

Non-Linear Modeling and Sensitive Analysis of a Magnetostrictive Force Sensor

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Outline

1. Introduction:

- Magnetostrictive materials and their applications
- Research background: Magnetostrictive force sensors

2. Problem and Objectives:

- Non-linear model of magnetostrictive force sensor
- Simulation of non-linear model

3. Sensitive Analysis:

- Specify the effective parameters on the sensor's performance
- Investigate the linearity and sensitivity of the sensor

4. Conclusions and Future Plans

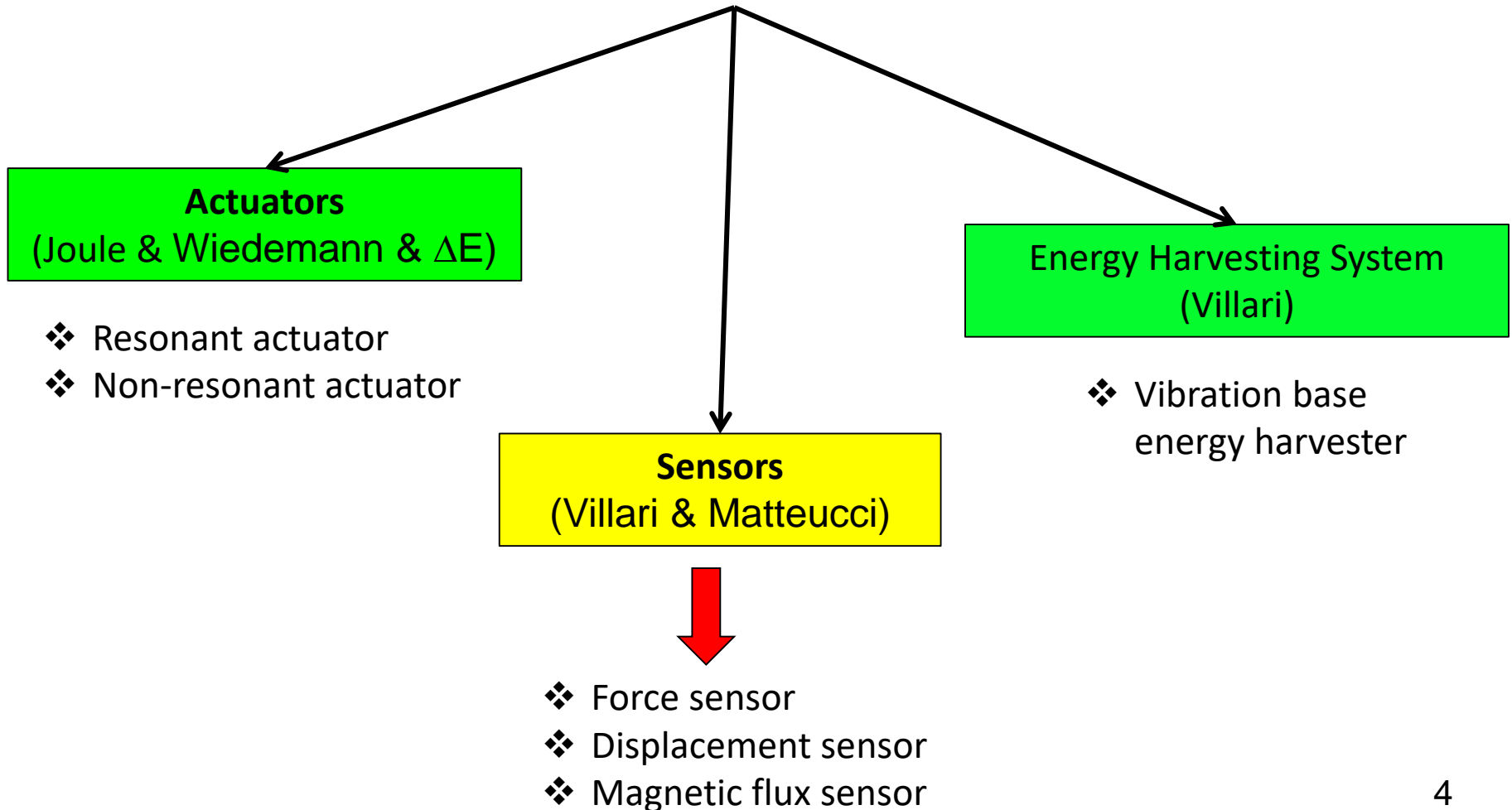
Magnetostrictive Materials:

Exhibit changes in **material properties** in response to externally imposed **magnetic field**.

Five Effects:

1. Joule effect (actuator)
2. Villari effect (**sensor** & harvester)
3. Wiedemann effect (actuator)
4. Matteucci effect (**sensor** & harvester)
5. ΔE effect (actuator)

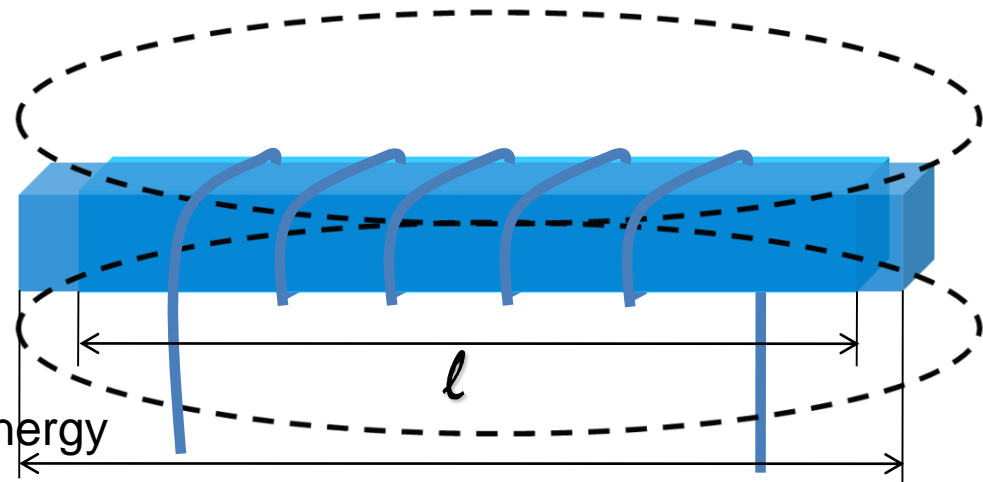
Magnetostrictive



Introduction: Magnetostrictive Effects

Joule effect

Iron: 6 ppm
 Nickel: -30 ppm
 Permandur: 70 ppm
 Terfenol-D: 2000 ppm (Brittle)

