

MIMO technologies used in latest generation of mobile communication systems

Andrei Alexandru Enescu, Ph D

University Politehnica of Bucharest

Faculty of Electronics, Telecommunications and Information Technology

Purposes

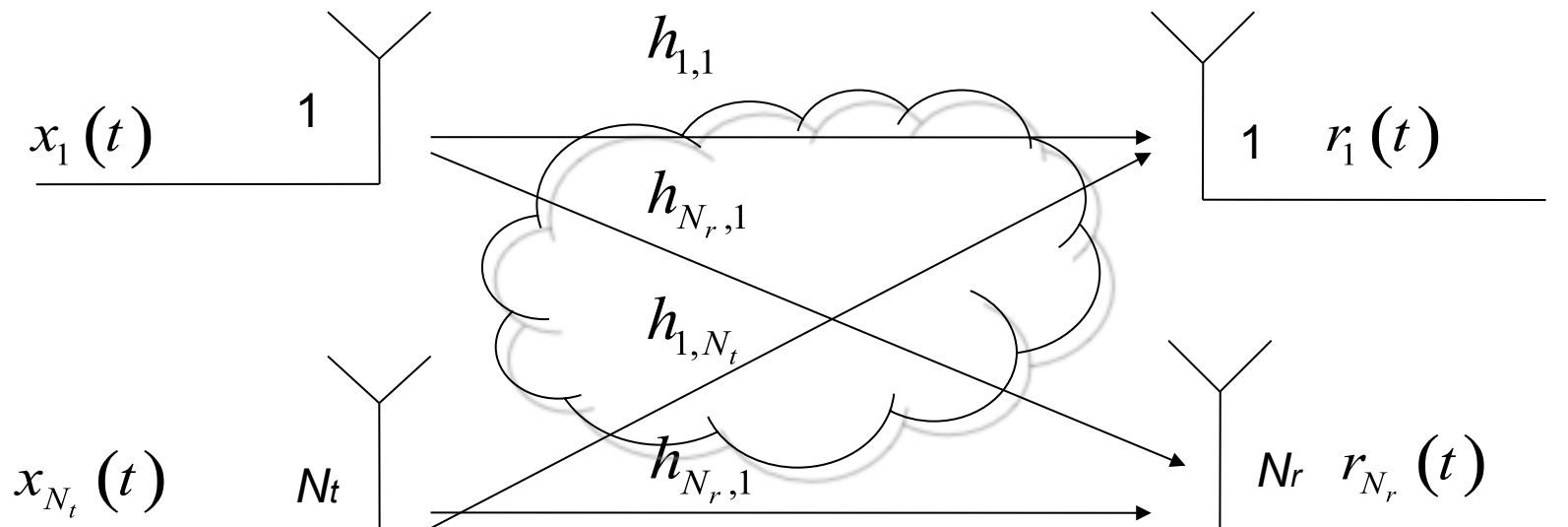
- ▶ To describe the main MIMO techniques and benefits
- ▶ To underline the constraints that exist in implementing MIMO techniques in different systems
- ▶ To give an example of the main MIMO mechanisms implemented in 4G communication systems (e.g. LTE, WiMAX)
- ▶ To propose a MIMO prototype system implemented on FPGA

Contents

- ▶ **MIMO channel**
- ▶ Spatial diversity
- ▶ Closed-loop MIMO
- ▶ MIMO – OFDM systems
- ▶ MIMO in WiMAX systems
- ▶ MIMO in LTE systems
- ▶ Case study: MCMA project

MIMO channel (1)

- ▶ MIMO = Multiple Input Multiple Output



$$r_i = \sum_{m=1}^{N_t} h_{i,m} x_m + z_i, \quad i = \overline{1, N_r}$$

MIMO channel (2)

▶ Matrix formulation

$$\mathbf{r} = \mathbf{H}\mathbf{x} + \mathbf{z} \quad \mathbf{r} = \begin{bmatrix} r_1 & \cdots & r_{N_r} \end{bmatrix}^T \quad \mathbf{z} = \begin{bmatrix} z_1 & \cdots & z_{N_r} \end{bmatrix}^T$$

$$\mathbf{H} = \begin{bmatrix} h_{1,1} & \cdots & h_{1,N_t} \\ \vdots & \ddots & \vdots \\ h_{N_r,1} & \cdots & h_{N_r,N_t} \end{bmatrix}$$

