# Planning for Autonomous Planetary Vehicles

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- receive an *activity sequence* from Earth operators
- move on an unknown, hazardous terrain up to a specific position;
- perform some activities, e.g., acquire data;
- all of this, while dealing with strict time and resource (especially energy) constraints.

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### Main Challenges:

# © the activity sequence (plan) must be very precise in order to optimise mission time and energy consumption

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Many planners and techniques have been proposed to deal with *"planning with time and resources consumption"*. Non-optimal planners:

- MAPGEN [Bresina et al. 2005]: the user provides the planner with a qualitative evaluation of the generated plans;
- ASPEN [Chien et al. 2000]: the plan is iteratively refined to fulfill the constraints.

Optimal planners:

- TM-LPSAT [Shin&Davis 2005] and UPPAAL/TIGA [Berhmann 2007]: can handle only *linear* domains;
- MIPS [Edelkamp&Heimert 2001] manages hybrid systems but does not perform well with nonlinearity due to the use of symbolic model checking.

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Model Checking refers to algorithms and tools which take in input the formal specification of a system S and of a property  $\varphi$  and return true if  $\varphi$  is satisfied by S, or return false and give a counterexample otherwise. An Explicit Model Checker:

- **()** Obtains the transition graph of the system S
- Omputes the reachable states, starting from the initial states
- Serifies  $\varphi$  on all reachable states.

Explicit Model Checking works well on nonlinear systems.

#### How to use a Model Checker as a Planner

If we look at error states as goal states, we can use a model checker as a plan generator.

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#### UPMurphi

### Universal Planner based on CMurphi model checker

#### UPMurphi is able to:

- exploit real numbers and external C/C ++ functions to model complex systems;
- exploit several techniques (inherited from CMurphi) that help to mitigate well-known *state explosion* problem;
- reduce memory usage through bit compression and hash compaction

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### We have used UPMurphi to *automatically* generate plans to:

- model Mars environmental conditions;
- model the rover dynamics (expressed by Ordinary Differential Equations);
- control rover's **engine** to move it for a specific distance, while satisfying system constraints and minimising both time and power consumption.

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- The rover is equipped with batteries, solar panels and very limited communication and computational resources
- During each communication session, the Earth control sends to the rover a plan to drive it to the next place and perform an activity;
- The rover has no error recovery procedure: when something unexpected happens, it stops and waits for Earth instructions

#### GOAL

The rover has to move for *d<sub>final</sub>* meters minimizing time and power consumption.

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- The rover requires energy<sub>standby</sub> Joule/second energy to power the CPU;
- The rover dynamics is given by the following:

where:

a(t) is the acceleration given by the rover engine at time t

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 $\mu$  is the kinetic friction coefficient of the rover wheels.

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$$\frac{\frac{\partial v}{\partial t}}{\frac{\partial d}{\partial t}} = a(t) - \mu \cdot g$$

$$\frac{\frac{\partial d}{\partial t}}{\frac{\partial t}{\partial t}} = v(t)$$
(1)

• the energy required to move the wheels with speed v and acceleration  $\dot{v}$  is given by [Tate&Boyd 2000]:

$$f(\mathbf{v}, \dot{\mathbf{v}}) = \left(\frac{1}{2} \cdot \rho \cdot \mathbf{v}^2 \cdot Cd \cdot fa + m \cdot g \cdot \left(Crr + \frac{\dot{\mathbf{v}}}{g}\right)\right) \cdot \mathbf{v}$$
(2)

where:

ho is the Mars' air density;

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# System Constraints

## The commands that can be used to control to the rover engine are:

## Accelerate: increase acceleration by $1.5 cm/s^2$ ;

Decelerate: decrease acceleration by  $1.5 cm/s^2$ ;

Continue: continue with constant acceleration.

A correct plan (sequence of commands) for the rover engine must obey the following constraints:

- the rover speed must not exceed v<sub>max</sub> cm/s;
- the rover must stop every d<sub>max</sub> meters to perform a cooling task (needed to cool the rover's instruments);
- each cooling task lasts t<sub>c</sub> seconds and requires energy<sub>cooling</sub> Joule/second;
- after d<sub>final</sub> meters the battery charge must be higher than c<sub>min</sub> Coulomb;
- the goal must be achieved in at most t<sub>max</sub> seconds.

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- each cooling task lasts t<sub>c</sub> seconds and requires energy<sub>cooling</sub> Joule/second;
- after d<sub>final</sub> meters the battery charge must be higher than c<sub>min</sub> Coulomb;
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Accelerate: increase acceleration by  $1.5 cm/s^2$ ;

Decelerate: decrease acceleration by  $1.5 cm/s^2$ ;

Continue: continue with constant acceleration.