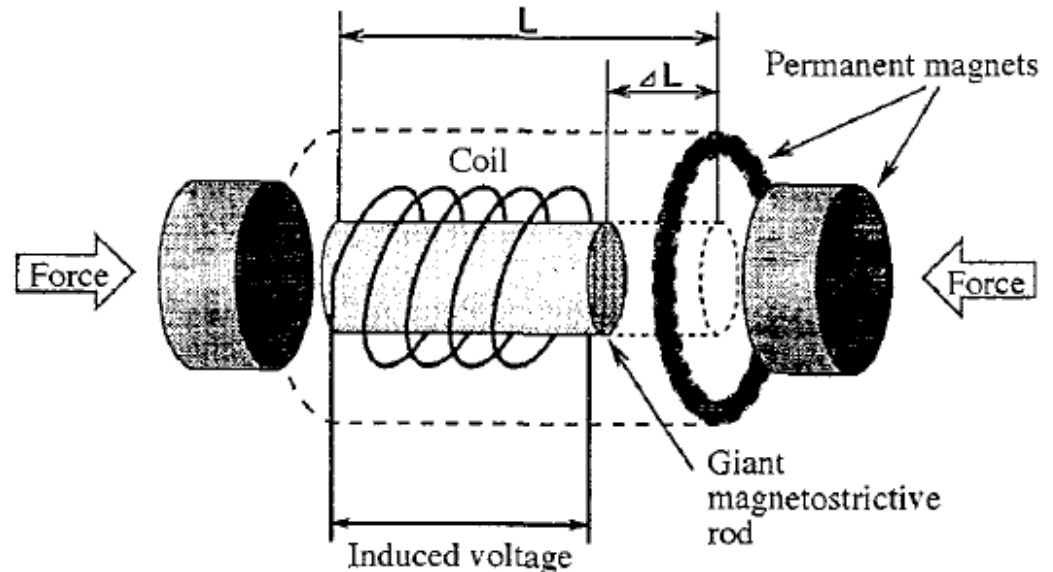


Villari effect

Applied the force

Magnetisation along the direction of magnetic field will be change

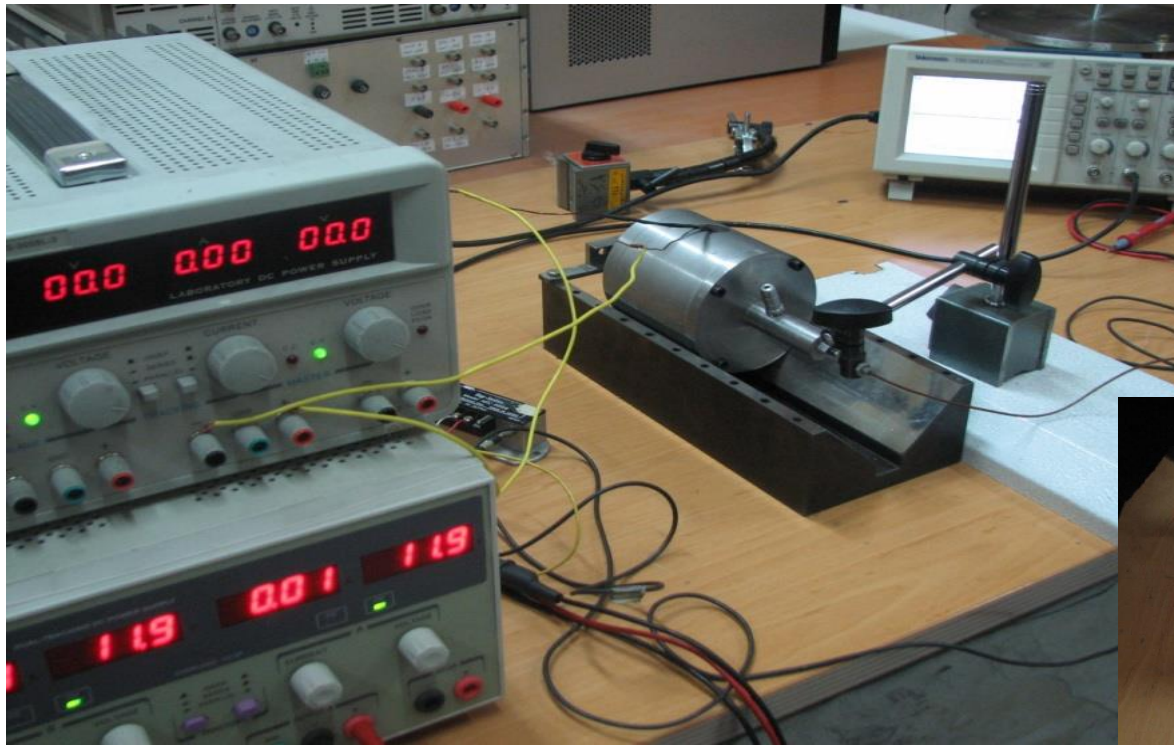
The flux variation induced voltage in the coil



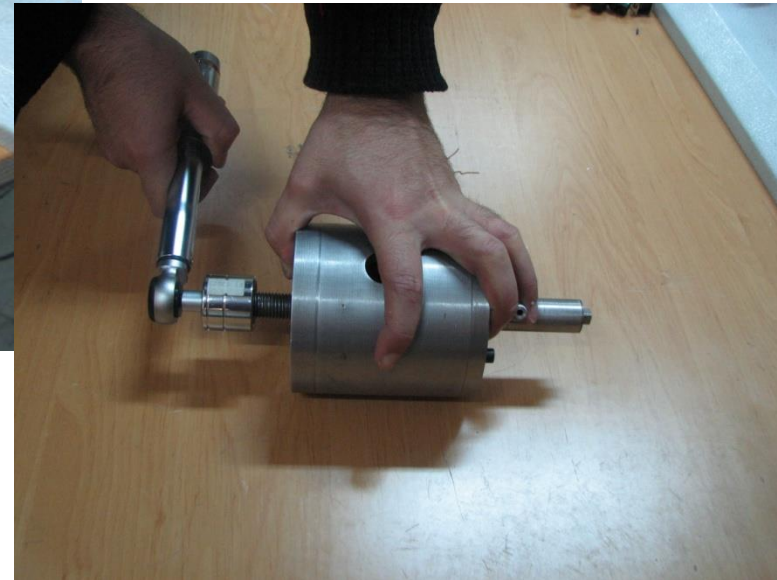
Mechanical energy → change of magnetic energy

Introduction: Applications: Gasoline Direct Injector

Joule Effect



Non-resonant Actuator

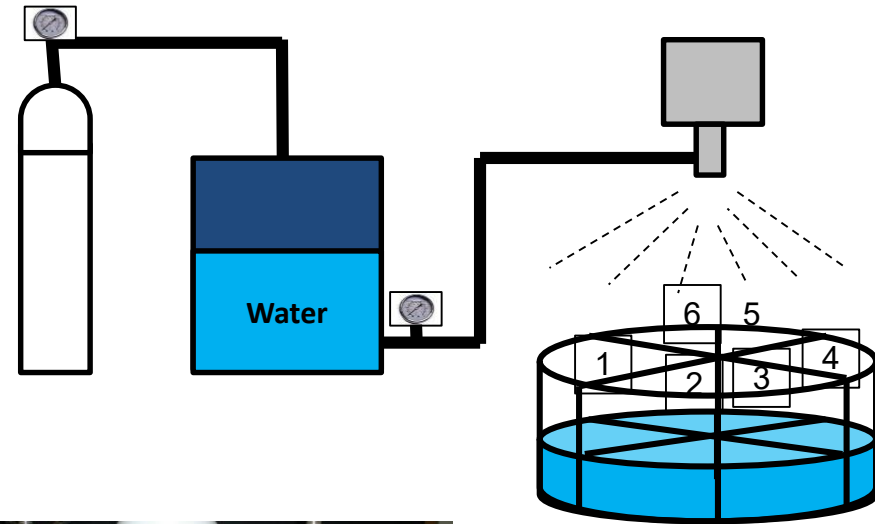


Gasoline Direct Injector

[Ghodsi, IEEE Industry Applications Magazine, 2017]

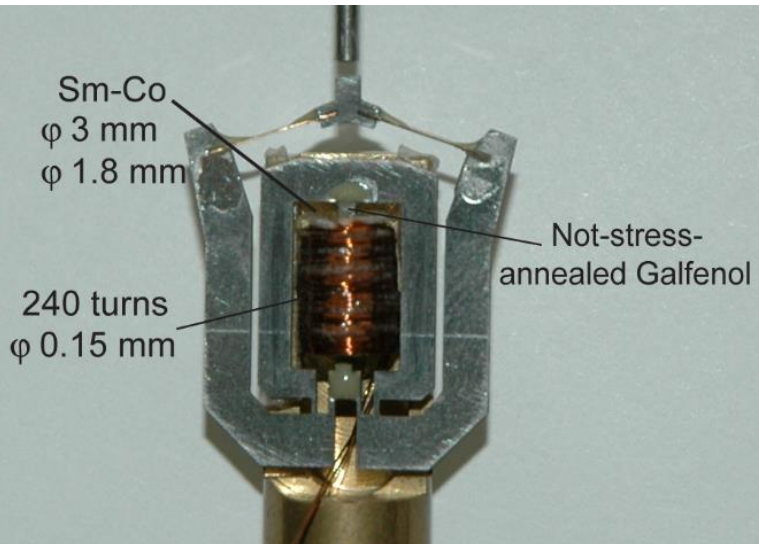
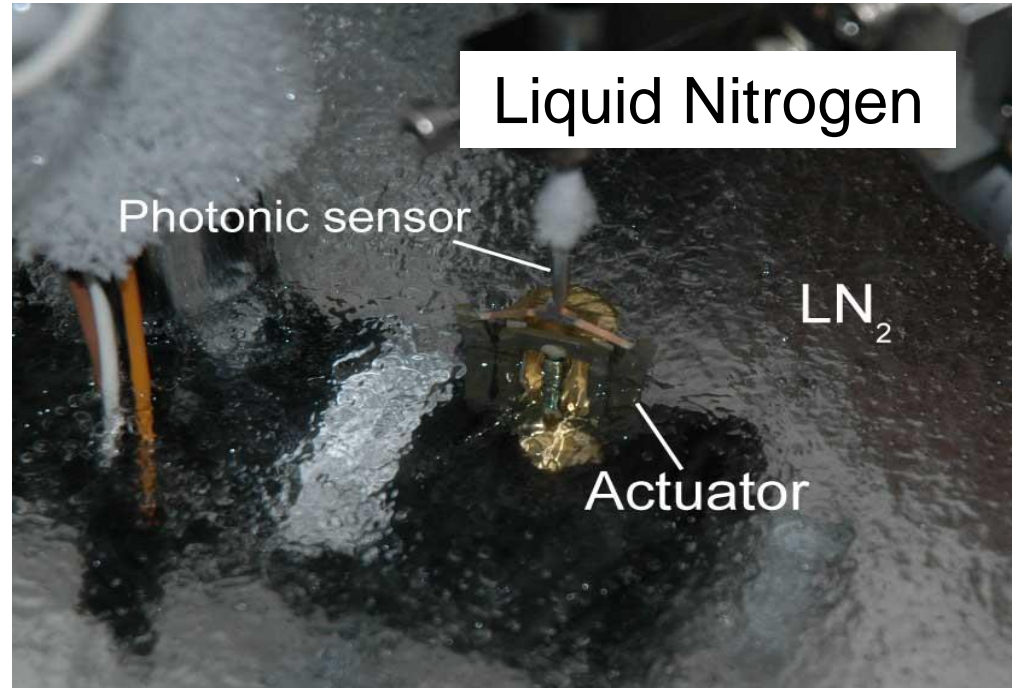
Introduction: Applications: Cold Test of GDI