▶ Formula holds only for

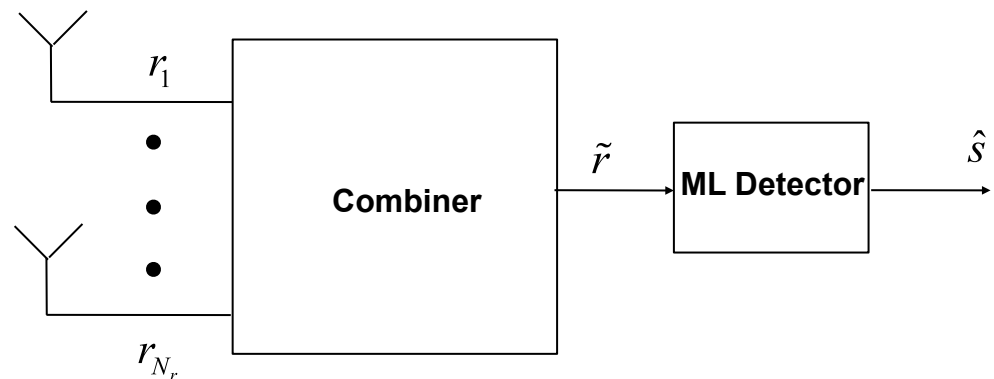
- Flat fading
 - Rich scattering environment
 - Multi-carrier systems
- Static fading
 - Fixed deployment systems

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Spatial diversity (1)

- ▶ Diversity
 - Modify the channel statistics
 - Reduce the fade margin
- ▶ Receive spatial diversity
 - Compliance to a standard is not necessary
 - Requires large antenna spacing
 - It is best to be applied over uplink
 - Brings $10\lg(N_r)$ [dB] gain for identical paths



Spatial diversity (2)

▶ Examples

- Large antenna spacing ULAs
 - Radiation pattern has many lobes
- Selection Diversity
 - Strongest received signal selected
- Equal Gain Combining
 - Received signal are summed co-phased
- Maximum Ratio Combining
 - Received signals are optimally combined, proportionally to their signal to noise ratio

Spatial diversity (3)

