

# Recovering Shape from Endoscope Image Using Eikonal Equation

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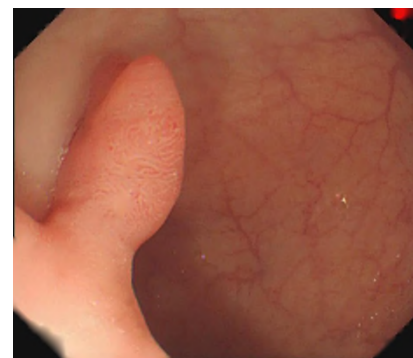
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# Introduction

- Endoscope is used to detect polyps and the examinations of abnormal parts in the stomach and intestines.
  - ✓ Polyps have a variety of sizes and shapes.
  - ✓ Medical doctors estimate the size and shape of polyp empirically.



Endoscope image



This paper proposes a new approach for a polyp shape and size recovery by solving Eikonal Equation under the condition of point light source and perspective projection for a supporting system of medical diagnosis.

## Preprocessing: Removal of Specular Reflectance Component and Generation of Lambertian Image [3]

Step 1: Classification using histogram of H

Step 2: Calculate the V ratio between interest color points and those neighboring points whose color is most frequent color.

Step 3: Equation of reflectance using V ratio calculated in Step 2 using the points which are not used in Step 2 of interest color.

Step 4: Equalization of reflectance for all color groups by repeat Step 2 and Step 3.

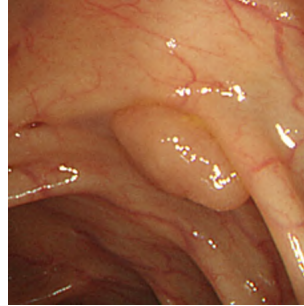
[3] N. Ikeda et al. "Generating Lambertian Image by Removing Specular Reflection Component and Difference of Reflectance Factor Using HSV, Proc, of ITC-CSCC 2016, pp.5470550, 2016.

# Experiment using actual image

**Endoscope  
images**



**Image1**

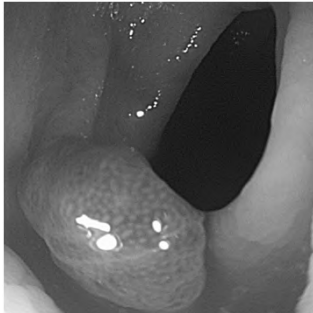


**Image2**

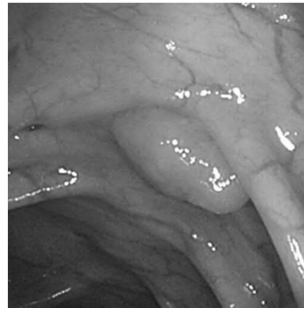


**Image3**

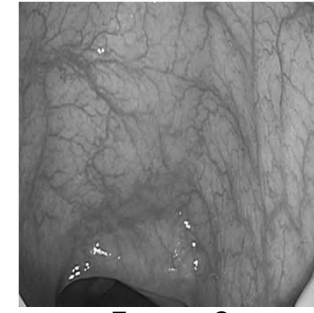
**Grayscale  
images**



**Image1**

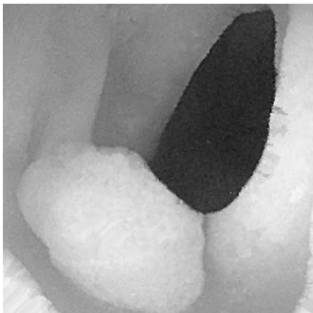


**Image2**



**Image3**

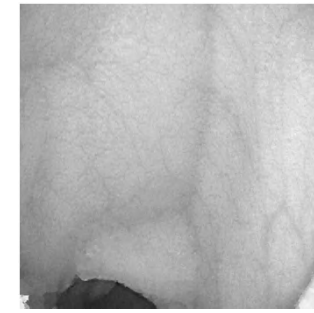
**Result  
images**



**Image1**



**Image2**



**Image3**

# Proposed Method

Photometric Constraint Equation and Geometric Constraint Equation should become the same depth value of Z for both.

Photometric Equation

Geometric Equation

$$\sqrt{\frac{CV(-px - qy + f)}{E(p^2 + q^2 + 1)^{\frac{1}{2}}}} = \frac{Z_k(f - p_k x_k - q_k y_k)}{f - p_k x_t - q_k y_t}$$



Eikonal Equation

Eq.(4)

$$\sqrt{p^2 + q^2} = \sqrt{\left(\frac{C}{E}\right)^2 A - 1} \quad A = \frac{V^2(f - p_k x_t - q_k y_t)^6}{Z_k^4(f - p_k x_k - q_k y_k)^4}$$