Cold Test: Experimental Results of Symmetrical Injection



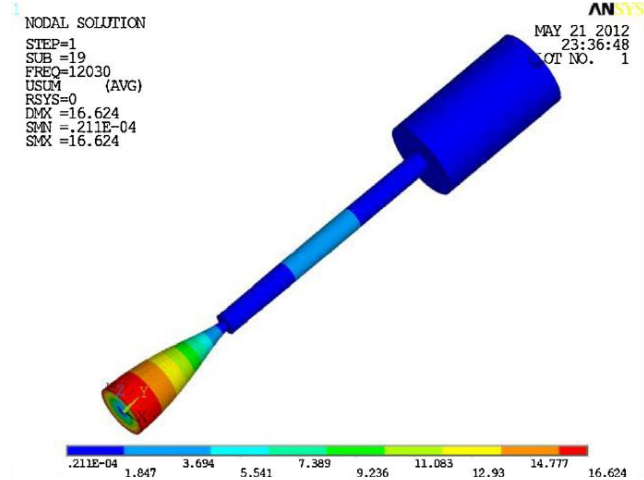
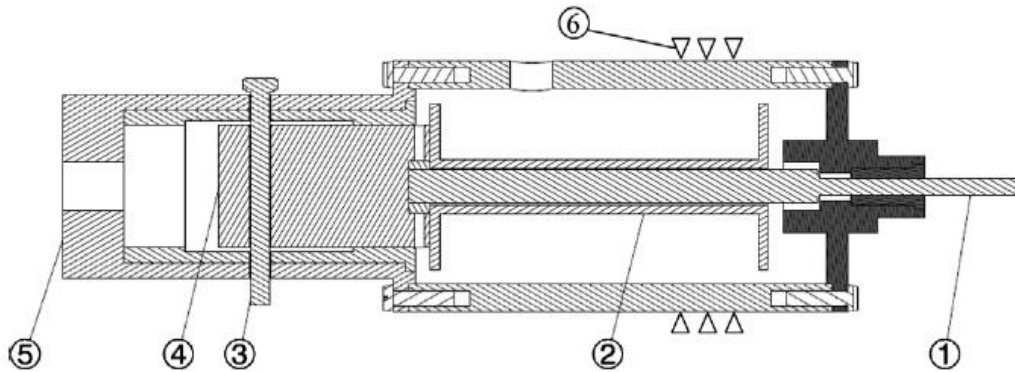
Joule Effect

Introduction: Applications: Actuator in liquid Nitrogen

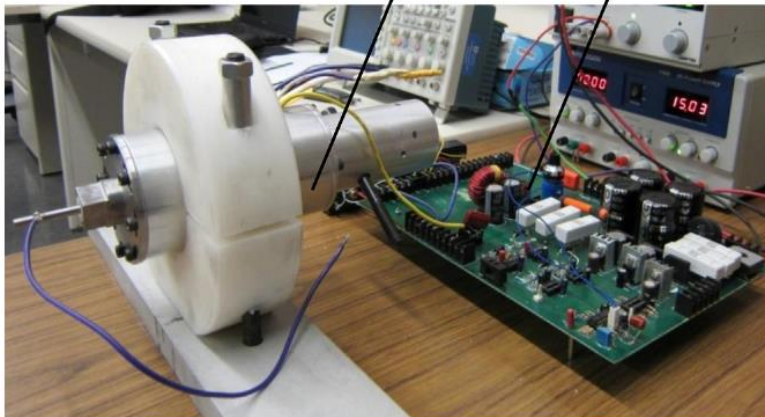


Magnification system using
Galfenol and Permendur
[Ghodsi, Ueno, Yano, Intermag 2008]

Introduction: Applications: Bone Drilling



MTRT Switching Power Supply



Wiedemann
Effect

Resonant Torsional Actuator

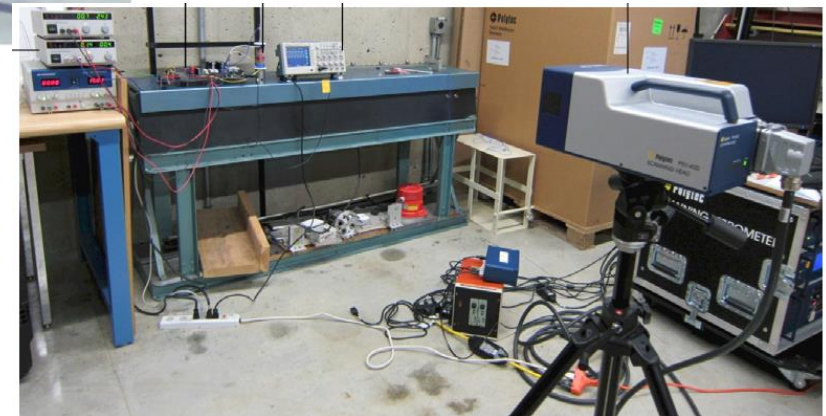
Wiedemann effect, [Ghodsi, Sensor and actuator, 2013]