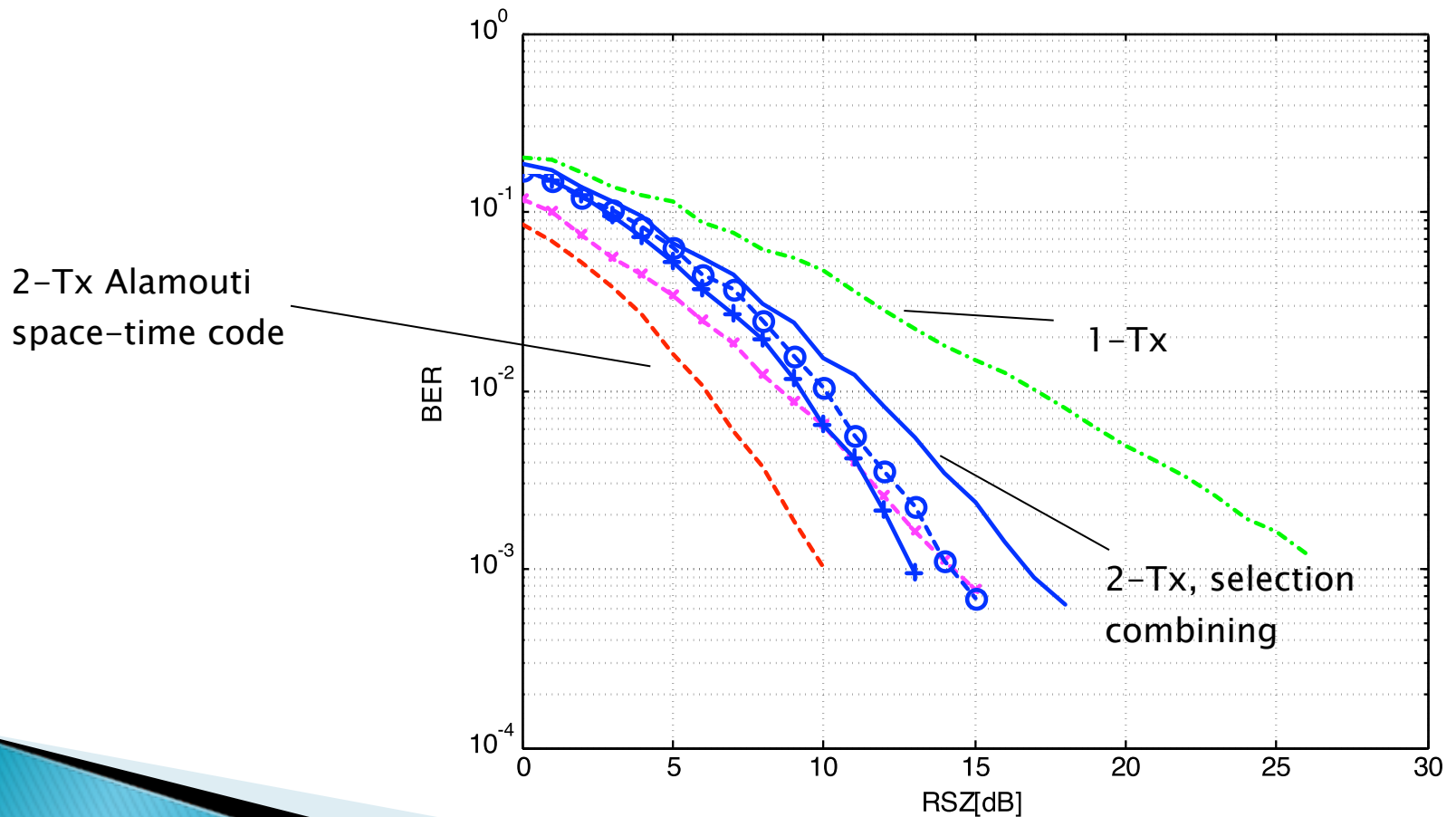
▶ Transmit diversity

- Compliance to a standard is necessary
- Requires large antenna spacing
 - It is best to be applied over downlink
- Large antenna spacing ULAs
- Space–time codes
 - Orthogonal space–time codes provide $N_t \times N_r$ order diversity
 - They exist only for 2–Tx systems (Alamouti codes)

$$\mathbf{C} = \begin{bmatrix} s_1 & -s_2^* \\ s_2 & s_1^* \end{bmatrix}$$

Spatial diversity (4)

- ▶ Diversity effects (QPSK, Rayleigh fading)



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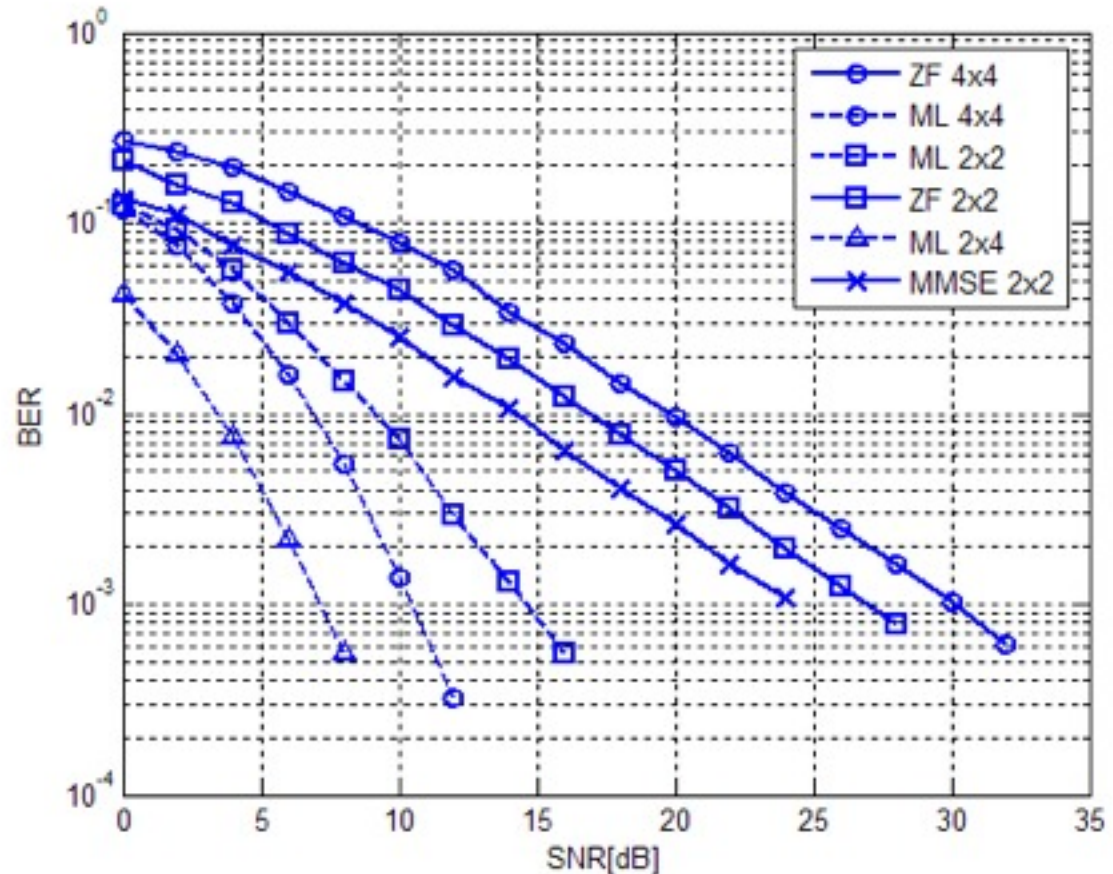
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- ▶ Spatial diversity
- ▶ **Spatial multiplexing**
- ▶ Closed-loop MIMO
- ▶ MIMO – OFDM systems
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Spatial multiplexing (1)