A correct plan (sequence of commands) for the rover engine must obey the following constraints:

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Engine blown: when the speed exceeds  $v_{max}$ , the entire mission fails;

to energy: if the energy becomes less than *c<sub>min</sub>*, the rover stops and uses the residual energy to wait for Earth instructions;

#### Plan evaluation function

The function  $C(s_i, a_i)$  evaluates the cost of a single plan step (considering time and energy). For each state  $s_i$  and for each action  $a_i$ ,  $C(s_i, a_i)$ :

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The function  $C(s_i, a_i)$  evaluates the cost of a single plan step (considering time and energy).

For each state *s*; and for each action *a*;, *C*(*s*;,*a*;):

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$$\frac{energy_{standby}^{2}}{t_{max}-i}$$
 when the rover is stopped;

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 $\frac{(energy_{standby} + energy_{cooling})^2}{t_{max} - i}$  when the rover is in a cooling phase;

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$$\frac{(energy_{standby} + f(v_i, \dot{v}_i))^2}{t_{max} - i}$$
 when the rover is moving.

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0 if the rover triggers failure conditions;

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# **Optimal Planning**

- In our experiment, we set  $d_{final} = 2m$ ,  $t_{max} = 60s$  and  $c_{min} = 1,000C$ ;
- All real variables were rounded up to first decimal digit;
- The number of different systems states, with the given variable approximation, is  $2.2 \times 10^{13}$ ;
- However, UPMurphi found that only 939,447 states were actually reachable
- UPMurphi sythesised the optimal plan (w.r.t. the given cost function) in 2,257 seconds with a peak memory requirement of 500 MB;
- Optimisation allowed us to save 922,7C w.r.t. the required minimal battery charge c<sub>min</sub>, and 17s w.r.t. the maximum allowed plan duration t<sub>max</sub>.

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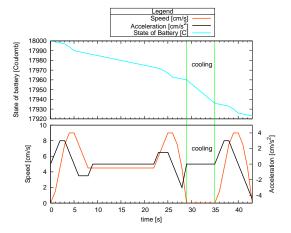
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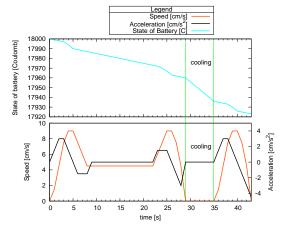


t = 0 the rover battery starts with 18,000*C* of charge and with  $v = 0, \dot{v} = 0$ 

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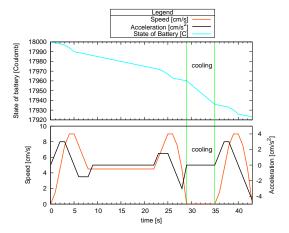


t = 5 during first 5 seconds the rover consumes a lot of energy to increase its speed

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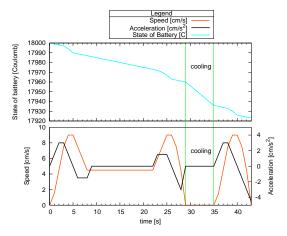


 $5 < t \le 22$  the rover reduces its speed to avoid an "engine blown" failure

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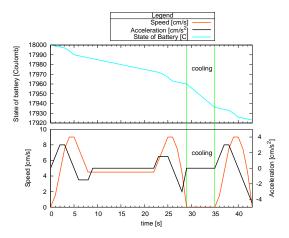


 $22 < t \leq 25$  the rover increases its speed again

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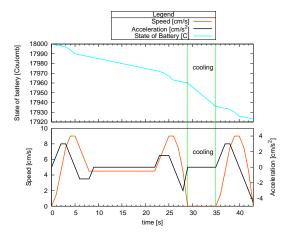


 $25 < t \le 29$  the rover brakes and stops to perform a cooling task

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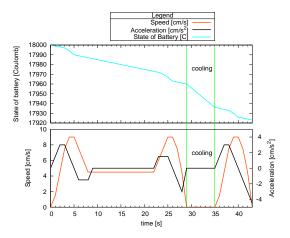


 $29 < t \le 35$  the rover performs a cooling task

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 $35 < t \le 43$  the rover covers the remaining distance to the goal.

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We showed how an explicit model checking based planner, namely UPMurphi, can be used to

- create a quite realistic model of a planetary rover (preserving its complex, nonlinear dynamics);
- generate time and resource-optimal plans to control rover engine;

Thus, UPMurphi could be an useful tool to plan activities for autonomous vehicles.

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