Introduction: Applications: Bone Drilling

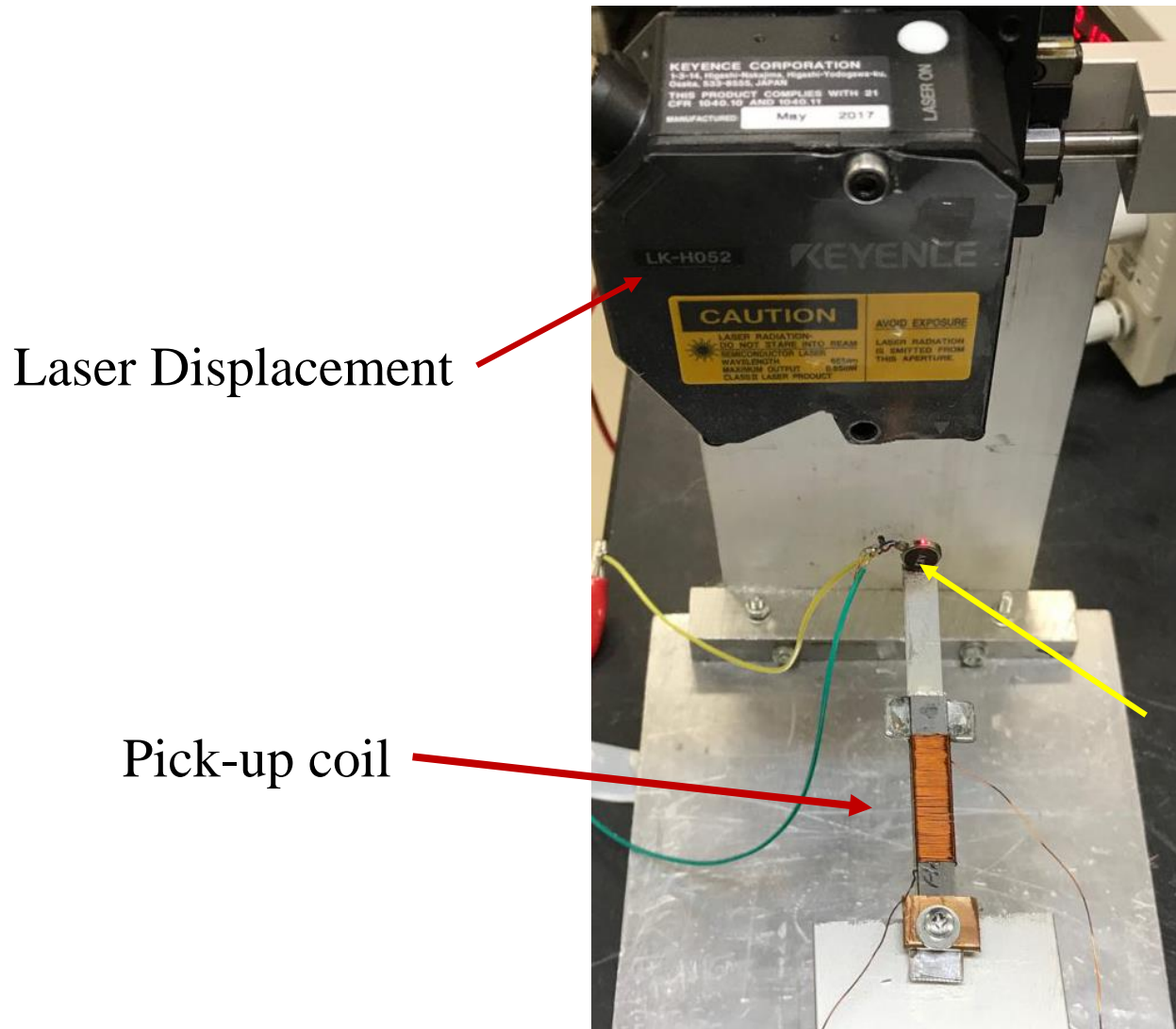


Wiedemann
Effect

Hybrid Longitudinal-Torsional
[Ghodsi 2013]

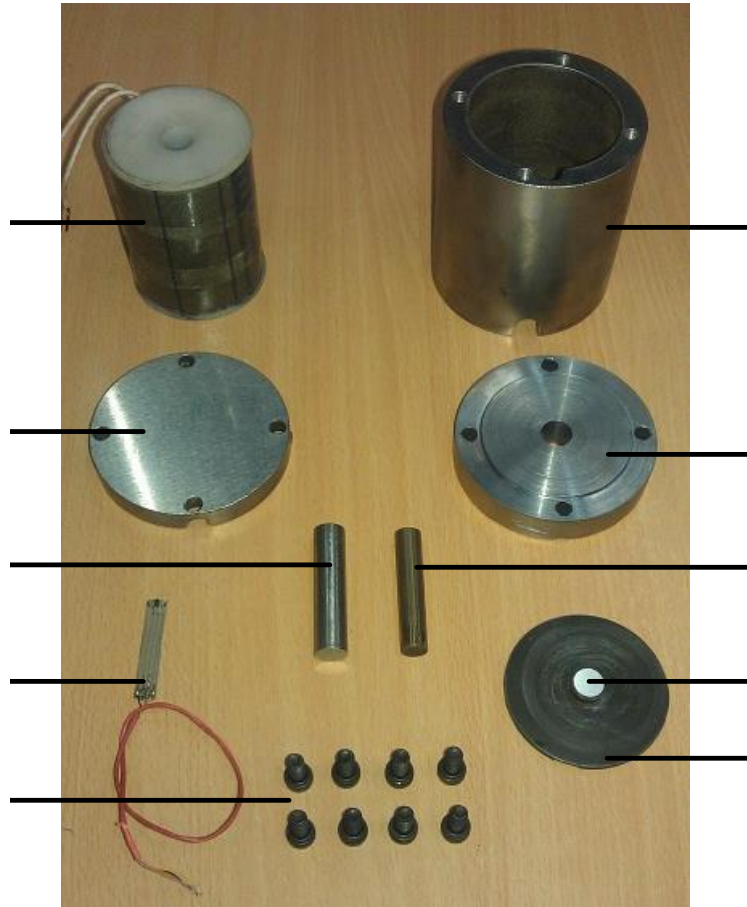


Introduction: Applications: Energy Harvester



[Ghodsi,Energy,2019]

Introduction: Applications: Force Sensor



[Ghodsi,2012]



Villari Effect

Introduction: Force Sensor



[Strainsense]

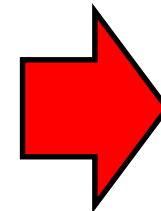
Conventional Force
sensor (Strain gauge)

- Static applications



[Ghodsi, 2015]

Smart material force
sensor



- Dynamic applications

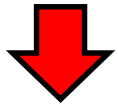
Research Background: Magnetostrictive Force Sensors

Year	Author	Mechanism	Material	Description
2015	Ghodsi	Rod configuration	Terfenol-D	Linear Modeling
2017	Zhu	Rod configuration	Terfenol-D	Frequency effect
2018	Li	Cantilever beam	Galfenol	Small force range (0-5 N)
2020	Shu	Cantilever beam	Galfenol	Suitable for Impact force

Challenge and Objectives

Challenge:

The developed Magnetostrictive force sensors suffer from low **sensitivity** and **linearity**.



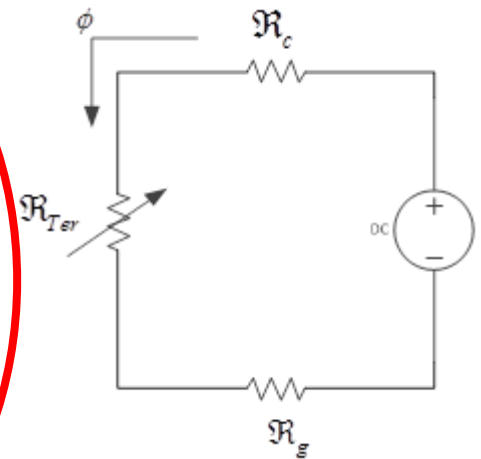
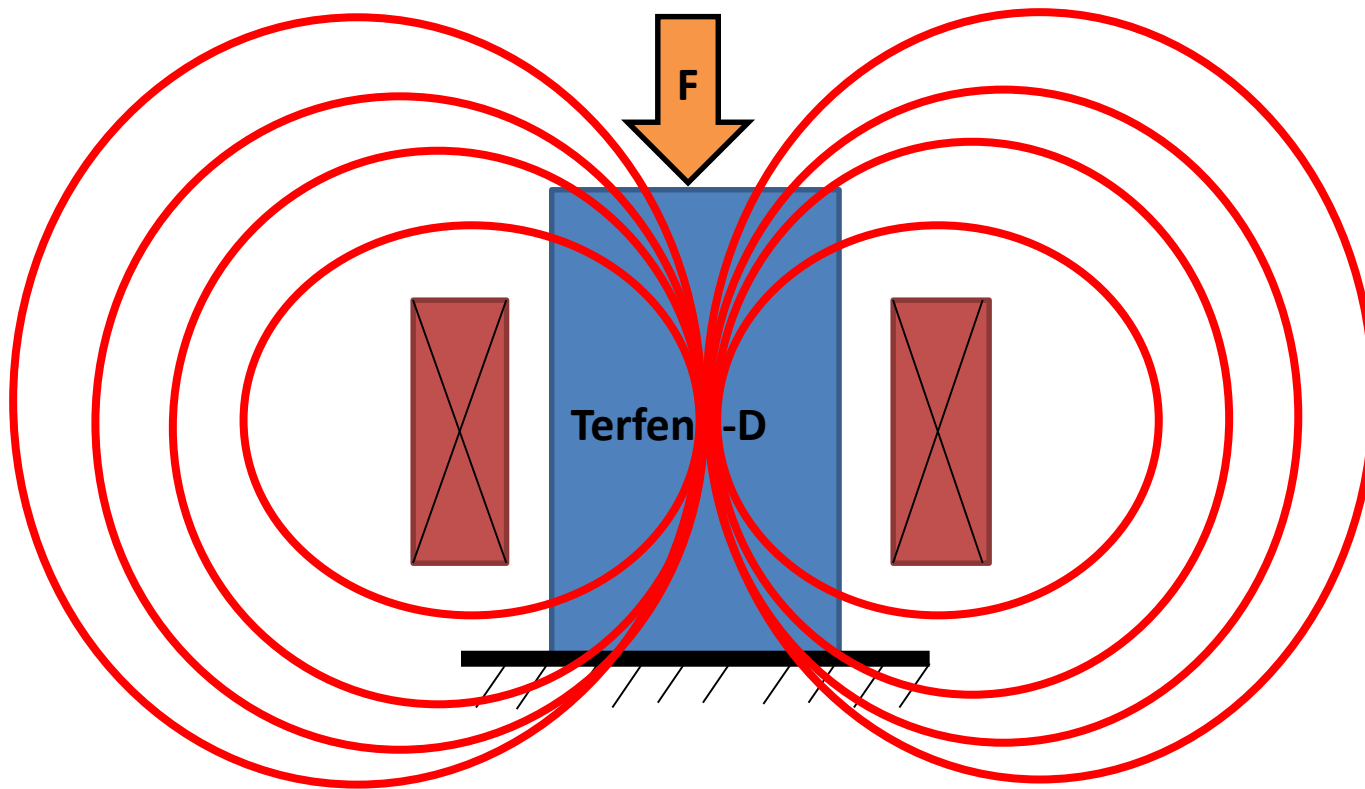
Objective I:

Develop an **accurate model** to predict the **sensitivity** of the sensor by combining the non-linear magneto-mechanical model and the Faraday's law.