- ▶ Transmit antennas carry independent streams
 - Throughput increases N_t times
- ▶ Requires low correlation between propagation paths (full-rank channel matrix)
 - Large antenna spacing
- ▶ A $N_t \times N_r$ SM system achieves:
 - N_t times greater throughput
 - Spatial diversity according to the decoding algorithm
 - ML algorithm or equivalent: N_r -order
 - MMSE algorithm: approximately $N_r - N_t$ - order

Spatial multiplexing (2)

- ▶ SM decoders performances (BPSK)



Spatial multiplexing (3)

- ▶ ML-based decoders
 - Exhaustive search (e.g. 64QAM, $4 \times 4 \Rightarrow 4M$ candidates)
 - Quasi-ML: sphere decoders (Fixed, K-Best)
- ▶ Sub-optimal
 - Zero Forcing
 - Noise enhancement
 - MMSE
 - Takes noise power into account
 - Interference cancellation (SIC, PIC)

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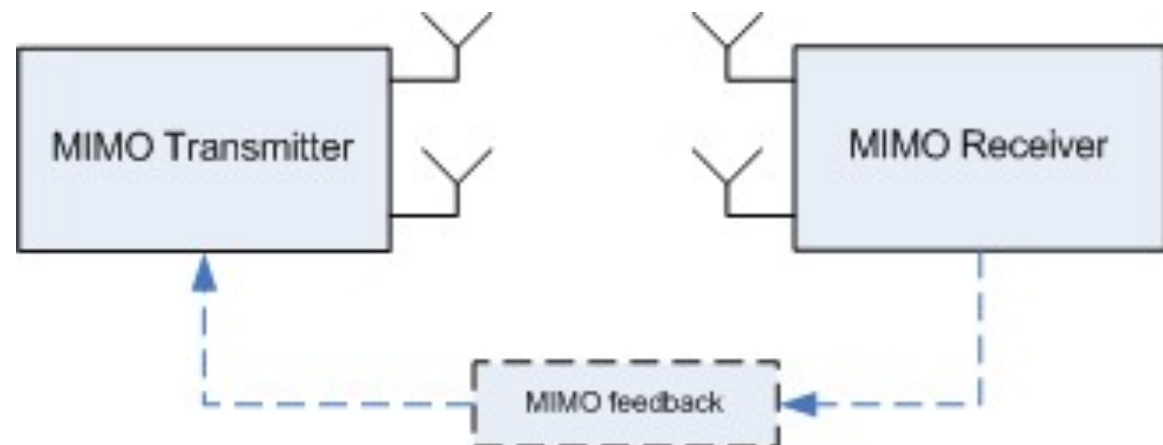
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- ▶ **Closed-loop MIMO**
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Why closed-loop MIMO?

- ▶ Choosing the right MIMO technique strongly depends on the type of channel
 - Mobile channel
 - Diversity 2x2, 4x4
 - Static fading, high SNR
 - Spatial multiplexing
 - How many layers: 2, 4 or 8?
 - Depends on the channel matrix rank

Closed-loop MIMO (1)

- ▶ CSI (Channel State Information) is provided as a feedback
 - Channel matrix coefficients
 - Channel matrix eigenvalues
 - Channel matrix rank number



Closed-loop MIMO (2)

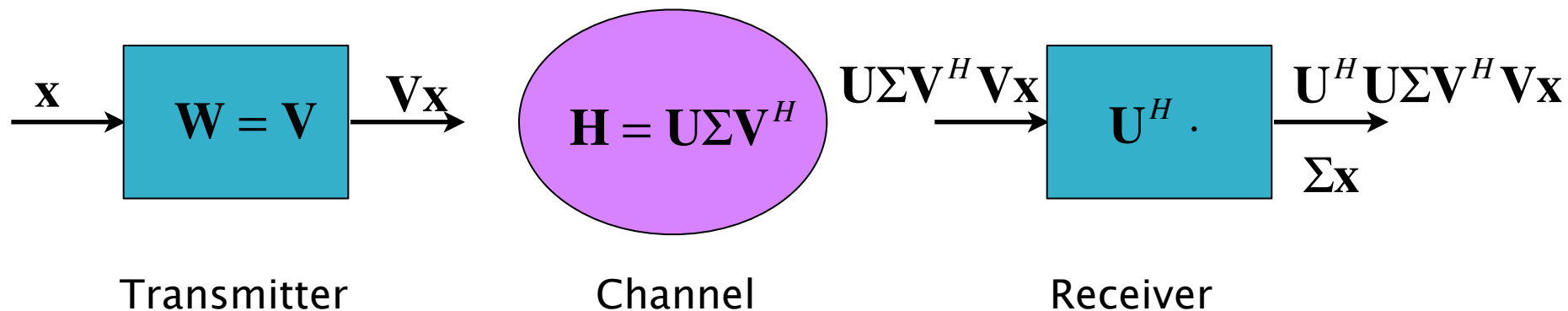
- ▶ MIMO mechanism selection
 - According to CSI feedback:
 - Mobile channel / low-rank channel => spatial diversity (3dB gain at least)
 - Static channel / full-rank channel => spatial multiplexing
- ▶ Antenna grouping
 - Different time-frequency resources use different transmit antenna pairs for space-time coding
- ▶ Antenna selection
 - Only N_t antennas are chosen from all transmit antennas for MIMO, according to CSI
- ▶ Precoding
 - Precoding matrix \mathbf{W} is applied according to the estimated matrix channel

