level of reliability

Enhanced MTTDL Equations for RAID Systems

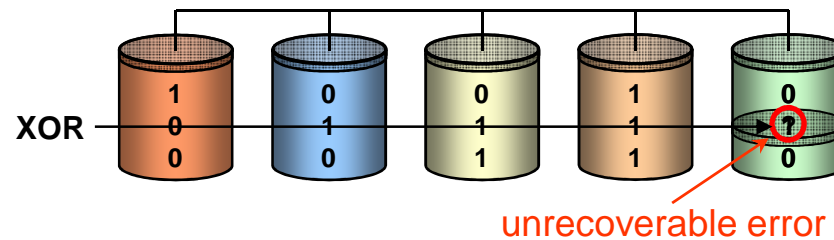
- Latent or unrecoverable errors

➤ $P_s = P(\text{sector error})$



- Disk scrubbing

- Periodically accesses disk drives to detect unrecoverable errors

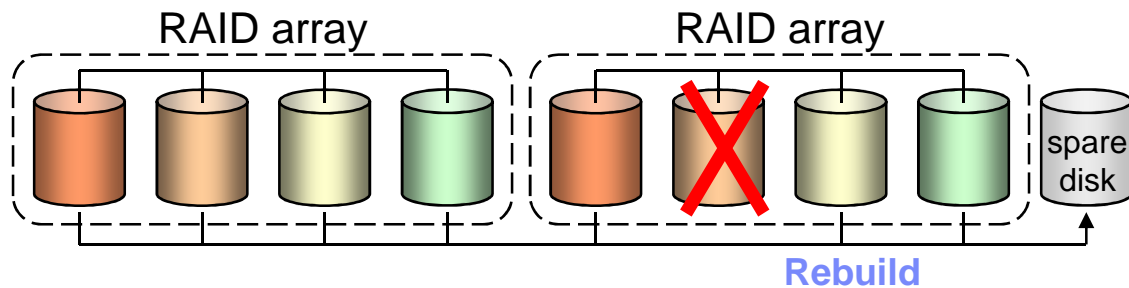


- Identifies unrecoverable errors at an early stage
- Corrects the unrecoverable errors using the RAID capability
- $P_s (\text{equivalent}) = P(\text{sector error} \mid \text{scrubbing is used})$

Distributed Storage Systems

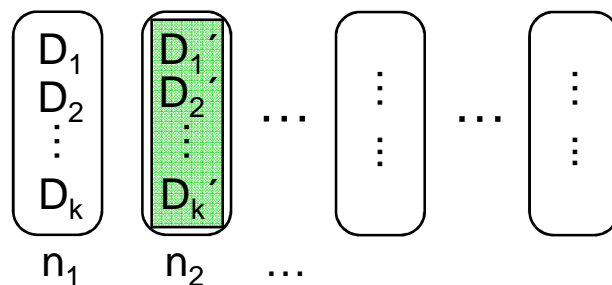
- **Markov models**

- Times to disk failures and rebuild durations exponentially distributed (-)
- MTTDL has been proven to be a useful metric for (+)
 - estimating the effect of the various parameters on system reliability
 - comparing schemes and assessing tradeoffs