**C** : Reflectance Factor

**f** : Focal Length

**E** : Image Intensity

**(p, q)** : Gradient Parameters

**(x, y)** : Image Coordinate

**(x<sub>k</sub>, y<sub>k</sub>)** (x,y) at known point

**(p<sub>k</sub>, q<sub>k</sub>)** (p,q) at known point

**(x<sub>t</sub>, y<sub>t</sub>)** (x,y) at trial point

**Z<sub>k</sub>** Depth at known point

Fast Marching Method

$$Z_{ij} = \begin{cases} \frac{Z_a + Z_b + \sqrt{2f_{ij}^2 - (Z_a - Z_b)^2}}{2} & (|Z_a - Z_b| < f_{ij}) \\ \min(Z_a, Z_b) + f_{ij} & (|Z_a - Z_b| \geq f_{ij}) \end{cases}$$

$$Z_a = \min(Z_{i-1,j}, Z_{i+1,j})$$

$$Z_b = \min(Z_{i,j-1}, Z_{i,j+1})$$

**(i, j)** specified pixel

**f<sub>ij</sub>** corresponds to the inverse of right term of Eq.(4)

# Estimating $C$ and Absolute Size

- Step1. SIFT (in Ref.[6]) or ORB (in Ref.[7]) feature points extracted from blood vessels using two images and movement  $\Delta Z$  of endoscope camera is estimated.
- Step2. Parameter  $C$  is estimated using  $\Delta Z$  (See Ref.[6]).
- Step3. Shape recovery is applied for each uniform Lambertian image generated by Ref.[3].

[6] Y. Iwahori et al. “Estimating Reflectance Parameter of Polyp Using Medical Suture Information in Endoscope Image”, Proc. of ICPRAM 2016, pp.503-509, 2016.

# Absolute size of polyp using two images with slight movement of $\Delta Z$

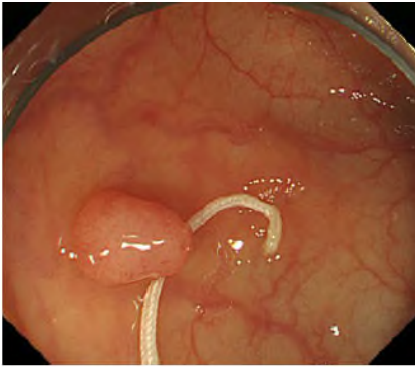


Figure 3: Input Image 1 (Experiment 1)

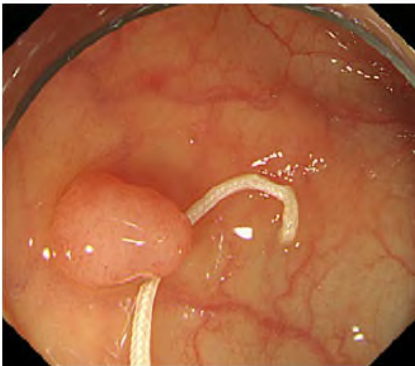


Figure 4: Input Image 2 (Experiment 1)

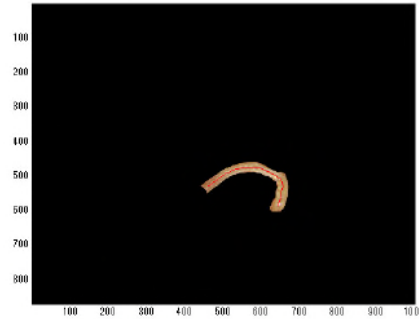


Figure 5: Medical Suture Region of Image 1 (Experiment 1)

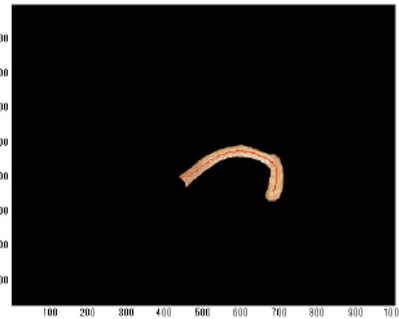


Figure 6: Medical Suture Region of Image 2 (Experiment 1)

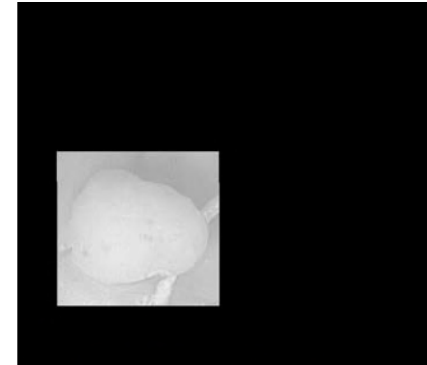
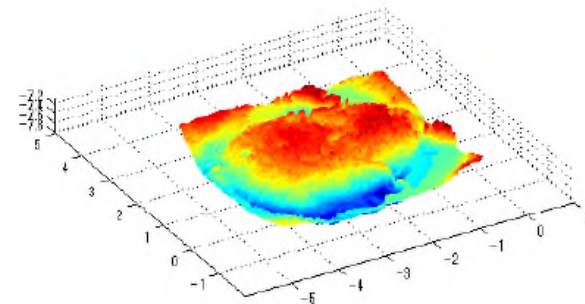


Figure 7: Test Object (Experiment 1)



These results are obtained from Ref.[6] and recovering algorithm is different one.  
[6] Y. Iwahori et al. "Estimating Reflectance Parameter of Polyp Using Medical Suture Information in Endoscope Image", Proc. of ICPRAM 2016, pp.503-509, 2016.