$$\mathbf{r} = \mathbf{H}\mathbf{W}\mathbf{x} + \mathbf{z} \qquad \mathbf{W} \in \{\mathbf{P}_1, \dots, \mathbf{P}_L\}$$

MIMO Precoding

- ▶ Precoding matrix $\mathbf{r} = \mathbf{H}\mathbf{W}\mathbf{x} + \mathbf{z}$
 - Precoding matrix can be chosen in order to decouple the propagation paths
 - SVD decomposition of the channel matrix

$$\mathbf{H} = \mathbf{U}\mathbf{\Sigma}\mathbf{V}^H \quad \mathbf{I} = \mathbf{U}^H\mathbf{U} \quad \mathbf{I} = \mathbf{V}^H\mathbf{V} \quad \mathbf{\Sigma} = \text{diag}\{\sigma_i\}$$



MIMO Precoding (2)

- ▶ Equivalent channel
- ▶ Precoding matrix decouples all propagation paths

$$\mathbf{r} = \Sigma \mathbf{x} + \mathbf{z} \quad r_k = \sigma_k x_k + z_k$$

- ▶ SNR per virtual channel is equal to the singular value σ_k
- ▶ Physical interpretation
 - Transmitted signal:

$$\mathbf{W}\mathbf{x} = \begin{bmatrix} \mathbf{w}_1 & \cdots & \mathbf{w}_{N_t} \end{bmatrix} \begin{bmatrix} x_1 \\ \vdots \\ x_{N_t} \end{bmatrix}$$

MIMO Precoding (3)

- ▶ Each layer is beamformed by a vector \mathbf{w}_k
- ▶ Beams for all N_t layers are orthogonal
 - Decorrelates channel paths for the layers
 - Optimum performance
- ▶ How do we choose matrix \mathbf{W} from a predefined set?
 - PMI indicator
 - Minimize off-diagonal entries of $\mathbf{\Omega} = \mathbf{W}(\mathbf{H}^H \mathbf{H})\mathbf{W}^H$

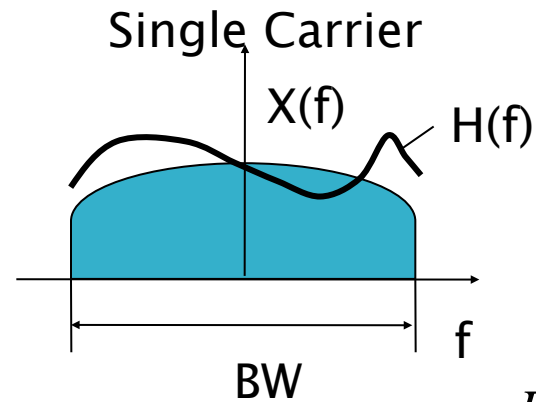
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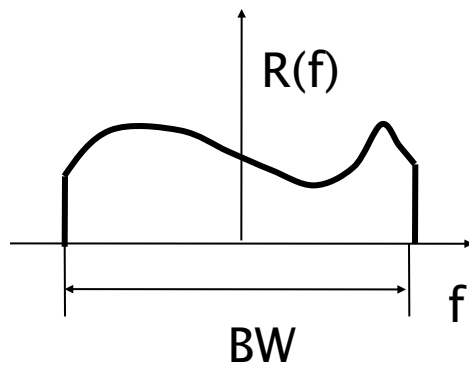
MIMO-OFDM systems (1)

- ▶ In the real-world
 - Selective fading, with coherence bandwidth $B_c \gg BW$
 - MIMO channel formula will not hold
- ▶ Solution: OFDM
 - Bandwidth is divided into K independent subbands, each of $\Delta f = BW / K \ll B_c$
 - MIMO is applied separately for each subband
 - Large computational effort
 - Examples: LTE (DL), WiMAX (512, 1024 subcarriers)