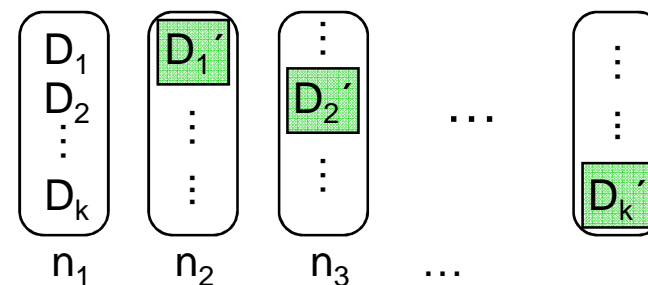
Reduce vulnerability window

- Distributing data
- Distributed rebuild method



- replicated data on the same node

Clustered Placement



- replicated data on different nodes

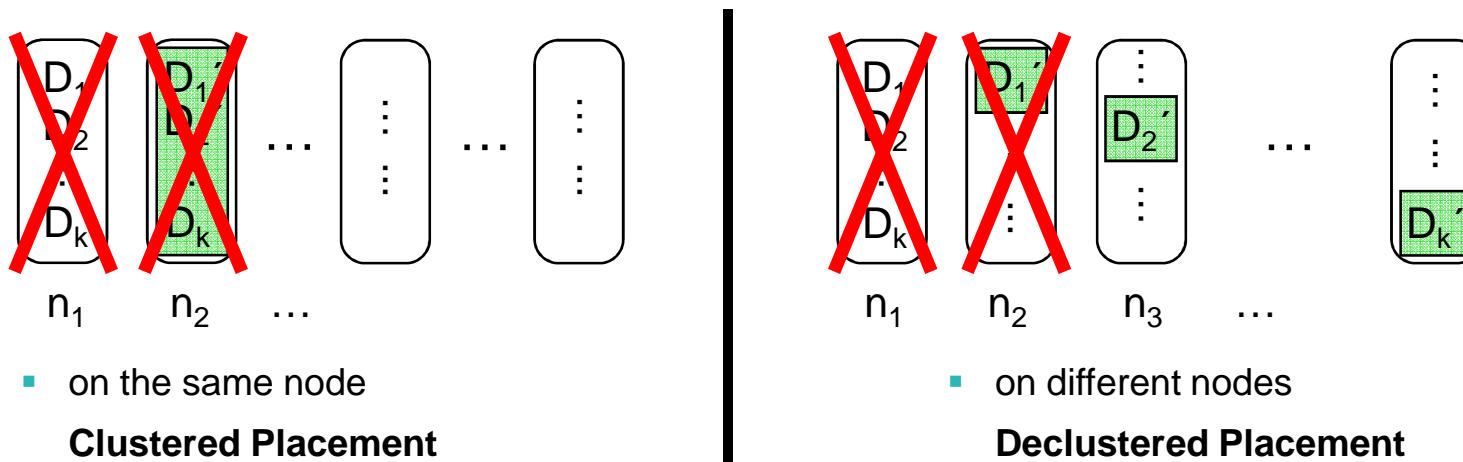
Declassed Placement

- **Non-Markov-based analysis**

- V. Venkatesan et al. "Reliability of Clustered vs. Declassed Replica Placement in Data Storage Systems", MASCOTS 2011
 - V. Venkatesan et al. "A General Reliability Model for Data Storage Systems", QEST 2012
- General non-exponential failure and rebuild time distributions
- MTTDL is insensitive to the failure time distributions; it depends only on the mean value

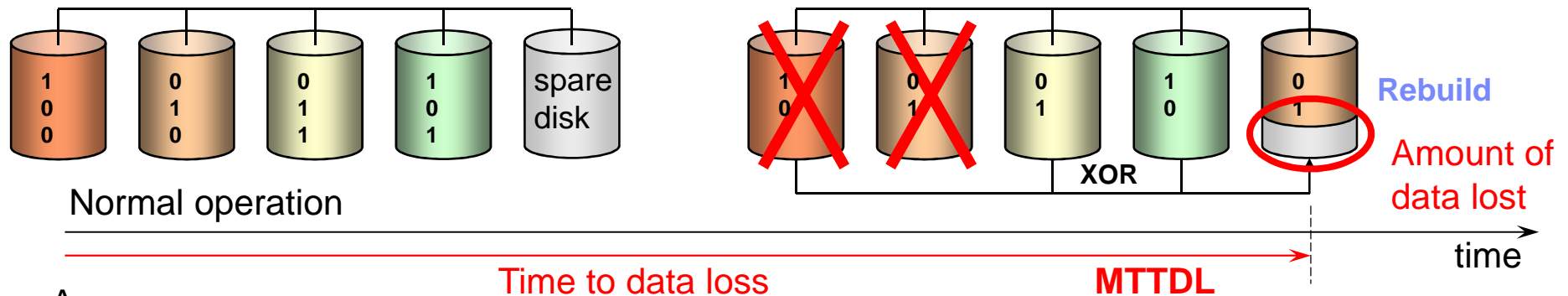
Time To Data Loss vs. Amount of Data Lost

- MTTDL measures time to data loss
 - no indication about amount of data loss
 - Consider the following example
 - Replicated data for D_1, D_2, \dots, D_k is placed:



- on the same node
Clustered Placement
 - on different nodes
Declassed Placement
- Distinguish between data loss events involving
 - high amounts of data lost
 - low amounts of data lost
 - Need for a measure that quantifies the amount of data lost

Expected Annual Fraction of Data Loss (EAFDL)