Objective II:

Find the **effective parameters** on sensitivity and non-linearity to optimize the performance of the force sensor.

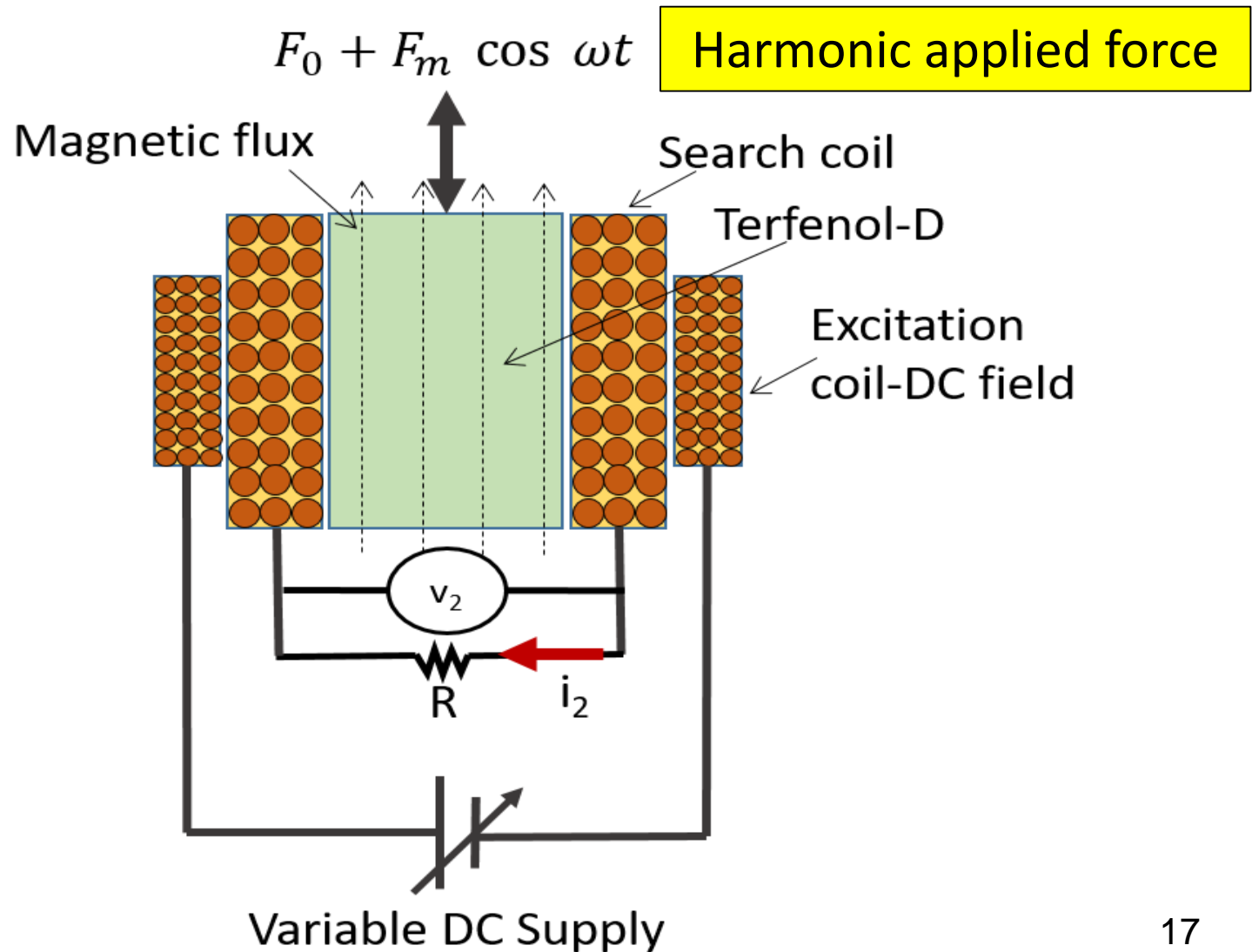
Principle of Force Sensor



$$\left(\mathfrak{R}_{Ter} = \frac{L_{Ter}}{\mu_0 \mu_{r_{Ter}} A_{Ter}} \right)$$

Villari Effect

Structure of the Force Sensor

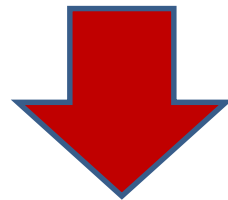


Mechanical Modelling of Force Sensor

Non-linear magneto-mechanical relation:

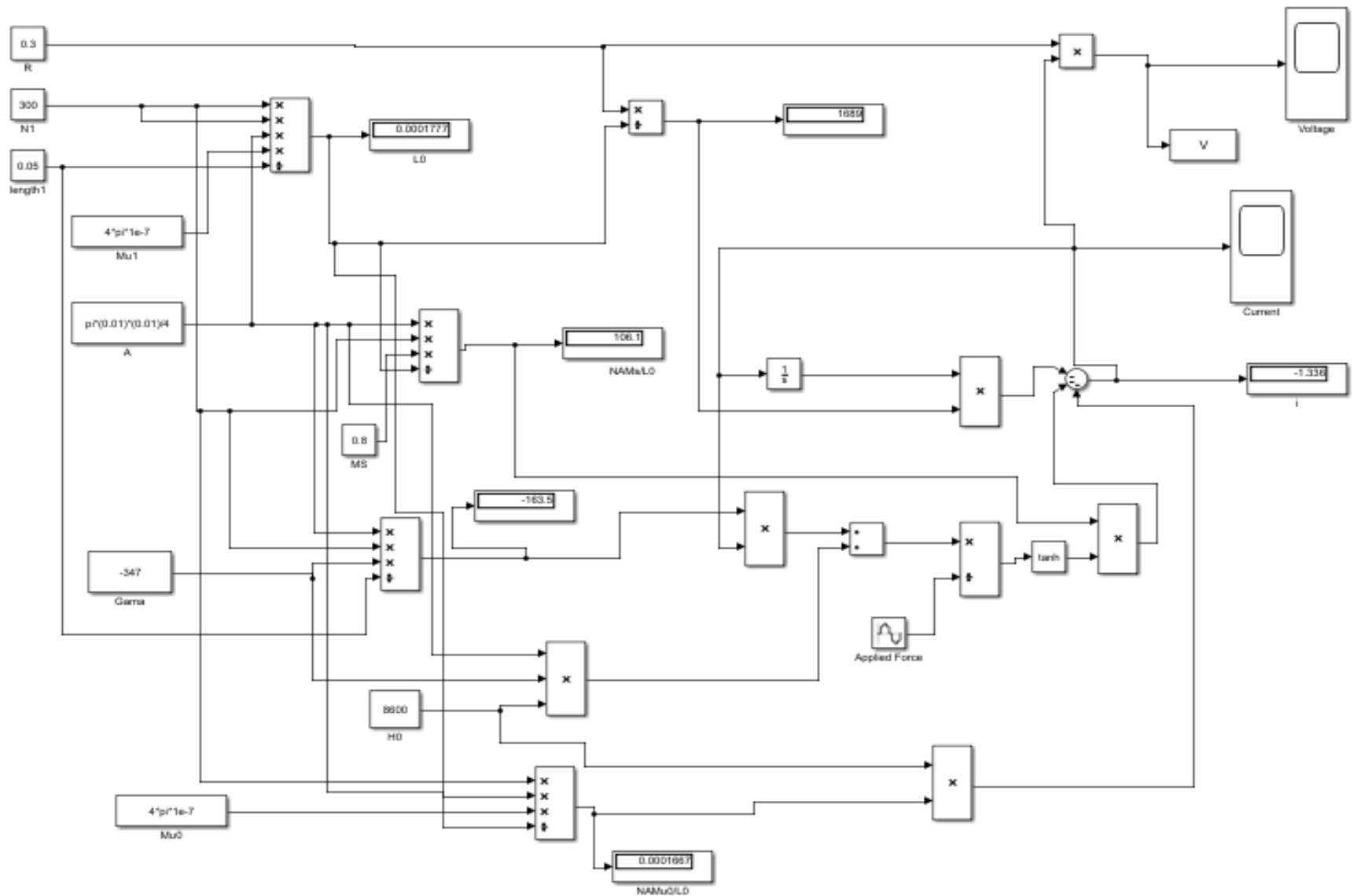
$$\begin{cases} \varepsilon = \frac{\sigma}{E} - \frac{M_s}{\gamma} \left[\frac{\gamma H}{\sigma} \tanh\left(\frac{\gamma H}{\sigma}\right) - \ln\left(\cosh\left(\frac{\gamma H}{\sigma}\right)\right) \right] \\ B = \mu_0 H + M_s \tanh\left(\frac{\gamma H}{\sigma}\right) \end{cases}$$