MIMO-OFDM systems (2)

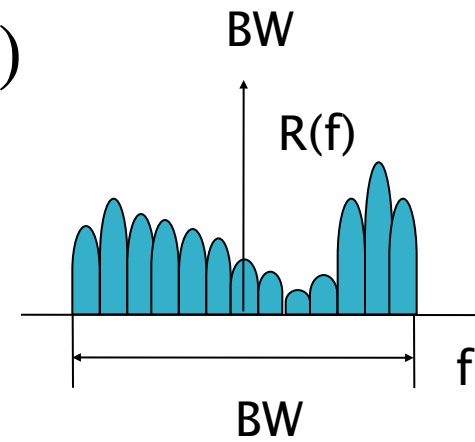
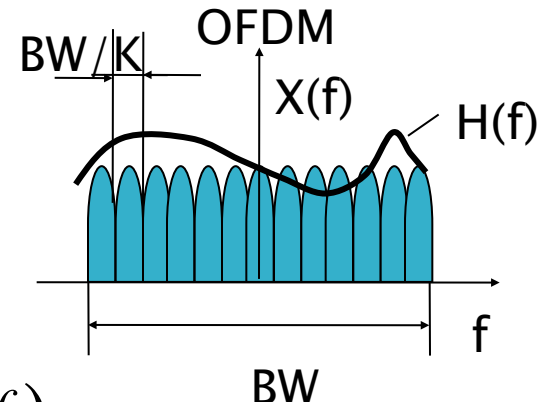


$$R(f) = H(f)X(f)$$



$$r(t) = h(t) * x(t)$$

$$\hat{x}(t) = r(t) * c(t), \text{ with } c(t) * h(t) = \delta(t)$$



$$r_k(t) = H(\omega_k)x_k(t)$$

$$x_k(t) = \frac{r_k(t)}{H(\omega_k)}$$

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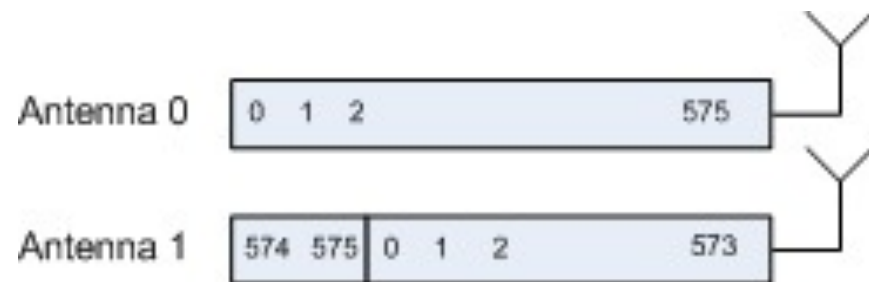
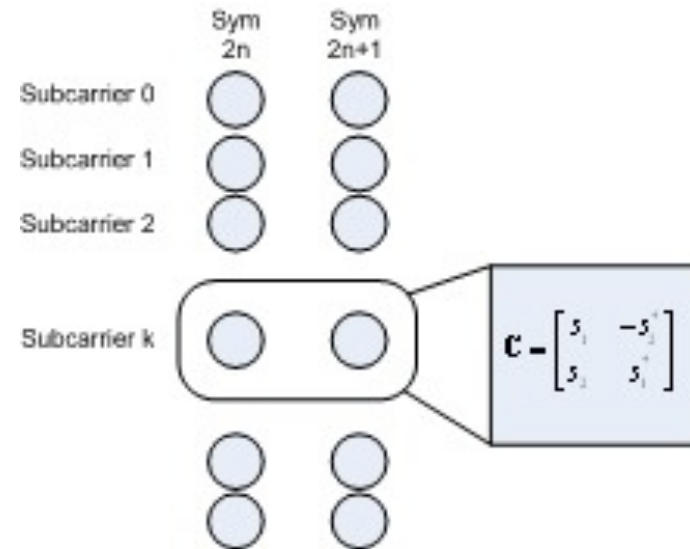
MIMO in WiMAX systems (1)

▶ Downlink

- Space-time coding (Matrix A)

- Alamouti coding

- Cyclic Delay Diversity (CDD)