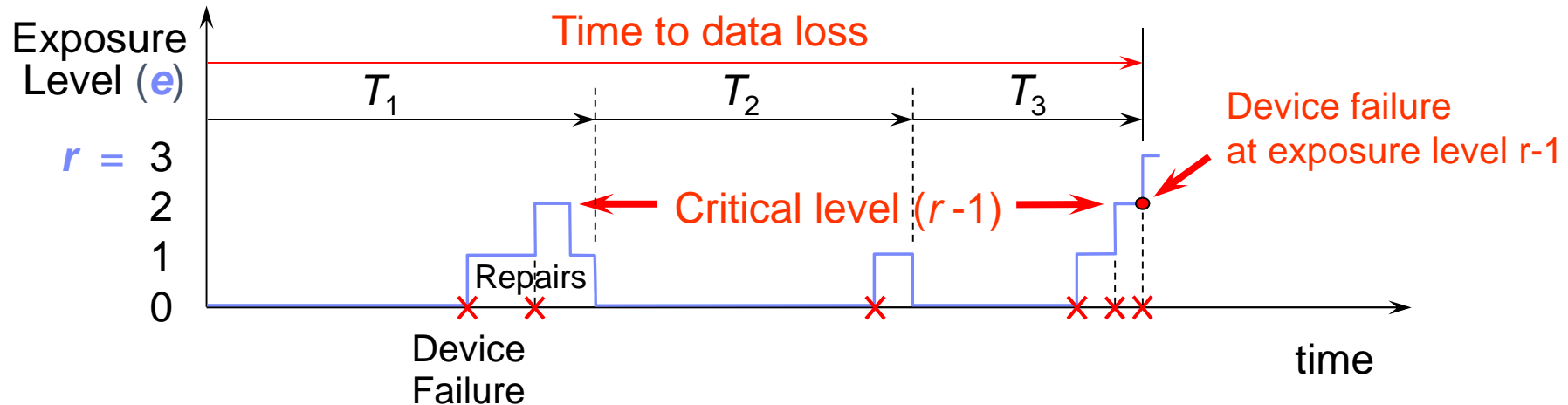


- Amazon
 - The Reduced Redundancy Storage option within Amazon S3 is designed to provide 99.999999999% durability of objects over a given year
 - average annual expected loss of a fraction of 10^{-11} of the data stored in the system
- Data loss events documented in practice by Yahoo!, LinkedIn, and Facebook
- Assess the implications of system design choices on the
 - frequency of data loss events
 - MTTDL
 - amount of data lost
 - **Expected annual fraction of data loss (EAFDL)**
 - Fraction of stored data that is expected to be lost by the system annually
 - EAFDL metric is meant to complement, not to replace MTTDL
 - These two metrics provide a useful profile of the magnitude and frequency of data losses
 - for storage systems with similar EAFDL
 - ✓ most preferable the one with the maximum MTTDL

Previous Work on Storage Reliability

Reliability Measure	Theory / Analysis	Simulation
MTTDL	<ul style="list-style-type: none"> ▪ Markov models <ul style="list-style-type: none"> – Original RAID-5 and RAID-6 MTTDL equations – Enhanced MTTDL Equations <ul style="list-style-type: none"> ➤ Latent or unrecoverable errors ➤ Scrubbing operations ▪ Non-Markov-based models <ul style="list-style-type: none"> – General non-exponential failure and rebuild time distributions – Placement schemes – Network bandwidth, Latent errors, Erasure codes 	Non-Markov-based MTTDL simulations
Other Metrics	<p>I. Iliadis and V. Venkatesan, “Expected Annual Fraction of Data Loss as a Metric for Data Storage Reliability” IEEE MASCOTS September 2014</p>	<ul style="list-style-type: none"> ▪ Normalized Magnitude of Data Loss (NOMDL) ▪ Fraction of Data Loss Per Year (FDLPY)* <p>* equivalent to EAFDL</p>

Non-Markov Analysis for EAFDL and MTTDL



- EAFDL evaluated in parallel with MTTDL

- r : Replication Factor
- e : Exposure Level: maximum number of copies that any data has lost
- T_i : Cycles (Fully Operational Periods / Repair Periods)
- P_{DL} : Probability of data loss during repair period
- U : Amount of user data in system
- Q : Amount of data lost upon a first-device failure

$$\text{MTTDL} \approx \sum_{i=1}^m E(T_i) \approx \frac{E(T)}{P_{DL}} \quad \text{EAFDL} = \frac{E(Q)}{E(T) \cdot U}$$

