## Comparison of multiple structures in torsion angle space

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28.03 .2013
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## Introduction

Comparison of biological molecule structures (e.g. RNAs, proteins) provides an insight into the details of their folds. A crucial element of the comparison process is the choice of similarity metrics.
Structure representation in torsion angle space proves to be very useful for this purpose [1], with MCQ as a distance measure. Here, we present how it can be incorporated into the scenario of multiple structure comparison and we show the visualization of MCQ application for two use cases.

## Torsion angle space

The 3D shape of a single residue (left figure: nucleotide, right figure: amino acid) can be described by a set of torsion angles, which completely define its structure.


## Torsion angle space

The overall molecule structure can be thus represented by a set of torsion angle values provided for each residue (cf. table with selected information about 1EHZ - 76-nucleotide t-RNA).

| resid | $\alpha$ | $\beta$ | $\gamma$ | $\delta$ | $\varepsilon$ | $\zeta$ | $\chi$ | $P$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | - | -128.1 | 67.8 | 82.9 | -155.6 | -68.6 | -167.8 | 16.1 |
| 2 | -67.4 | -178.4 | 53.8 | 83.4 | -145.1 | -76.8 | -163.8 | 16.1 |
| $\ldots$ |  |  |  |  |  |  |  |  |
| 76 | -71.0 | 130.2 | 164.6 | 160.9 | - | - | 138.5 | 176.1 |

## Mean of Circular Quantities (MCQ)

Mean of circular quantities is an average of circular (e.g. angle) values. In our approach it can be used as a distance measure to compare molecule structures in torsion angle space. The following formula is applied:
$\operatorname{MCQ}\left(\mathbf{S}, \mathbf{S}^{\prime}\right)=\arctan \left(\frac{\mathbf{1}}{\mathbf{r}|\mathbf{T}|} \sum_{\mathbf{a} \in \mathbf{T}} \sum_{\mathbf{r}}^{\mathbf{i}=\mathbf{1}} \sin \boldsymbol{\Delta}\left(\mathbf{a}_{\mathbf{i}}, \mathbf{a}_{\mathbf{i}}^{\prime}\right), \frac{\mathbf{1}}{\mathbf{r}|\mathbf{T}|} \sum_{\mathbf{a} \in \mathbf{T}} \sum_{\mathbf{r}}^{\mathbf{i}=\mathbf{1}} \cos \boldsymbol{\Delta}\left(\mathbf{a}_{\mathbf{i}}, \mathbf{a}_{\mathbf{i}}^{\prime}\right)\right)$ where:

S, $\mathbf{S}^{\prime}$ - two compared structures
$\mathbf{r}$ - number of residues (the same for $\mathbf{S}$ and $\mathbf{S}^{\prime}$ )
T - a set of torsion angles
$\Delta\left(\mathbf{a}_{\mathbf{i}}, \mathbf{a}_{\mathbf{i}}^{\prime}\right)$ - function which takes into account the periodicity of angles

## MCQ parametrization

Case 1: $\mathbf{r}=$ all residues, $\mathbf{T}=$ all predefined angles Result = a single MCQ value for a pair of structures A global dissimilarity score Allows to build a dissimilarity matrix in a many-to-many comparison
Case 2: $\mathbf{r}=1, \mathbf{T}=$ all predefined angles Result = a vector of MCQ values (1 value for a pair of residues)
Allows to find fragments of high or low similarity

## Use case I: models from RNA-Puzzles

As the first use case, we have chosen RNA-Puzzles challenge 1 (dimer):

Predict the structure of the following sequence: 5'-CCGCCGCGCCAUGCCUGUGGCGG-3' knowing that the crystal structure shows a homodimer that contains two strands of the sequence that hybridize with blunt ends (C-G closing base pairs) [2].

## Use case I: models from RNA-Puzzles

A dissimilarity matrix of all submitted models was calculated and transformed into 2D visualization (classical multidimensional scaling) to show relative distances in torsion angle space.


## Use case II: NMR models

The second use case concerns 1M2F associated with 25 NMR 3D models [3]. Their comparison result is visualized as 2D colormap, where the vector of MCQ values is colored according to the distance between residues:

## Use case II: NMR models



## Software availability

The executable and source code licensed under BSD are freely available and can be downloaded from: http://www.cs.put.poznan.pl/tzok/mcq/


## References

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