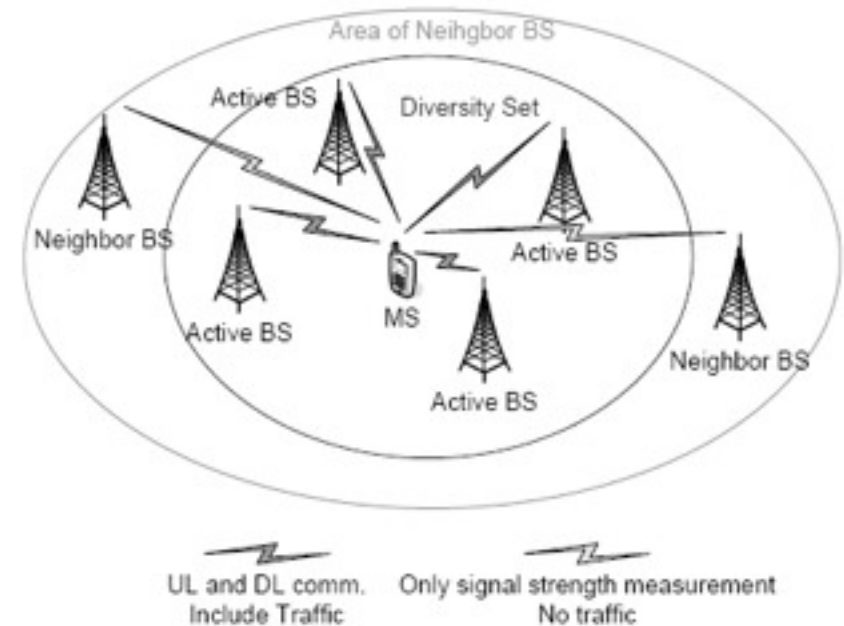


$$r_j(n) = h_{j,1}x(n) + h_{j,2}x(n-2)$$

MIMO in WiMAX systems (2)

▶ Downlink

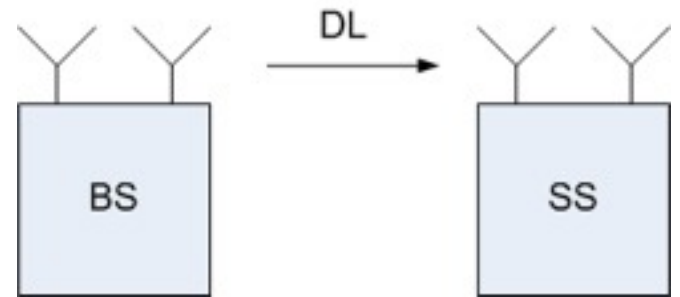
- Macro Diversity HandOver (MDHO) / Fast Base Station Switching (FBSS)
 - Soft-bit combining between two base-stations during handover
 - Diversity BSs share the same MS context



MIMO in WiMAX systems (3)

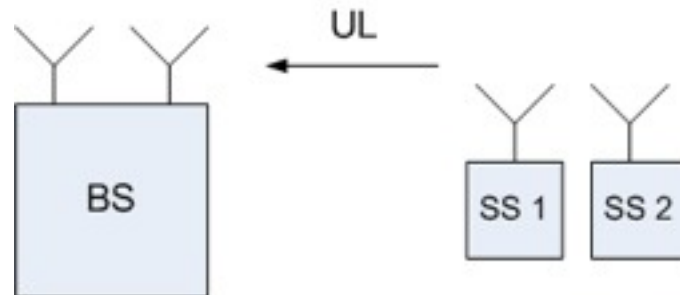
▶ Downlink

- Spatial multiplexing (Matrix B)
 - 2-Tx transmit antennas
 - Maximum spectral efficiency: $\sim 4\text{b/s/Hz}$



▶ Uplink

- Collaborative Spatial Multiplexing (CSM)
- MRC diversity scheme



MIMO in WiMAX systems (4)

- ▶ Optional techniques:
 - Precoding
 - Codebook indicated over Fast Feedback channel
 - Antenna grouping
 - Particular weighting matrix
 - Golden space-time code
 - Rate 2, full diversity
 - Adaptive Antenna Systems
 - Increase instantaneous signal to noise ratio
 - FHDC (Frequency Hopping Diversity Coding)
 - STC is applied in frequency, not in time
 - Up to 4Tx SM and STC

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MIMO in LTE systems (1)

▶ Downlink

- Spatial multiplexing using precoding (up to 4 Tx)
 - Codebook selection, based on CSI
 - MU-MIMO => SDMA
- Transmit diversity
 - Adaptive switching between STC and SM for MIMO channel rank-one

▶ Uplink

- Collaborative spatial multiplexing (MU-MIMO)
- Antenna selection: best transmit antenna out of 2

Transmit diversity

- ▶ 2-Tx
 - CDD
 - Alamouti
 - Rotation diversity
- ▶ 4-Tx
 - CDD
 - Alamouti (x2) + rotation diversity (x2)
- ▶ DFT spreading precoding
 - Equalize SNR per virtual channels, in order to avoid unequal singular values of the channel