$$\varphi = BA = -\frac{1}{N} \int v_2 dt$$

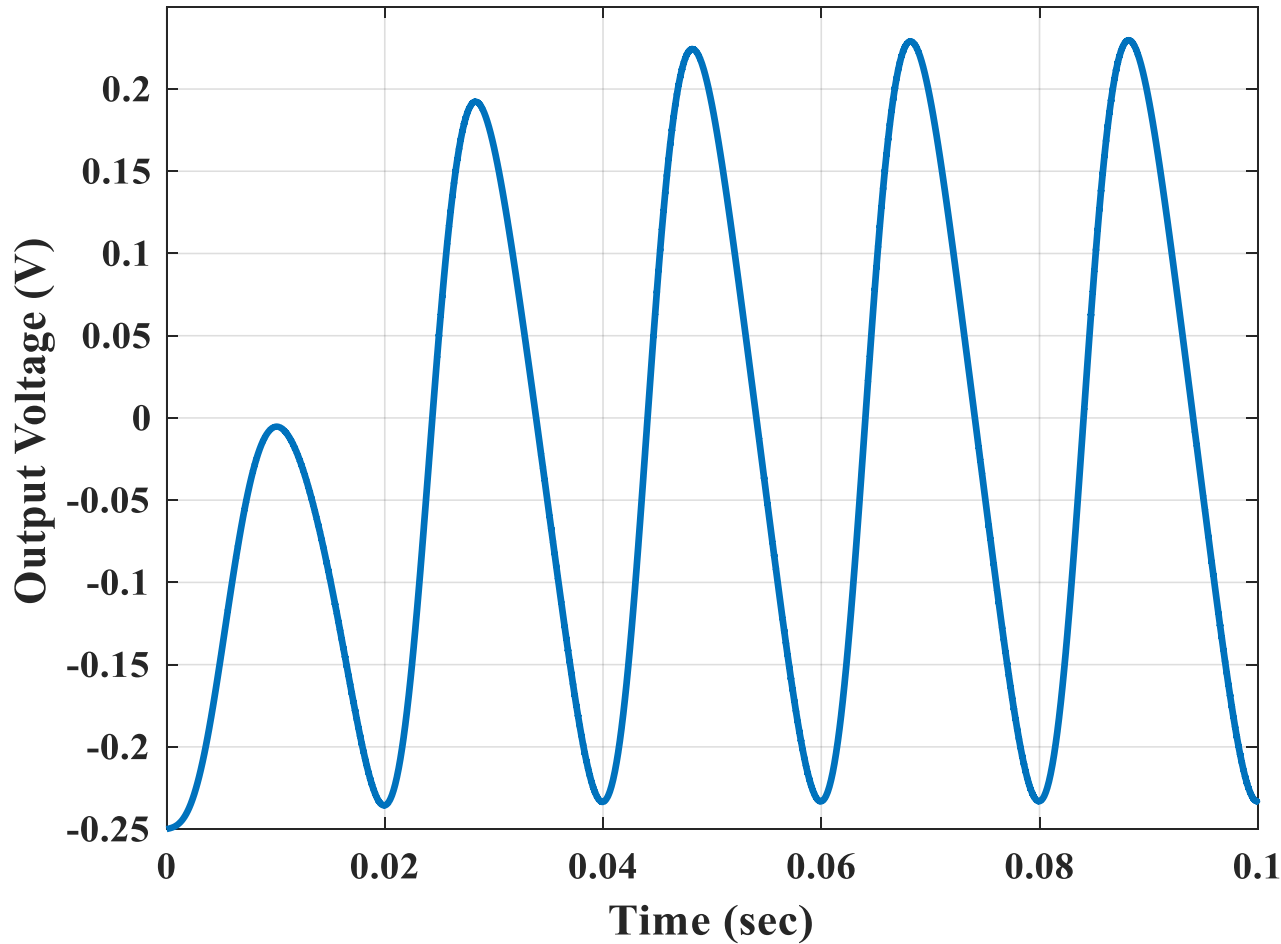


$$-\frac{R}{L_0} \int_0^\tau i_2 dt = i_2 + \frac{NAM_s}{L_0} \tanh\left(\frac{\frac{\gamma AN i_2}{l_0} + \gamma AH_0}{F_0 + F_m \cos \omega t}\right) + \frac{NA\mu_0}{L_0} H_0$$