MTTDL / EAFDL equations obtained using non-Markov Analysis

Theoretical Results

- n : number of storage devices
- c : amount of data stored on each device
- r : replication factor
- b : reserved rebuild bandwidth per device
- $1/\lambda$: mean time to failure of a storage device

4 to 64

12 TB

2, 3, 4

96 MB/s

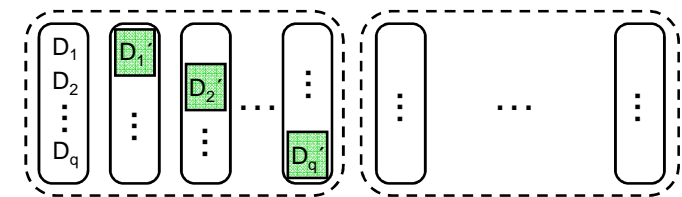
10,000 h - Weibull distributions with shape parameters greater than one

➤ increasing failure rates over time

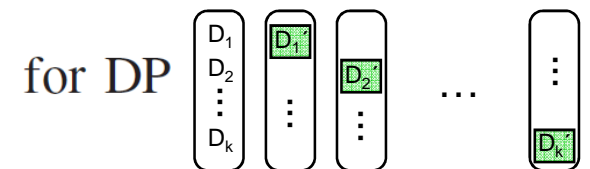
- shape parameter = 1.5

$$\text{MTTDL} \approx \begin{cases} \left(\frac{b}{\lambda c}\right)^{r-1} \frac{1}{n \lambda}, \\ \left(\frac{b}{2 \lambda c}\right)^{r-1} \frac{(r-1)!}{n \lambda} \prod_{e=1}^{r-2} \left(\frac{n-e}{r-e}\right)^{r-e-1} \end{cases}$$

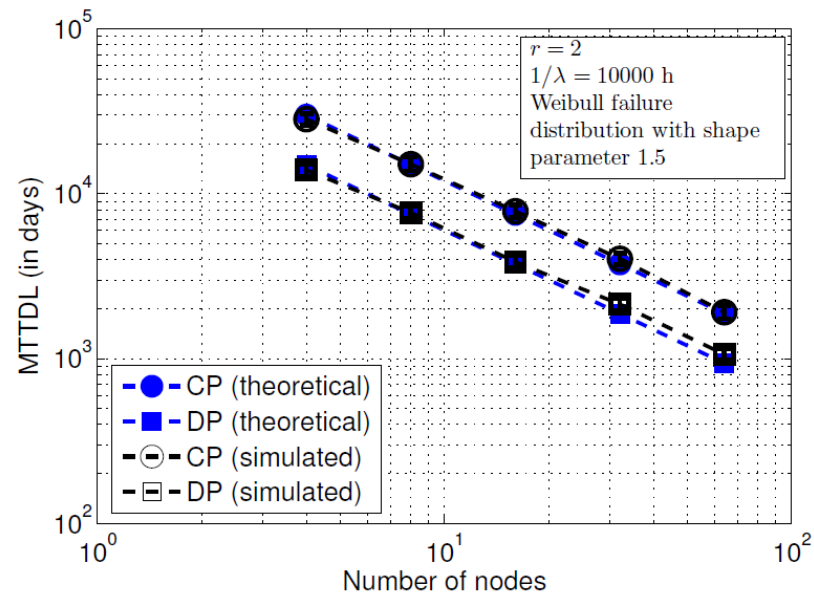
$$\text{EAFDL} \approx \begin{cases} \left(\frac{\lambda c}{b}\right)^{r-1} \lambda, \\ \left(\frac{2 \lambda c}{b}\right)^{r-1} \frac{\lambda}{(r-1)!} \prod_{e=1}^{r-1} \left(\frac{r-e}{n-e}\right)^{r-e} \end{cases}, \text{ for DP}$$