Closed-loop MIMO

▶ Precoding matrix

- Example 4x4
 - 16 precoding matrices
- Based on 16 orthogonal Householder vectors, \mathbf{u}_n

$$\mathbf{W}_n = \mathbf{I}_4 - 2 \frac{\mathbf{u}_n \mathbf{u}_n^H}{\mathbf{u}_n^H \mathbf{u}_n}$$

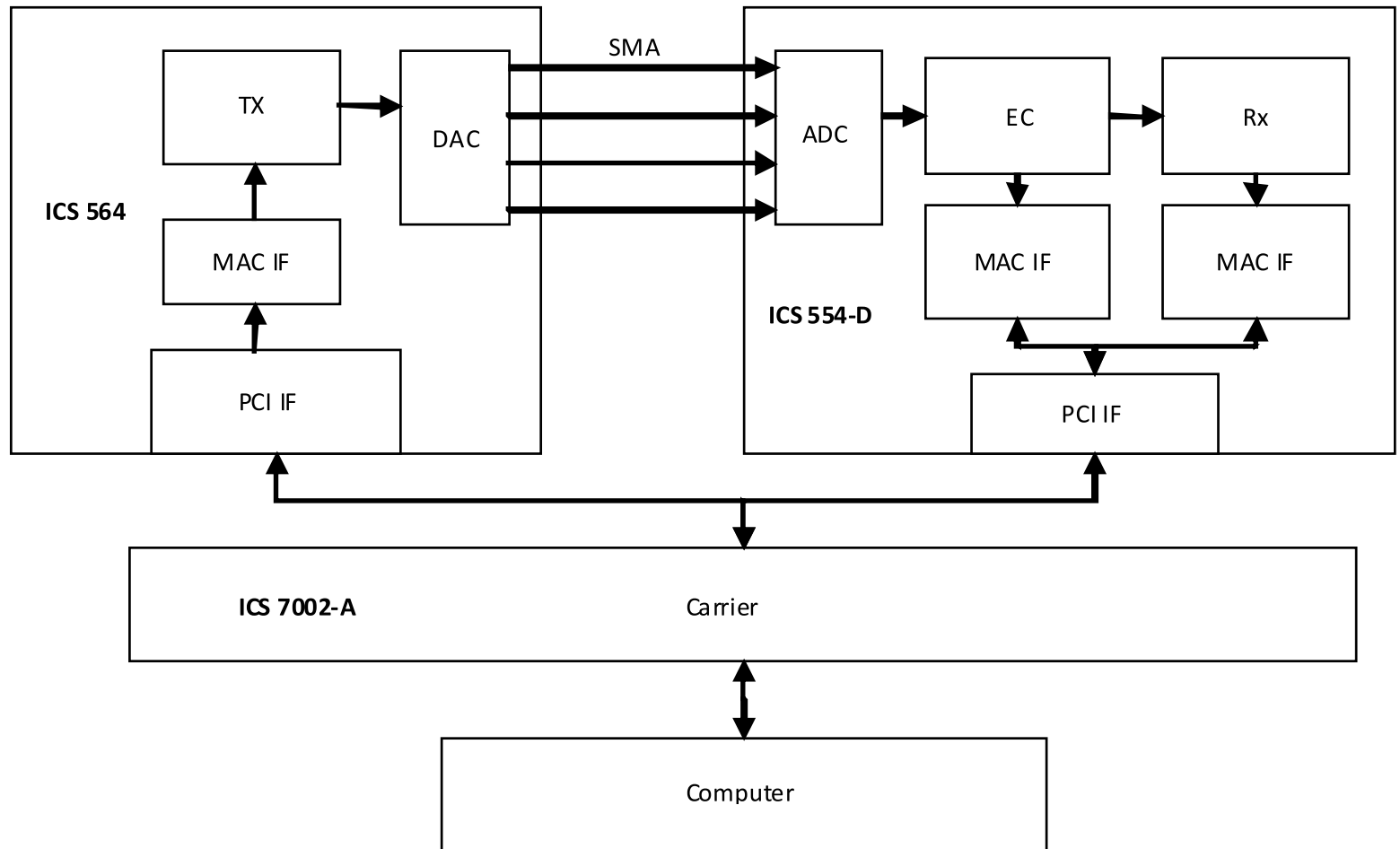
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Case study: MCMA project (1)

- ▶ Internal project, carried by a team of 6 students and 2 teachers
- ▶ Prototype system
 - App. 16Mbps . / 1.25MHz BW
 - Spectral efficiency: 12.8b/s/Hz
 - 16 subcarriers
 - 4x4 spatial multiplexing with sphere decoder, quasi-ML
 - Maximum delay spread: 1.3 μ s
 - Maximum Doppler frequency: 200Hz

Case study: MCMA project (2)



Thank you!