Solve Equations: Simulation-Simulink

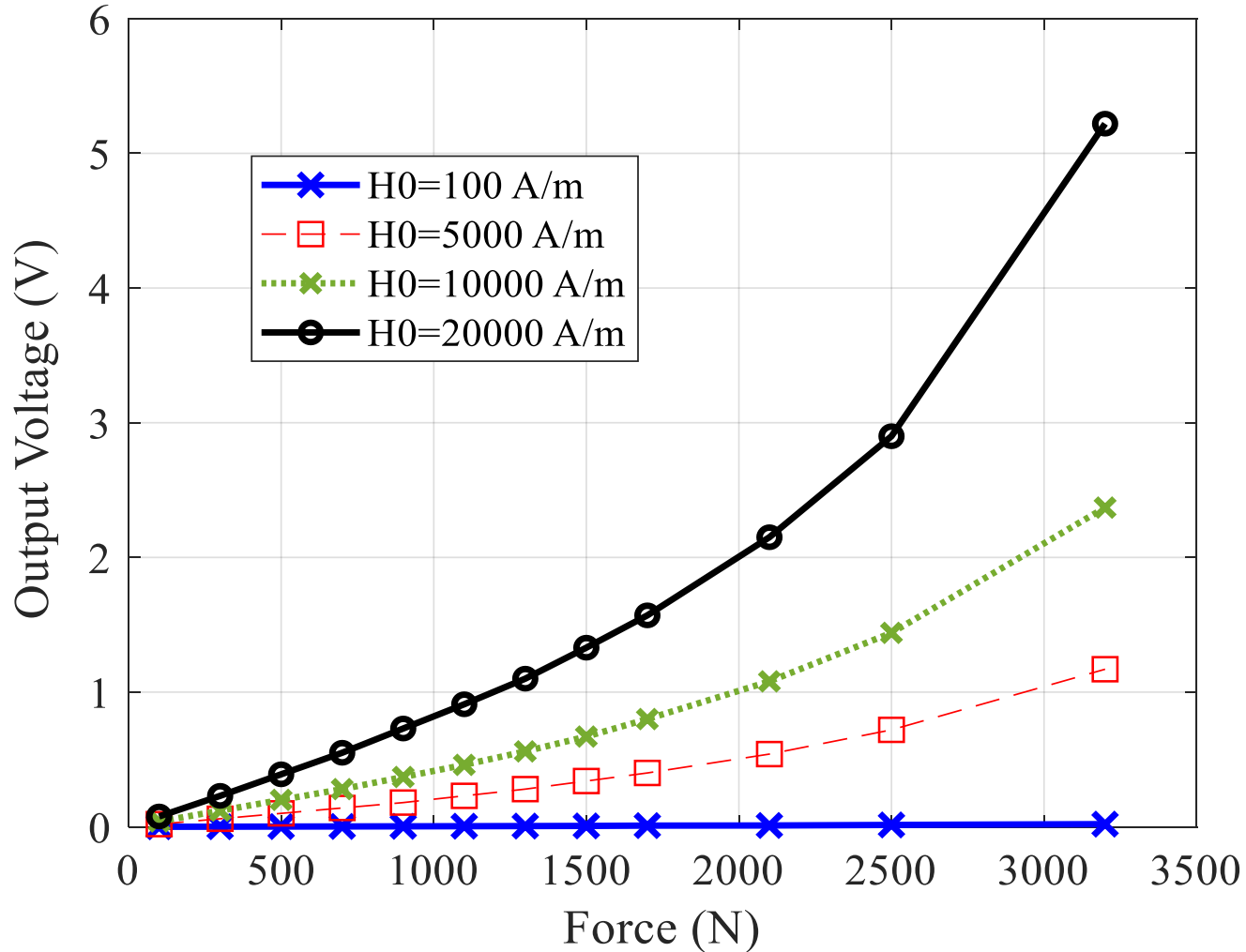


Simulation : Output Voltage of Sensor



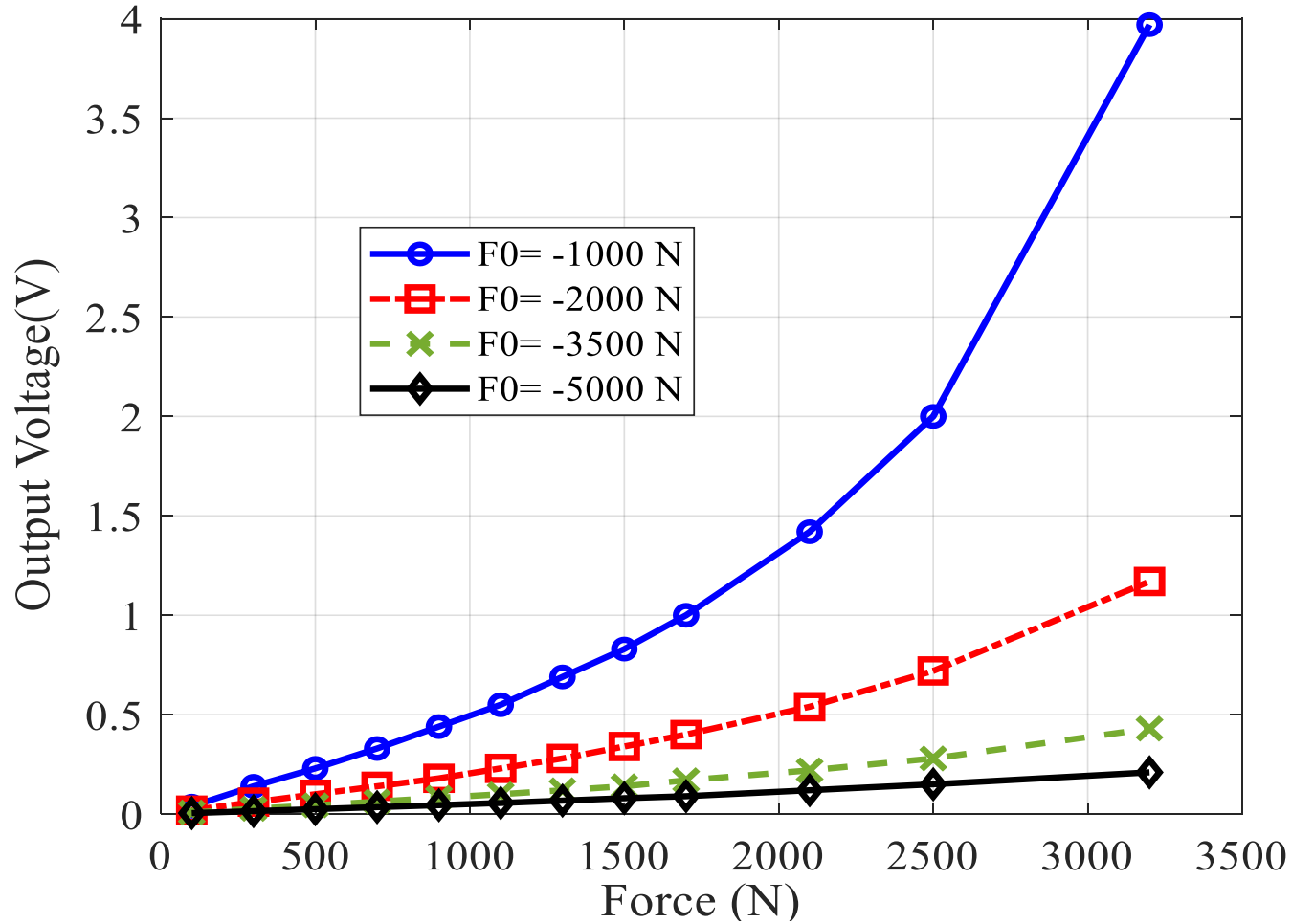
Output voltage of search coil, $R=0.3 \Omega$, $H_0=5 \text{ kA/m}$, $F_0= -1060 \text{ N}$, $F_m= 1000 \text{ N}$, $f= 50 \text{ Hz}$

Simulation result : Output Voltage



Output voltage of force sensor (V_{pp}); $R=0.3 \Omega$; $F_0 = -1000$ N

Simulation result : Output Voltage



Output voltage of force sensor (V_{pp}); $R=0.3 \Omega$; $H_0 = 5000 \text{ A/m}$

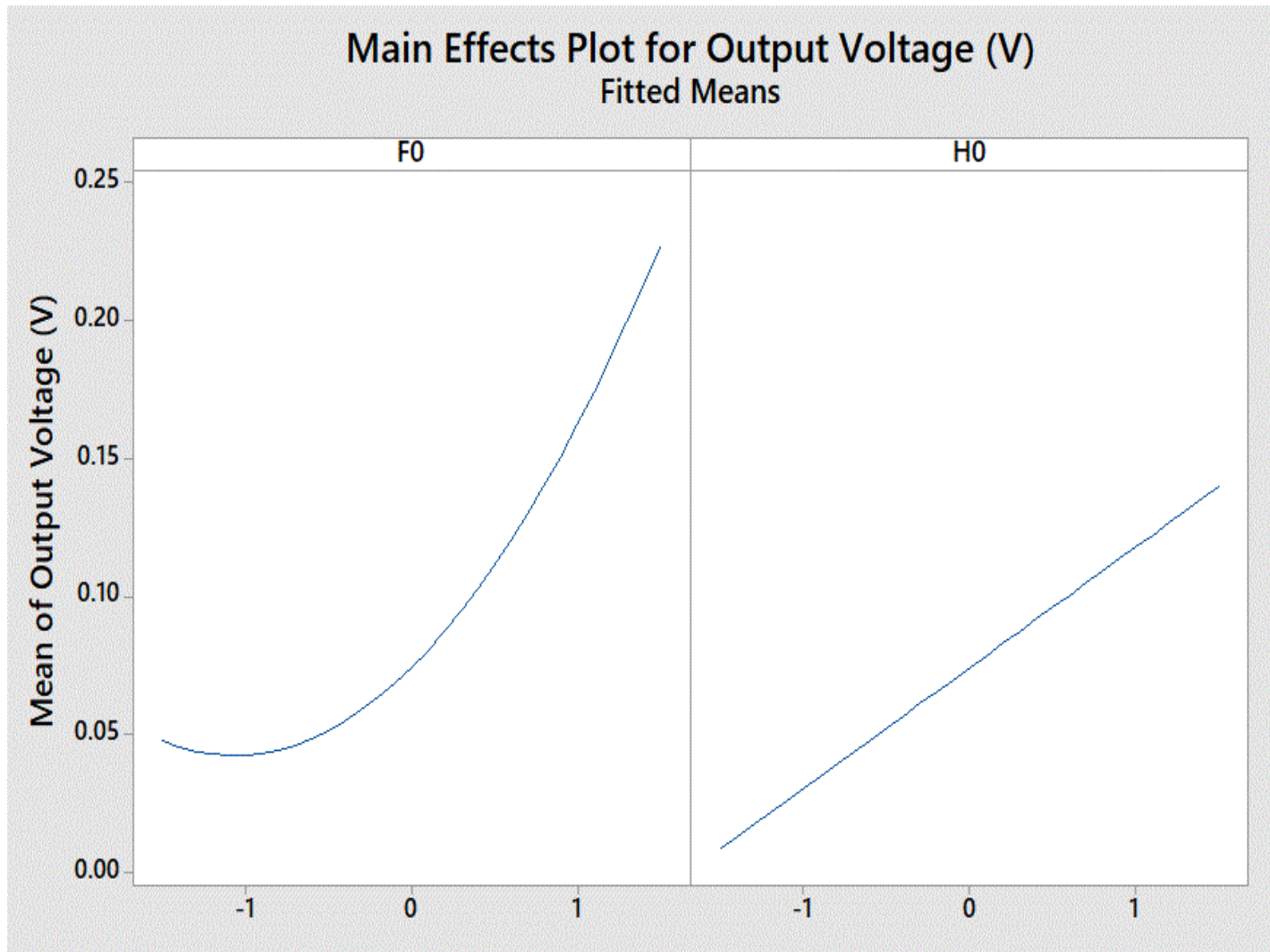
Sensitive analysis: Response Surface Method

Factors	- a	-1	0	1	+ a
F_0	-3940	-3500	-2500	-1500	-1060
H_0	1400	2500	5000	7500	8600

Order	F_0 (N)	H_0 (A/m)	V_m (v)
1	-3500	2500	0.023
2	-1500	2500	0.075
3	-3500	7500	0.07
4	-1500	7500	0.225
5	-3940	5000	0.038
6	-1060	5000	0.23
7	-2500	1400	0.0215
8	-2500	8600	0.13
9	-2500	5000	0.075