Symmetric placement



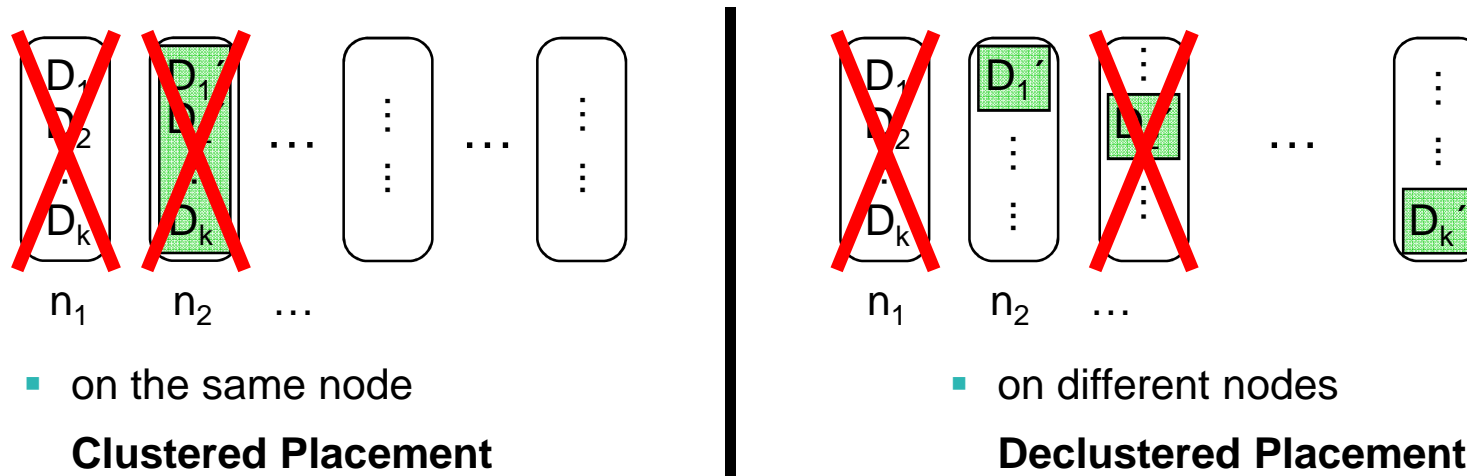
Reliability Results for Replication Factor of 2



- MTDL
 - Decentralized placement is not better than clustered one

Distributed Storage Systems

Replicated data for D_1, D_2, \dots, D_k is placed:



- on the same node

Clustered Placement

- on different nodes

Declustered Placement

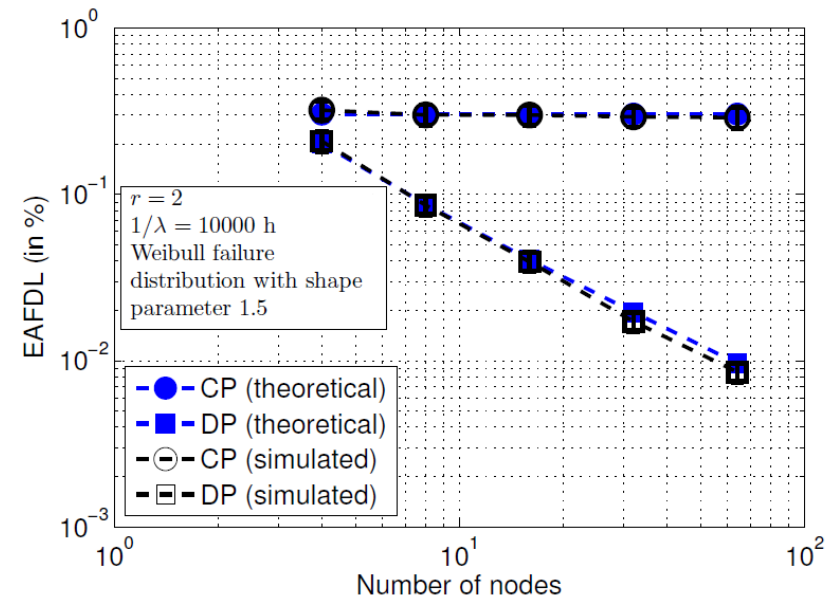
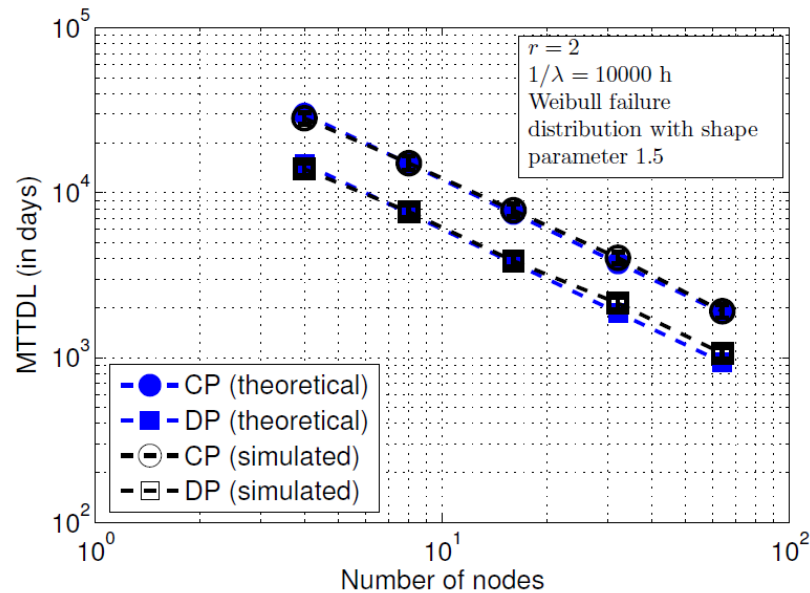
- MTTDL

- Reduced repair time (+)
- Reduced vulnerability window
- Increased exposure to subsequent device failures (-)

- EAFDL

- Reduced amount of data lost (+)

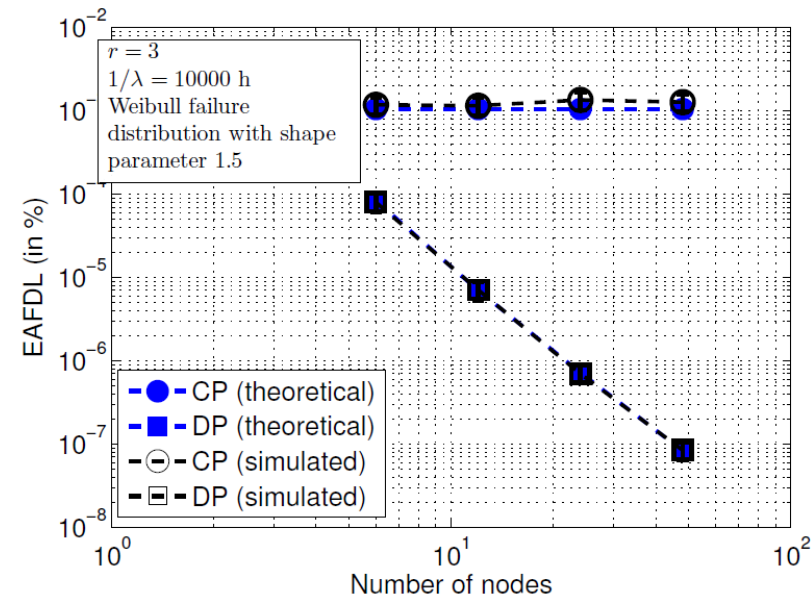
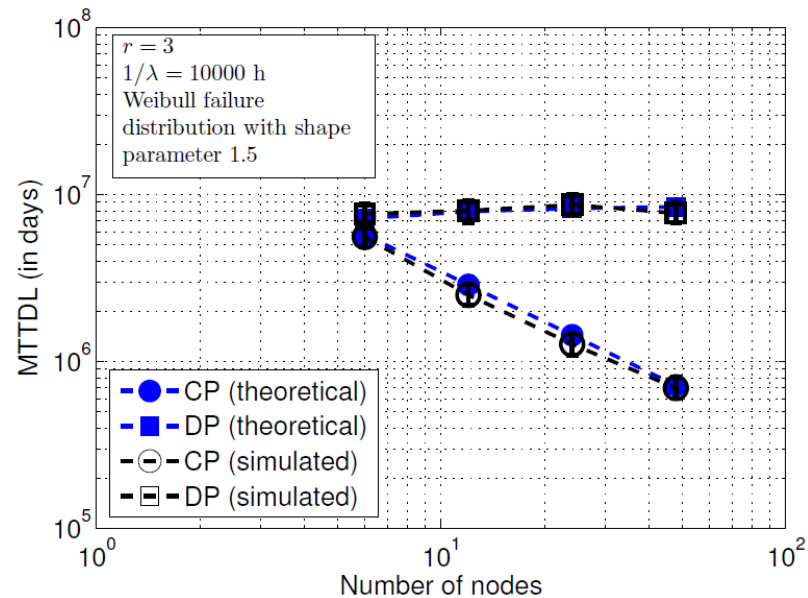
Reliability Results for Replication Factor of 2