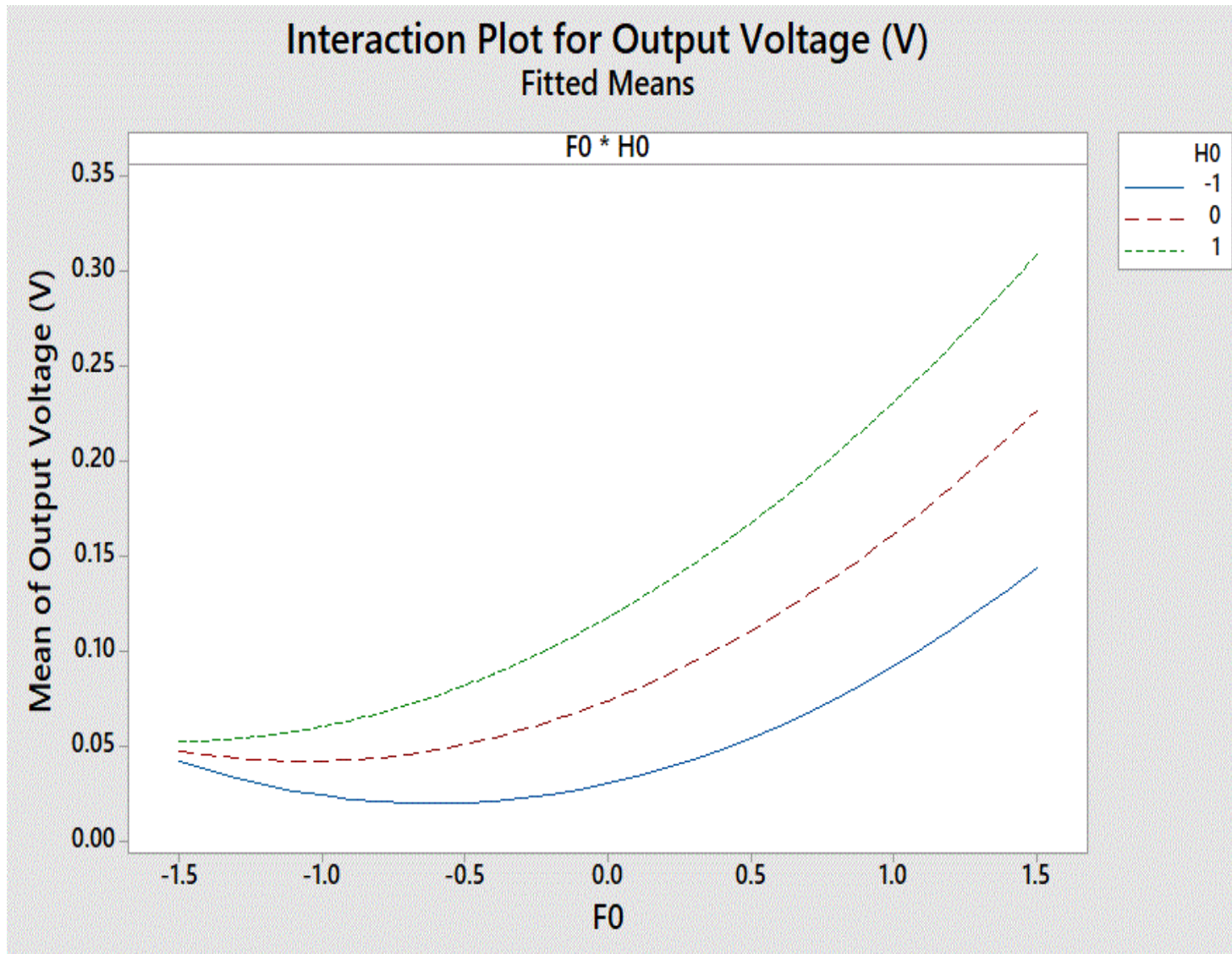
$$V = 0.07411 + 0.05982 F_0 + 0.04381 H_0 + 0.02801 F_0 \times F_0 + 0.02575 F_0 \times H_0$$

Sensitive analysis: Main Effects



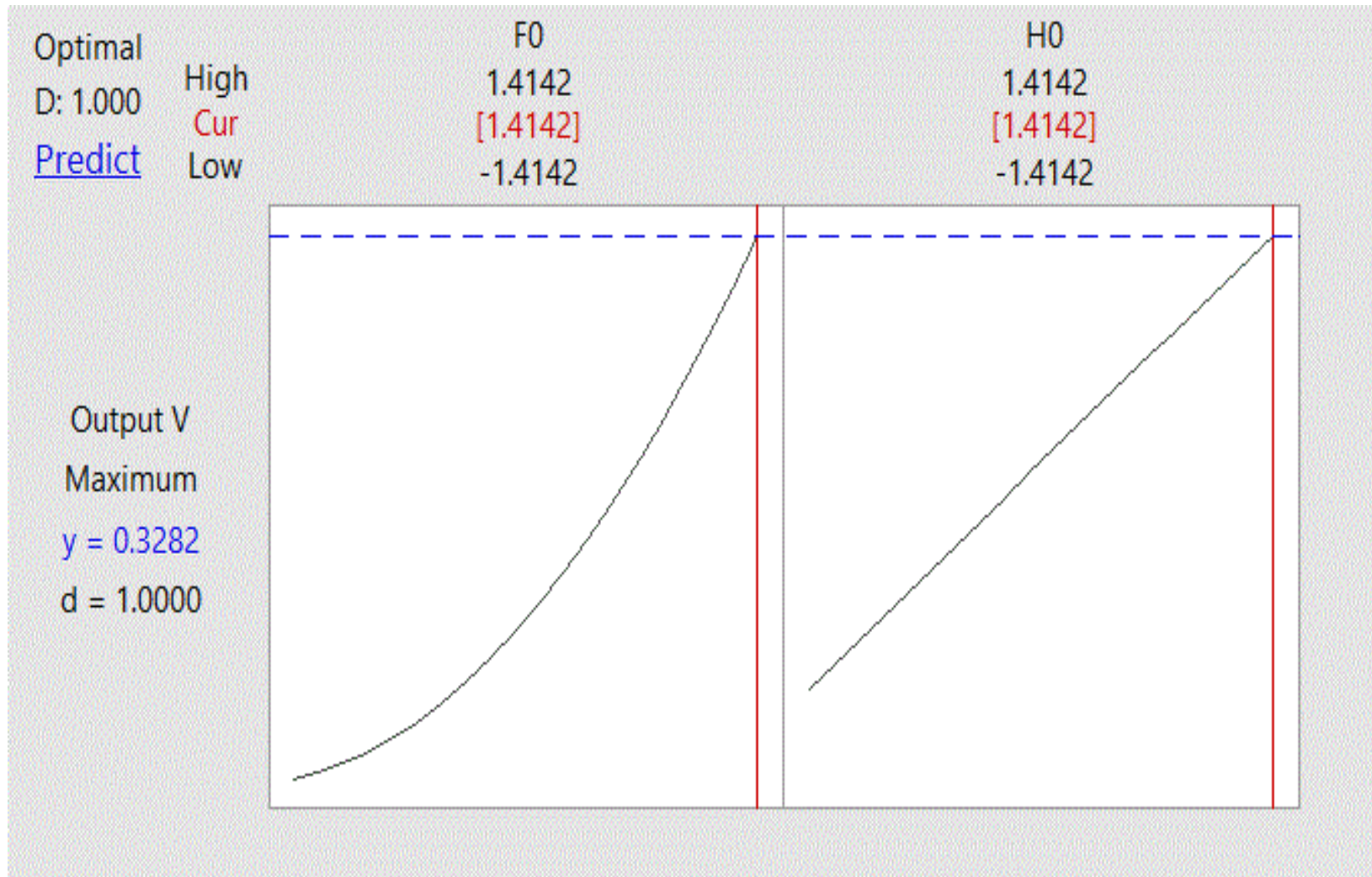
Relationship between Output voltage and main effects, F_0 and H_0

Sensitive analysis: Interactive between Factors



Interaction between F_0 and H_0

Sensitive analysis: Minitab-Optimizser



RSM optimizer to predict the maximum output

Conclusions and Future Plans:

Conclusions:

- A non-linear magneto-mechanical magnetostrictive force sensor was modeled.
- It is found that pre-stress and bias magnetic field are the significant parameter's on sensitivity and nonlinearity of the force sensors.
- Sensor's sensitivity \propto bias magnetic field.
- Sensor's linearity $\propto \frac{1}{\text{bias magnetic field}}$



- Trade-off between sensitivity and non-linearity of sensor

Future Plans:

- Verify the simulation results by experimental results