- MTTDL
 - Declustered placement not better than clustered one

- EAFDL
 - Independent of the number of nodes for clustered placement
 - Inversely proportional to the number of nodes for declustered placement
 - Declustered placement better than clustered one

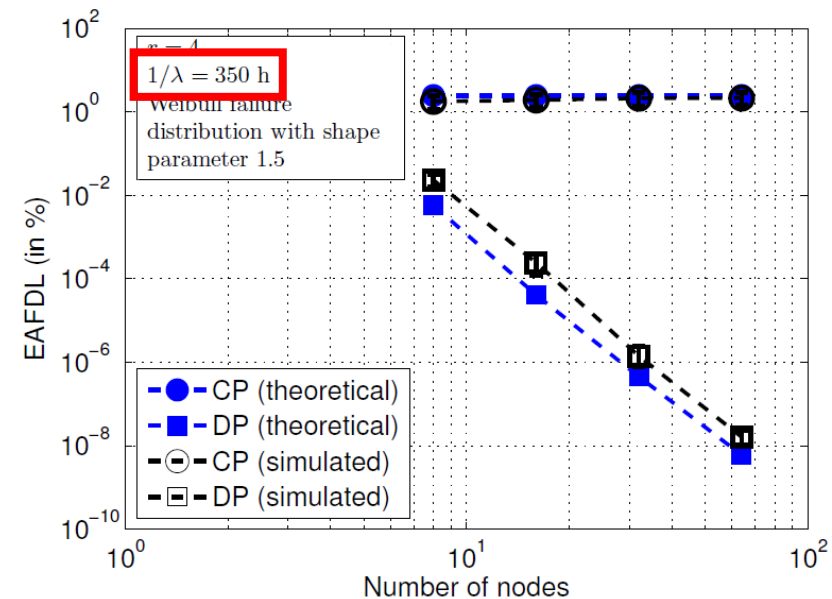
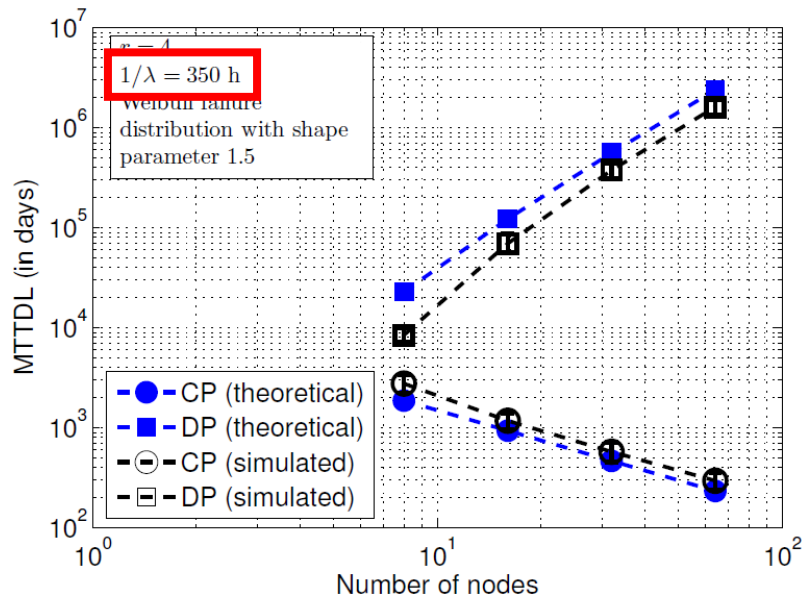
Reliability Results for Replication Factor of 3



- MTTDL
 - Inversely proportional to the number of nodes for clustered placement
 - Independent of the number of nodes for declustered placement
 - Declustered placement better than clustered one

- EAFDL
 - Independent of the number of nodes for clustered placement
 - Inversely proportional to the **cube** of the number of nodes for declustered placement
 - Declustered placement better than clustered one

Reliability Results for Replication Factor of 4



MTTR/MMTF ratio: $34.7/350 \approx 0.1$ not very small \Rightarrow Deviation between theory and simulation

■ MTDL

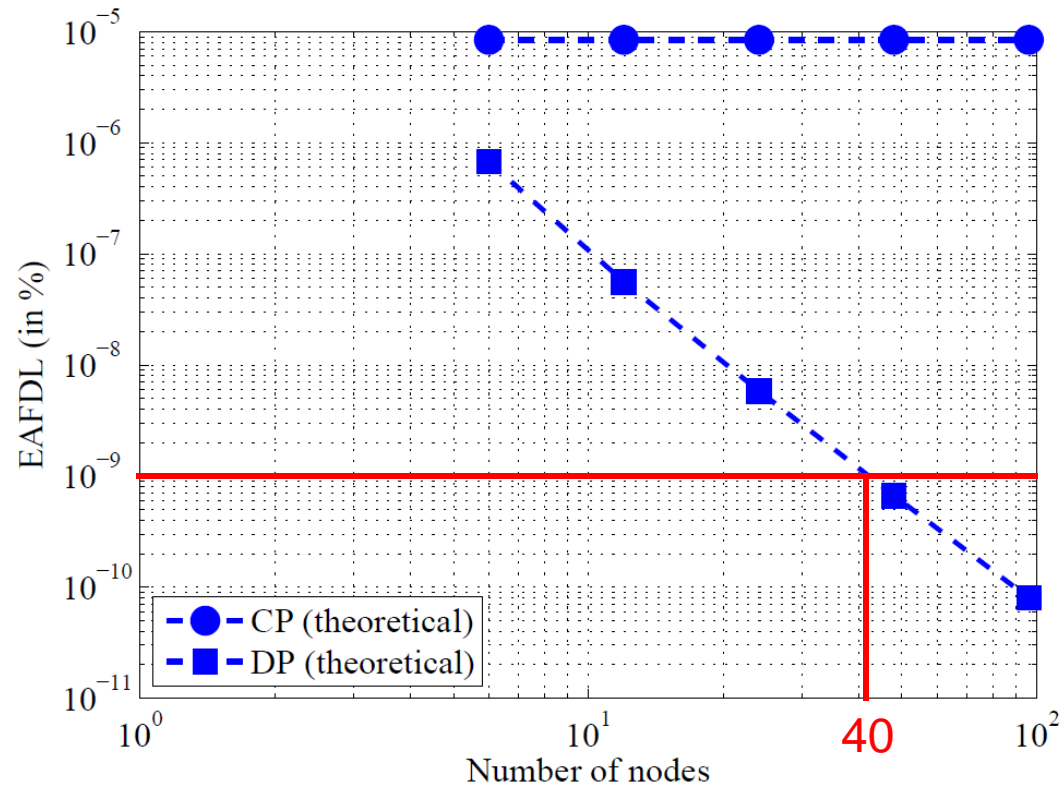
- Proportional to the **square** of the number of nodes for declustered placement
 - Declustered placement far superior to the clustered one

■ EAFDL

- Inversely proportional to the **sixth power** of the number of nodes for declustered placement
 - Declustered placement far superior to the clustered one

Theoretical EAFDL Results for Replication Factor of 3

$$\text{MTTF} = 1/\lambda = 50,000 \text{ h}$$



- Theoretical results are accurate when devices are very reliable
 - MTTR/MTTF ratio is small
 - Quick assessment of EAFDL
 - No need to run lengthy simulations

Discussion

- EAFDL should be used cautiously
 - suppose EAFDL = 0.1%
 - this does not necessarily imply that 0.1% of the user data is lost each year
 - System 1: MTTDL=10 years 1% of the data lost upon loss
 - System 2: MTTDL=100 years 10% of the data lost upon loss
 - The desired reliability profile of a system depends on the
 - application
 - underlying service
 - If the requirement is that data losses should not exceed 1% in a loss event
 - only <System 1> could satisfy this requirement

Summary

- Reviewed the widely used mean time to data loss (MTTDL) metric
- Demonstrated that unrecoverable errors are becoming a significant cause of user data loss
- Considered the expected annual fraction of data loss (EAFDL) metric
- Established that the EAFDL metric, together with the traditional MTTDL metric
 - provide a useful profile of the magnitude and frequency of data losses
 - can be jointly evaluated analytically in a general theoretical framework
- Derived the MTTDL/EAFDL in the case of replication-based storage systems that use clustered and declustered data placement schemes and for a
 - large class of failure time distributions
 - real-world distributions, such as Weibull and gamma
- Demonstrated the superiority of the declustered placement scheme

Future Work

- Apply the methodology developed to derive the reliability of systems using other redundancy schemes, such as erasure codes